



## Chapter 3 – Describing Syntax and Semantics

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### CS-4337 Organization of Programming Languages

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# Chapter 3 Topics

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- Introduction
- The General Problem of Describing Syntax
- Formal Methods of Describing Syntax
- Attribute Grammars
- Describing the Meanings of Programs:  
Dynamic Semantics

# Introduction

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- Syntax: the form or structure of the expressions, statements, and program units
- Semantics: the meaning of the expressions, statements, and program units
- Syntax and semantics provide a language's definition
  - Users of a language definition
    - Other language designers
    - Implementers
    - Programmers (the users of the language)

# The General Problem of Describing Syntax:

## Terminology

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- A sentence is a string of characters over some alphabet
- A language is a set of sentences
- A lexeme is the lowest level syntactic unit of a language (e.g., `*`, `sum`, `begin`)
- A token is a category of lexemes (e.g., `identifier`)

# Example: Lexemes and Tokens

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`index = 2 * count + 17`

*Lexemes*

*Tokens*

<code>index</code>	<code>identifier</code>
<code>=</code>	<code>equal_sign</code>
<code>2</code>	<code>int_literal</code>
<code>*</code>	<code>mult_op</code>
<code>count</code>	<code>identifier</code>
<code>+</code>	<code>plus_op</code>
<code>17</code>	<code>int_literal</code>
<code>;</code>	<code>semicolon</code>

# Formal Definition of Languages

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- Recognizers

- A recognition device reads input strings over the alphabet of the language and decides whether the input strings belong to the language
- Example: syntax analysis part of a compiler
  - Detailed discussion of syntax analysis appears in Chapter 4

- Generators

- A device that generates sentences of a language
- One can determine if the syntax of a particular sentence is syntactically correct by comparing it to the structure of the generator

# Formal Methods of Describing Syntax

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- Formal language-generation mechanisms, usually called **grammars**, are commonly used to describe the syntax of programming languages.

# BNF and Context-Free Grammars

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- Context-Free Grammars
  - Developed by Noam Chomsky in the mid-1950s
  - Language generators, meant to describe the syntax of natural languages
  - Define a class of languages called context-free languages
- Backus-Naur Form (1959)
  - Invented by John Backus to describe the syntax of Algol 58
  - BNF is equivalent to context-free grammars



# BNF Fundamentals

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- In BNF, abstractions are used to represent classes of syntactic structures — they act like syntactic variables (also called non-terminal symbols, or just non-terminals)
- Terminals are lexemes or tokens
- A rule has a left-hand side (LHS), which is a nonterminal, and a right-hand side (RHS), which is a string of terminals and/or nonterminals

# BNF Fundamentals (continued)

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- Nonterminals are often enclosed in angle brackets
  - Examples of BNF rules:  
`<ident_list> → identifier | identifier, <ident_list>`  
`<if_stmt> → if <logic_expr> then <stmt>`
- Grammar: a finite non-empty set of rules
- A start symbol is a special element of the nonterminals of a grammar

# BNF Rules

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- An abstraction (or nonterminal symbol) can have more than one RHS

$$\begin{aligned} \langle \text{stmt} \rangle &\rightarrow \langle \text{single\_stmt} \rangle \\ &\quad | \text{ **begin** } \langle \text{stmt\_list} \rangle \text{ **end** } \end{aligned}$$

- The same as...

$$\begin{aligned} \langle \text{stmt} \rangle &\rightarrow \langle \text{single\_stmt} \rangle \\ \langle \text{stmt} \rangle &\rightarrow \text{ **begin** } \langle \text{stmt\_list} \rangle \text{ **end** } \end{aligned}$$

# Describing Lists

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- Syntactic lists are described using recursion

$$\begin{aligned} \langle \text{ident\_list} \rangle &\rightarrow \text{ident} \\ &\quad | \text{ident}, \langle \text{ident\_list} \rangle \end{aligned}$$

- A derivation is a repeated application of rules, starting with the start symbol and ending with a sentence (all terminal symbols)

# An Example Grammar

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$\langle \text{program} \rangle \rightarrow \langle \text{stmts} \rangle$

$\langle \text{stmts} \rangle \rightarrow \langle \text{stmt} \rangle \mid \langle \text{stmt} \rangle ; \langle \text{stmts} \rangle$

$\langle \text{stmt} \rangle \rightarrow \langle \text{var} \rangle = \langle \text{expr} \rangle$

$\langle \text{var} \rangle \rightarrow \mathbf{a} \mid \mathbf{b} \mid \mathbf{c} \mid \mathbf{d}$

$\langle \text{expr} \rangle \rightarrow \langle \text{term} \rangle + \langle \text{term} \rangle \mid \langle \text{term} \rangle - \langle \text{term} \rangle$

$\langle \text{term} \rangle \rightarrow \langle \text{var} \rangle \mid \mathbf{const}$

# An Example Derivation

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$\langle \text{program} \rangle \Rightarrow \langle \text{stmts} \rangle$   
 $\Rightarrow \langle \text{stmt} \rangle$   
 $\Rightarrow \langle \text{var} \rangle = \langle \text{expr} \rangle$   
 $\Rightarrow a = \langle \text{expr} \rangle$   
 $\Rightarrow a = \langle \text{term} \rangle + \langle \text{term} \rangle$   
 $\Rightarrow a = \langle \text{var} \rangle + \langle \text{term} \rangle$   
 $\Rightarrow a = b + \langle \text{term} \rangle$   
 $\Rightarrow a = b + \text{const}$

# Derivations

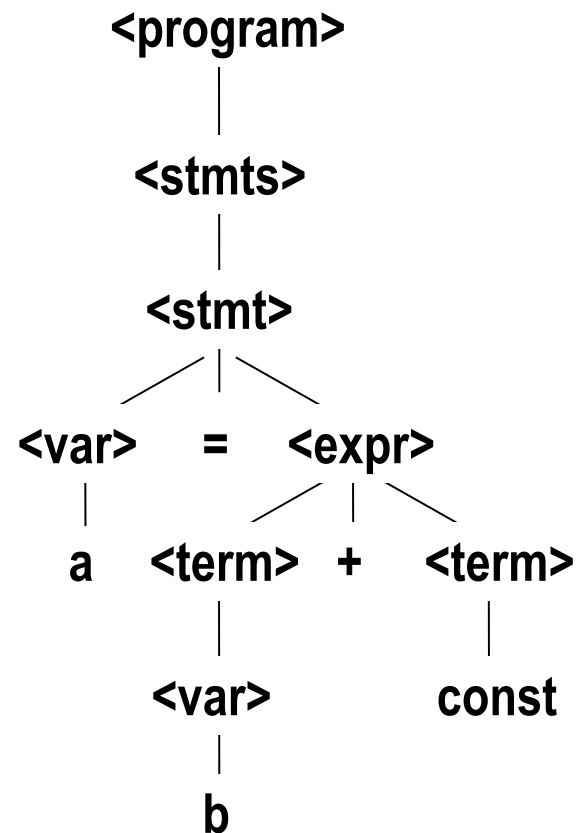
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- Every string of symbols in a derivation is a sentential form
- A sentence is a sentential form that has only terminal symbols
- A leftmost derivation is one in which the leftmost nonterminal in each sentential form is the one that is expanded
- A derivation may be neither leftmost nor rightmost

# Parse Tree

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- A hierarchical representation of a derivation



**a = b + const**



# Ambiguity in Grammars

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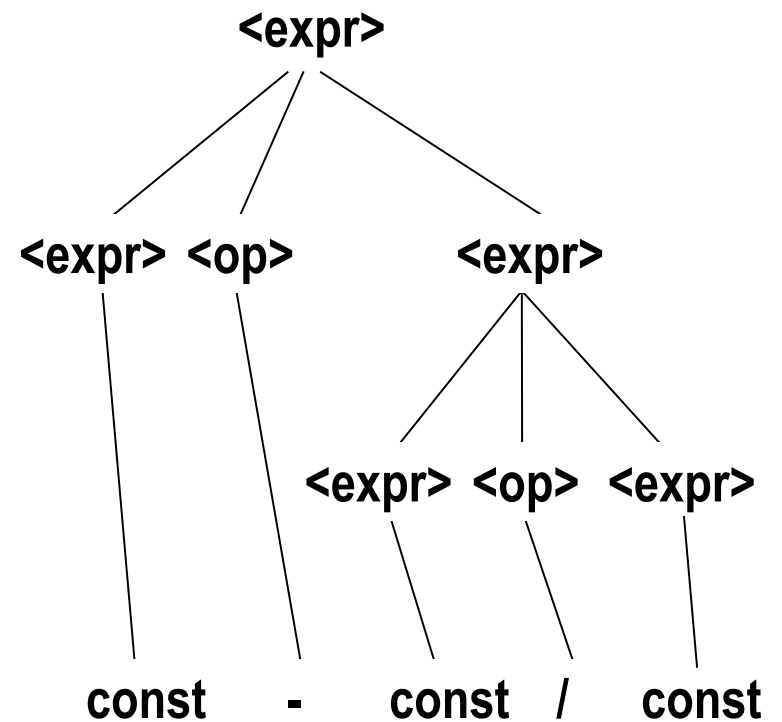
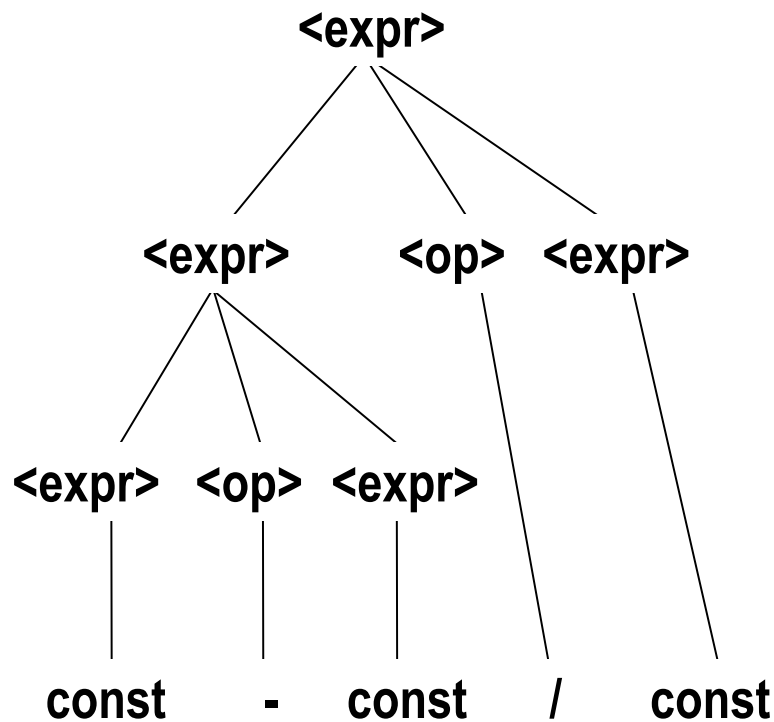
- A grammar is ambiguous if and only if it generates a sentential form that has two or more distinct parse trees

# An Ambiguous Expression Grammar

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$\langle \text{expr} \rangle \rightarrow \langle \text{expr} \rangle \langle \text{op} \rangle \langle \text{expr} \rangle \mid \text{const}$

$\langle \text{op} \rangle \rightarrow / \mid -$



# Ambiguous Grammars

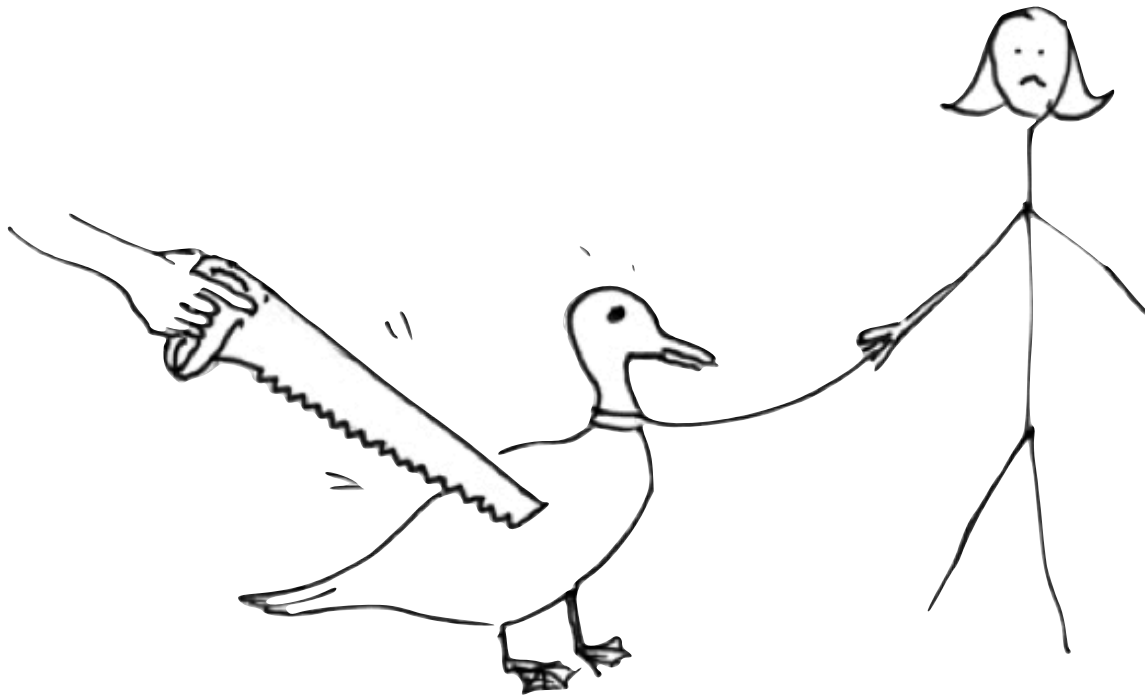
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- “I saw her duck”

# Ambiguous Grammars

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- “I saw her duck”



# Ambiguous Grammars

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“The men saw a boy in the park with a telescope”

# Logical Languages

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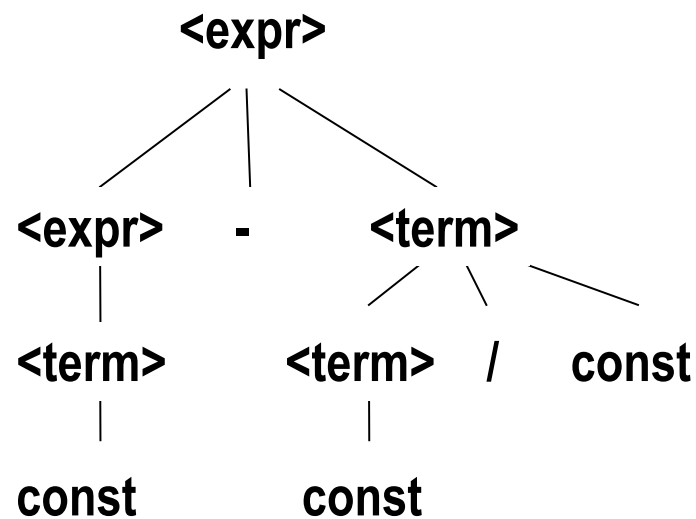
- LOGLAN (1955)
  - Grammar based on predicate logic
  - Developed Dr. James Cooke Brown with the goal of making a language so different from natural languages that people learning it would think in a different way if the hypothesis were true
  - Loglan is the first among, and the main inspiration for, the languages known as logical languages, which also includes **Lojban** and **Ceqli**.
  - To investigate the Sapir-Whorf Hypothesis

# An Unambiguous Expression Grammar

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- If we use the parse tree to indicate precedence levels of the operators, we cannot have ambiguity

$\langle \text{expr} \rangle \rightarrow \langle \text{expr} \rangle - \langle \text{term} \rangle \mid \langle \text{term} \rangle$   
 $\langle \text{term} \rangle \rightarrow \langle \text{term} \rangle / \text{const} \mid \text{const}$



# Operator Precedence

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- If we use the parse tree to indicate precedence levels of the operators, we cannot have ambiguity

$\langle \text{assign} \rangle \rightarrow \langle \text{id} \rangle = \langle \text{expr} \rangle$

$\langle \text{id} \rangle \rightarrow \mathbf{A} \mid \mathbf{B} \mid \mathbf{C}$

$\langle \text{expr} \rangle \rightarrow \langle \text{expr} \rangle + \langle \text{term} \rangle \mid \langle \text{term} \rangle$

$\langle \text{term} \rangle \rightarrow \langle \text{term} \rangle * \langle \text{factor} \rangle \mid \langle \text{factor} \rangle$

$\langle \text{factor} \rangle \rightarrow ( \langle \text{expr} \rangle ) \mid \langle \text{id} \rangle$



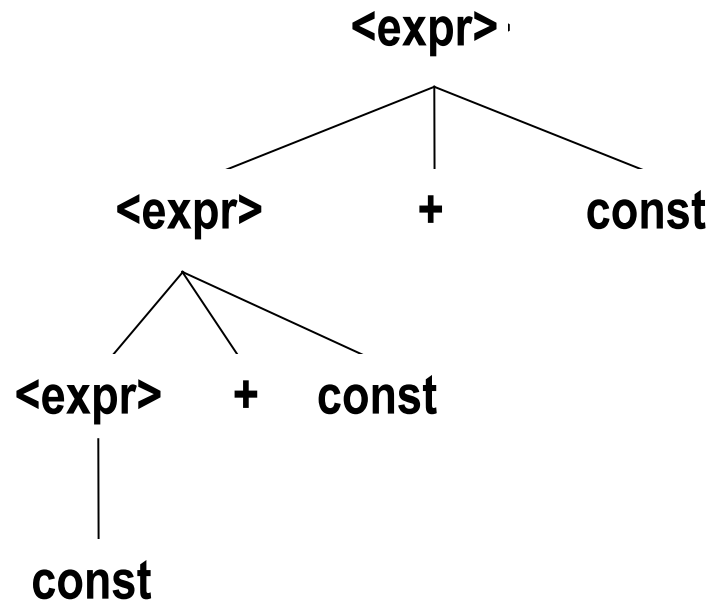
# Associativity of Operators

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- Operator associativity can also be indicated by a grammar

$\langle \text{expr} \rangle \rightarrow \langle \text{expr} \rangle + \langle \text{expr} \rangle \mid \mathbf{const}$  (ambiguous)

$\langle \text{expr} \rangle \rightarrow \langle \text{expr} \rangle + \mathbf{const} \mid \mathbf{const}$  (unambiguous)



# Extended BNF

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- Optional parts are placed in brackets [ ]

`<proc_call> → ident [(<expr_list>)]`

- Alternative parts of RHSs are placed inside parentheses and separated via vertical bars

`<term> → <term> (+|-) const`

- Repetitions (0 or more) are placed inside braces { }

`<ident_list> → <identifier> {, <identifier>}`

# BNF and EBNF

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- BNF

```
<expr> → <term> |  
        <expr> + <term> |  
        <expr> - <term>  
<term> → <factor> |  
        <term> * <factor> |  
        <term> / <factor>
```

- EBNF

```
<expr> → <term> { (+ | -) <term> }  
<term> → <factor> { (* | /) <factor> }
```

# Recent Variations in EBNF

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- Alternative RHSs are put on separate lines
- Use of a colon instead of  $\Rightarrow$
- Use of `opt` for optional parts
- Use of `oneof` for choices

# Attribute Grammars

# Static Semantics

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- Nothing to do with meaning
- Context-free grammars (CFGs) cannot describe all of the syntax of programming languages
- Categories of constructs that are trouble:
  - Context-free, but cumbersome (e.g., types of operands in expressions)
  - Non-context-free (e.g., variables must be declared before they are used)

# Attribute Grammars

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- Attribute grammars (AGs) have additions to CFGs to carry some semantic info on parse tree nodes
- Primary value of AGs:
  - Static semantics specification
  - Compiler design (static semantics checking)

# Attribute Grammars : Definition

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- **Def:** An attribute grammar is a context-free grammar  $G = (S, N, T, P)$  with the following additions:
  - For each grammar symbol  $x$  there is a set  $A(x)$  of attribute values
  - Each rule has a set of functions that define certain attributes of the nonterminals in the rule
  - Each rule has a (possibly empty) set of predicates to check for attribute consistency



# Attribute Grammars: Definition

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- Let  $X_0 \rightarrow X_1 \dots X_n$  be a rule
- Functions of the form  $S(X_0) = f(A(X_1), \dots, A(X_n))$  define synthesized attributes
- Functions of the form  $I(X_j) = f(A(X_0), \dots, A(X_n))$ , for  $i \leq j \leq n$ , define inherited attributes
- Initially, there are intrinsic attributes on the leaves

# Attribute Grammars: An Example

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- **Syntax rule:**

```
<proc_def> → procedure <proc_name>[1]  
<proc_body> end <proc_name>[2];
```

- **Predicate:**

```
<proc_name>[1].string == <proc_name>[2].string
```

# Attribute Grammars: An Example

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- **Syntax**

$\langle \text{assign} \rangle \rightarrow \langle \text{var} \rangle = \langle \text{expr} \rangle$

$\langle \text{expr} \rangle \rightarrow \langle \text{var} \rangle + \langle \text{var} \rangle \mid \langle \text{var} \rangle$

$\langle \text{var} \rangle \rightarrow \mathbf{A} \mid \mathbf{B} \mid \mathbf{C}$

- `actual_type`: synthesized for `<var>` and `<expr>`
- `expected_type`: inherited for `<expr>`

# Attribute Grammar (continued)

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- **Syntax rule:**  $\langle \text{expr} \rangle \rightarrow \langle \text{var} \rangle[1] + \langle \text{var} \rangle[2]$

**Semantic rules:**

$\langle \text{expr} \rangle.\text{actual\_type} \leftarrow \langle \text{var} \rangle[1].\text{actual\_type}$

**Predicate:**

$\langle \text{var} \rangle[1].\text{actual\_type} == \langle \text{var} \rangle[2].\text{actual\_type}$

$\langle \text{expr} \rangle.\text{expected\_type} == \langle \text{expr} \rangle.\text{actual\_type}$

- **Syntax rule:**  $\langle \text{var} \rangle \rightarrow \text{id}$

**Semantic rule:**

$\langle \text{var} \rangle.\text{actual\_type} \leftarrow \text{lookup} (\langle \text{var} \rangle.\text{string})$

# Attribute Grammars (continued)

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- How are attribute values computed?
  - If all attributes were inherited, the tree could be decorated in top-down order.
  - If all attributes were synthesized, the tree could be decorated in bottom-up order.
  - In many cases, both kinds of attributes are used, and it is some combination of top-down and bottom-up that must be used.

## Attribute Grammars (continued)

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`<expr>.expected_type ← inherited from parent`

`<var>[1].actual_type ← lookup (A)`

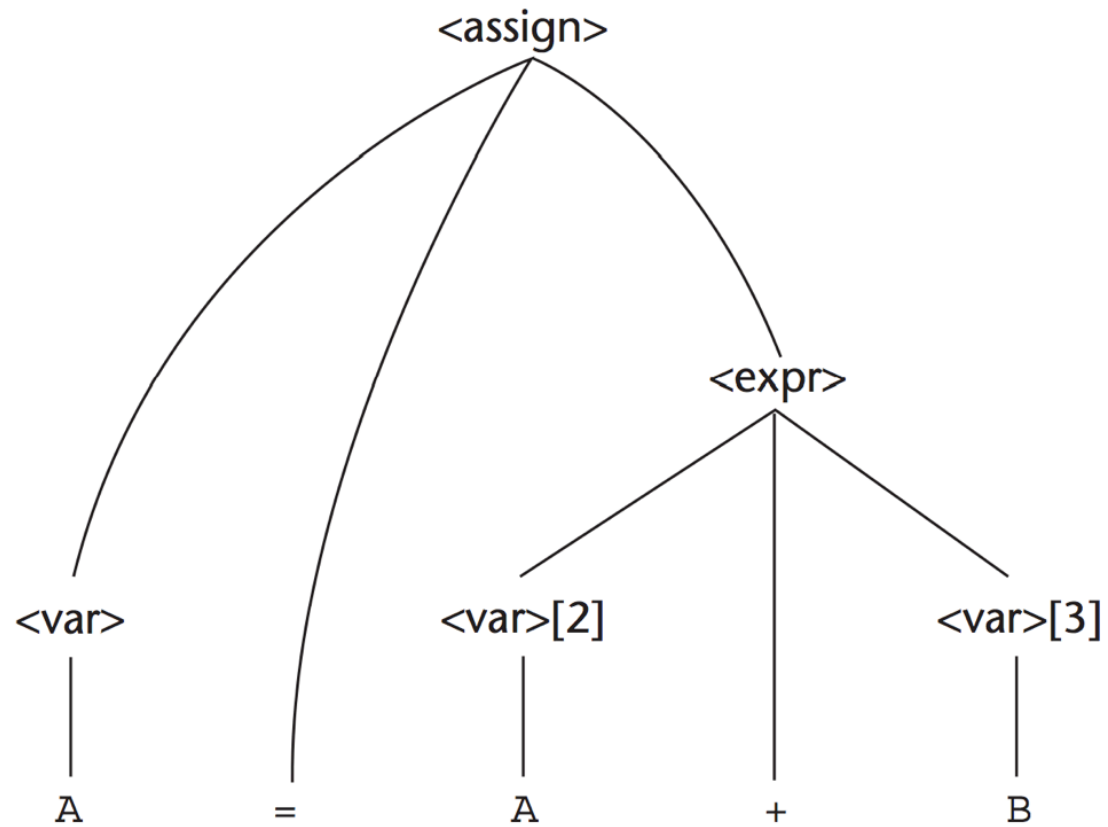
`<var>[2].actual_type ← lookup (B)`

`<var>[1].actual_type =? <var>[2].actual_type`

`<expr>.actual_type ← <var>[1].actual_type`

`<expr>.actual_type =? <expr>.expected_type`

# Parse Tree



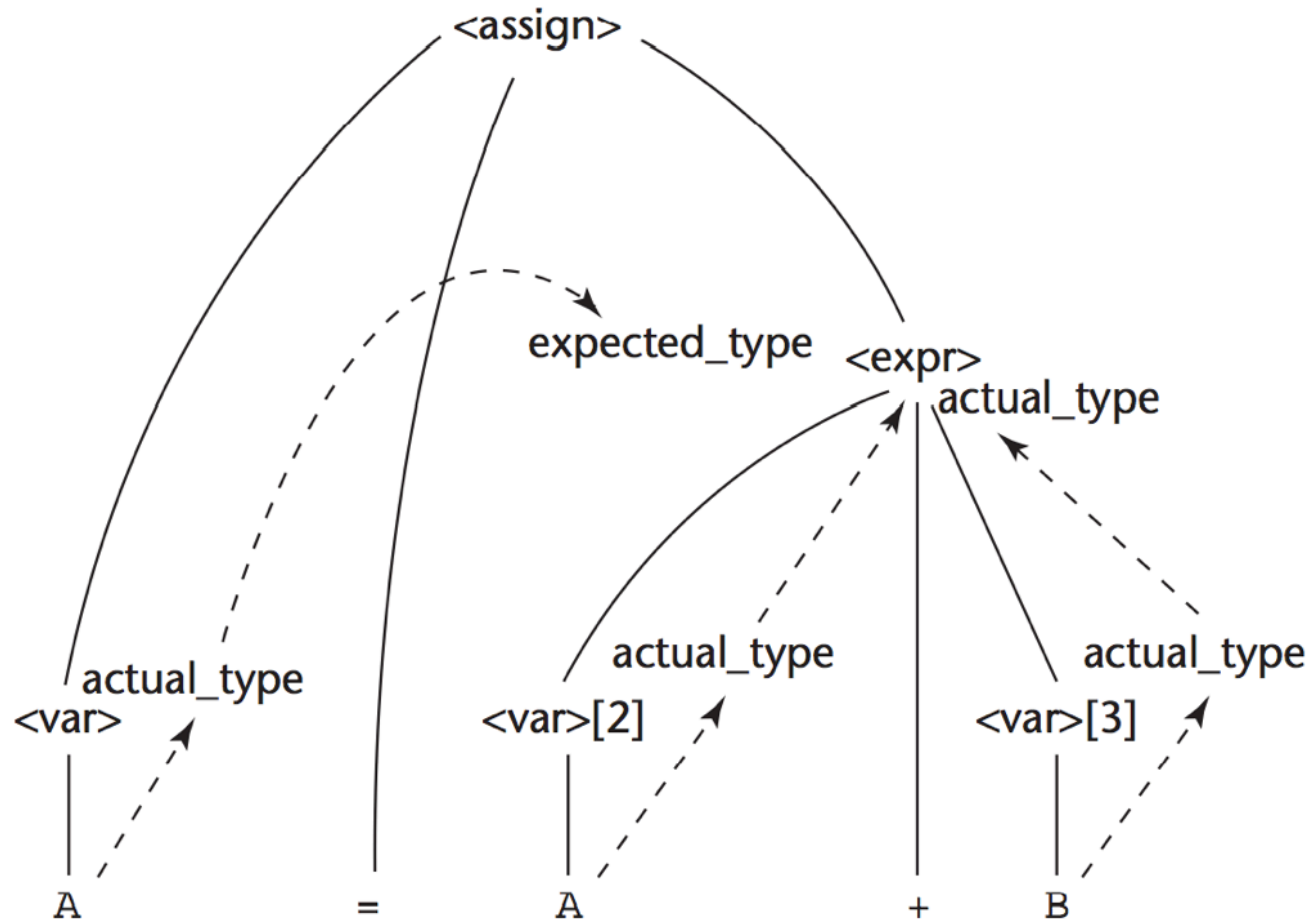
# Computing Attribute Values



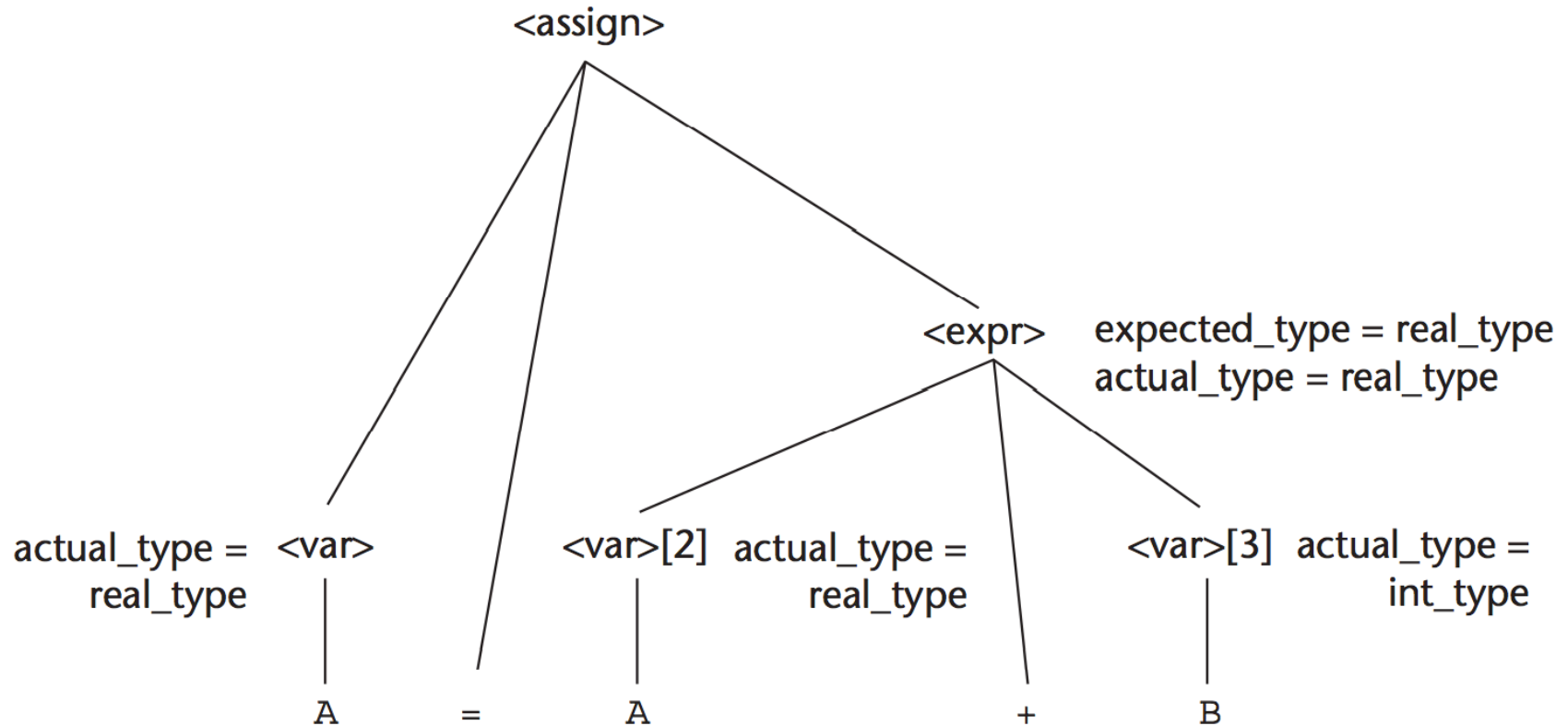
1. `<var>.actual_type ← look-up(A)` (Rule 4)
2. `<expr>.expected_type ← <var>.actual_type`  
(Rule 1)
3. `<var>[2].actual_type ← look-up(A)` (Rule 4)  
`<var>[3].actual_type ← look-up(B)` (Rule 4)
4. `<expr>.actual_type ← either int or real`  
(Rule 2)
5. `<expr>.expected_type == <expr>.actual_type`  
is either  
  
TRUE or FALSE (Rule 2)



# Flow of Attributes in the Tree



# A Fully Attributed Parse Tree



# Semantics

# Semantics

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- There is no single widely acceptable notation or formalism for describing semantics
- Several needs for a methodology and notation for semantics:
  - Programmers need to know what statements mean
  - Compiler writers must know exactly what language constructs do
  - Correctness proofs would be possible
  - Compiler generators would be possible
  - Designers could detect ambiguities and inconsistencies

- 
- Operational Semantics
  - Denotational Semantics
  - Axiomatic Semantics

# Operational Semantics

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- Operational Semantics
  - Describe the meaning of a program by executing its statements on a machine, either simulated or actual. The change in the state of the machine (memory, registers, etc.) defines the meaning of the statement
- To use operational semantics for a high-level language, a virtual machine is needed

# Operational Semantics

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- A hardware pure interpreter would be too expensive
- A software pure interpreter also has problems
  - The detailed characteristics of the particular computer would make actions difficult to understand
  - Such a semantic definition would be machine-dependent

# Operational Semantics (continued)

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- A better alternative: A complete computer simulation
- The process:
  - Build a translator (translates source code to the machine code of an idealized computer)
  - Build a simulator for the idealized computer
- Evaluation of operational semantics:
  - Good if used informally (language manuals, etc.)
  - Extremely complex if used formally (e.g., VDL), it was used for describing semantics of PL/I.



# Operational Semantics (continued)

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- Uses of operational semantics:
  - Language manuals and textbooks
  - Teaching programming languages
- Two different levels of uses of operational semantics:
  - Natural operational semantics
  - Structural operational semantics
- Evaluation
  - Good if used informally (language manuals, etc.)
  - Extremely complex if used formally (e.g., VDL)

# Denotational Semantics

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- Based on recursive function theory
- The most abstract semantics description method
- Originally developed by Scott and Strachey (1970)

# Denotational Semantics – continued

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- The process of building a denotational specification for a language:
  - Define a mathematical object for each language entity
  - Define a function that maps instances of the language entities onto instances of the corresponding mathematical objects
- The meaning of language constructs are defined by only the values of the program's variables

# Denotational Semantics: program state

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- The state of a program is the values of all its current variables

$$s = \{ \langle i_1, v_1 \rangle, \langle i_2, v_2 \rangle, \dots, \langle i_n, v_n \rangle \}$$

- Let **VARMAP** be a function that, when given a variable name and a state, returns the current value of the variable

$$\text{VARMAP}(i_j, s) = v_j$$

# Evaluation of Denotational Semantics

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- Can be used to prove the correctness of programs
- Provides a rigorous way to think about programs
- Can be an aid to language design
- Has been used in compiler generation systems
- Because of its complexity, it is of little use to language users

# Axiomatic Semantics

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- Based on formal logic (predicate calculus)
- Original purpose: formal program verification
- Axioms or inference rules are defined for each statement type in the language (to allow transformations of logic expressions into more formal logic expressions)
- The logic expressions are called assertions

# Axiomatic Semantics (continued)

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- An assertion before a statement (a precondition) states the relationships and constraints among variables that are true at that point in execution
- An assertion following a statement is a postcondition
- A weakest precondition is the least restrictive precondition that will guarantee the postcondition

# Evaluation of Axiomatic Semantics

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- Developing axioms or inference rules for all of the statements in a language is difficult
- It is a good tool for correctness proofs, and an excellent framework for reasoning about programs, but it is not as useful for language users and compiler writers
- Its usefulness in describing the meaning of a programming language is limited for language users or compiler writers



# Denotation Semantics vs Operational Semantics

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- In operational semantics, the state changes are defined by coded algorithms
- In denotational semantics, the state changes are defined by rigorous mathematical functions

# Summary

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- BNF and context-free grammars are equivalent meta-languages
  - Well-suited for describing the syntax of programming languages
- An attribute grammar is a descriptive formalism that can describe both the syntax and the semantics of a language
- Three primary methods of semantics description
  - Operation, Axiomatic, Denotational