

Matlab Programming Help

Online Help:

1. http://www.mathworks.com/academia/student_center/tutorials/launchpad.html
2. <http://www.math.ufl.edu/help/matlab-tutorial/>
3. <http://www.ag.unr.edu/moeltner/Matlab%20Tutorial/Matlab%20Tutorial.pdf>
4. <http://terpconnect.umd.edu/~nsw/ench250/for-mat.htm> (Comparison between Matlab and Fortran f77)

Programming Basic

1. Input and output statement: output is written first.

Example 1:

```
X = Y + 1
```

Define X as Y+1.

X can be a scalar, vector, matrix. To do so, you have to define it first. For scalar case, you don't need to do so.

Code	Meaning
Y=1	Variable Y is defined as 1
Y=1+Y	Variable Y is defined as 1 + 1, so that Y becomes 2
X=Y+1	Variable X is defined as 2 + 1
Y = zeros(1,2)	Y becomes a 1x2 null vector. Y = (0, 0)
Y(1,1) =1 Y(1,2) =2	Y = (1,2)

2. Do Loop

Suppose that you want to add the sequence of numbers from 1 to 10. Let's program this.

Ex2. $X = 1 + 2 + 3 + 4 + 5 + \dots + 10$

Sol 1: Write as

```
X =1 + 2 + 3 + 4 + 5 + 6 + 7 + 8 + 9 + 10
```

Sol 2: Write as

```
X = 1
```

```
X = X + 2
```

```
X = X + 3
```

```
...
```

```
X = X + 10
```

Sol 3: Use "For" statement

<pre>X = 0; For i = 1:10; X = X + i; End;</pre>	<pre>Assign 0 to X. Need ";" to continue program it. Start Do loop. First assign i to be 1, and increase it by 1 up to 10. X becomes X + i, Repeat this until i = 10</pre>
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Let $X = [1\ 3\ 4\ 2\ 2\ 2\ 4\ 1\ 23\ 5]$; That is, X is a 10x1 vector. Calculate its mean by using For statement

<pre>Z = 0; For i = 1:10; Z = Z + X(i); End;</pre>	<pre>Assign 0 to Z. Start Do loop. First assign i to be 1, and increase it by 1 up to 10. Z becomes Z + X(i), Repeat this until i = 10</pre>
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Exercise: For Statement

1. Add 1 through 100
2. Multiply 1 through 20
3. $2 \times 4 \times 6 \times 8 \times \dots \times 20$
4. $X(1) \times Y(1) + X(2) \times Y(2) + \dots + X(n) \times Y(n)$

3. IF Statement

Format:

IF condition statement End

Example: $X = [1\ -2\ 3\ -4]$

We want to change X to index such that $Y = 0$ if $X > 0$, $Y=1$ o.w.

```
Y = X;
```

```
For i = 1:4;
```

```
    if X(i) > 0; Y(i) = 0; end;
```

```
    if X(i) < 0; Y(i) = 1; end;
```

```
end;
```

Exercise: IF Statement

1. $X = [1\ 3\ 4\ 8]$. Find the maximum of X.
2. Find the minimum of X
3. Sort X.

4. Data (Matrix & Vector) Modification

Ex: $A = \begin{bmatrix} 1 & 2 \\ 3 & 4 \end{bmatrix}$ implies $A = \begin{matrix} 1 & 2 \\ 3 & 4 \end{matrix}$

Type the following commends.

1. `A'`
2. `sum(A)`
3. `sum(A')`
4. `sum(A')'`
5. `diag(A)`
6. `sum(diag(A))`
7. `inv(A)`
8. `A(1,2)`
9. `A(1,1)`
10. `A(2,1)`
11. `A(:,1)`
12. `A(1,:)`
13. `A(:)`
14. `A(:,end)`

Expression

`.*` element by element product
`./` element by element division
`\` inverse
`.^` element by element power

Type `A = [1 2; 3 4]; B = [1 1; 2 3];`

1. `a`
2. `A`
3. `b`
4. `B`
5. `A.*B`
6. `A./B`
7. `A\B`
8. `Inv(A)*B`
9. `A'*A`
10. `B'*B`
11. `Inv(A).*A`
12. `Inv(A)*A`

Ex $b = \begin{bmatrix} 2 & 3 \end{bmatrix}$. You want to calculate $A - b = \begin{matrix} 1-2 & 2-3 \\ 3-2 & 4-3 \end{matrix}$

Important Functions

Type `A = [-3 4; 1 3; 2 2]`

1. `a`

2. A
3. mean(A)
4. sum(A)
5. sort(A)
6. [B,id] = sort(A)
7. max(A)
8. min(A)
9. std(A)
10. var(A)
11. cov(A)
12. abs(A)

5. Function Statement

Format

Function output = functionname(inputs)

Example: Average

Function y = mymean(x)

```
t = length(x);
```

```
y = 0;
```

```
for i = 1:t;
```

```
y = y + x(i);
```

```
end;
```

Then in the main program, you can recall 'mymean'.

```
z = mymean(x);
```

In Fortran, this function statement is called as 'subroutine' program.

In Gauss, it is called as 'proc' program.

Matlab library contains many function statements.

Assignment 1: Download X and Y variables from the class homepage.

- A. Sort X from smallest to largest
- B. Sort Y from largest to smallest
- C. Calculate mean and variance of X and Y.
- D. Calculate correlation between X and Y
- E. Make functions (mymean, myvar, mycorr) and use them to calculate C,D and E.
- F. Program OLS function.

Input = x and y. both them are Tx1 vectors.

Regression: $y = bx + u$.

output:

$b = \text{inv}(x'x) * x'y$

R^2 ,

ordinary t-value.

Function $[b,r2,tb] = \text{myols}(y,x)$

Lecture 2: OLS & GLS

Cross section or Time series data

Model $y = a + X*b + u$

Where X is a matrix ($n \times k$, k is number of regressors), a is scalar, b is a vector.

Define a vector such that

```
n = length(y);
a = ones(n,1);
```

Next, define a matrix such that

```
Z = [a X];
[n,k] = size(Z);
```

OLS estimator:

```
bhat = inv(Z'*Z)*Z'*y;
```

1. Regression residuals: $uhat = y - Z*bhat$;

a. t-ratio needs variance of $bhat$:

i. IID case:

```
sigma = uhat.*uhat;
sigma = sum(sigma)/(n-k);
sigma = sigma*inv(Z'*Z);
sigma = diag(sigma);
```

ii. IDIN case:

```
uuhat = Z.*repmat(uhat,1,2);
sigma = uuhat'*uuhat;
sigma = sum(sigma)/(n-k);
sigma = inv(Z'*Z)*sigma*inv(Z'*Z)*n;
```

b. R-squares $Rbar$ -squares:

Example file: ex2.m

```
n = 100;
y = randn(n,1);
x = randn(n,1);
```

```
z = [ones(n,1) x];
b = inv(z'*z)*z'*y;
u = y - z*b;
```

```
sig1 = u'*u/(n-2);
sig1 = sig1*inv(z'*z);
```

```
h = z.*repmat(u,1,2);
sig2 = h'*h/(n-2);
sig2 = inv(z'*z)*sig2*inv(z'*z)*n;
```

```
tra1 = b./sqrt(diag(sig1));
tra2 = b./sqrt(diag(sig2));
```

```
[tra1 tra2]
```

GLS Estimator: AR(1) coefficient case

```
n = 100;
y = randn(n,1);
x = randn(n,1);

z = [ones(n,1) x];
b = inv(z'*z)*z'*y;
u = y - z*b;

% estimation of AR(1) coefficient
uy = u(2:n); ux = u(1:n-1);
rho = inv(ux'*ux)*ux'*uy; % or equivalently rho = sum(ux.*uy)/sum(ux.*ux)
e = uy-ux*rho;
ve = var(e);

% constructing co-variance and variance matrix

omega = eye(n).*ve./(1-rho^2);
for i = 1:n;
    for j = i+1:n;
        omega(i,j) = rho^(j-i);
        omega(j,i) = omega(i,j);
    end;
end;

% Cholesky Decomposition
P = chol(omega);

% Pre-multiplying P matrix
ys = P*y;
zs = P*z;

c = inv(zs'*zs)*zs'*ys;

% variance matrix for c
vc = inv(zs'*zs);

% t-values
tra = c./sqrt(diag(vc));

tra
```

Pooled OLS and LSDV

```
clear;
t=2;
n=10;

y = randn(t,n);
x = randn(t,n);
% LSDV
a = ones(t,1);
a = kron(eye(n),a);

vx = x(:);
z = [a vx];
b = inv(z'*z)*z'*y(:);
b

% POLS

a = ones(t,1);
a = repmat(a,1,n);
a = a(:);
z = [a vx];
b = inv(z'*z)*z'*y(:);
b
```

Assignment 3:

- A. Suppose that you want to program the following regressions
$$y(it) = a_i + cX(it) + u(it)$$
 1. Input must be y and x where X is a nxk matrix
 2. Output must include point estimates, their standard errors (ordinary one, panel robust one), r-bar squares etc.
- B. Suppose that you want to program the following regressions
$$Y(it) = a_i + bz(i) + cX(it) + u(it)$$
 3. Make function for LSDV and POLS
 4. Output must include point estimates, their standard errors (ordinary one, panel robust one), r-bar squares etc.