Systematic Software Testing Techniques: Combinatorial Testing

Dr. Renée Bryce Associate Professor University of North Texas Renee.Bryce@unt.edu

## Presentation outline

- Introductions
- □ Motivation
- Background on combinatorial testing
  - Exercise Create a combinatorial test suite on paper
- □ Algorithms for combinatorial testing
  - Exercise Download and use the ACTS tool
- Prioritized Combinatorial Testing

## Introductions

# Briefly share your experiences with Software Testing

# Motivation

### Costs of software defects

■ Software defects cost ~\$59 billion per year [1]

#### One contributor to software defects

 Many system components are tested individually, but often unexpected interactions between components cause failures.

[1] National Institute of Standards and Technology, The Economic Impacts of Inadequate Infrastructure for Software Testing, U.S. Department of Commerce, May 2002.

# Combinatorial Test Example

Hardware	Operating System	Network Connection	Memory	
РС	Windows XP	Dial-up	64MB	
Laptop	Linux	DSL	128MB	
PDA	FreeBSD	Cable	256MB	_

Four factors (components) have three levels (options) each

#### Sample test

Test No.	Hardware	Operating System	Network Connection	Memory
1	PC	Windows XP	Dial-up	64MB

#### **Pairs covered**

1. (PC, Windows XP)	4. (Windows XP, Dial-up)
2. (PC, Dial-up)	5. (Windows XP, 64MB)
3. (PC, 64MB)	6. (Dial-up, 64MB)

## Combinatorial Test Example

Hardwar	e	Operating		Network	Memory				
		System		Connection				Four factor	S
РС		Windows XP		Dial-up	64MB		$\succ$	(component three levels	ts) have
Laptop		Linux		DSL	128MB			each	
PDA		FreeBSD		Cable	256MB	)			
Test N	Ha	ardware	Op Sy	perating /stem	Network Connectior	ו	I	Memory	
1 <sup>0.</sup>	Р	C	W	indows XP	Dial-up		(	64MB	
2	La	aptop	Fr	eeBSD	DSL			64MB	
3	PI	DA	Li	nux	Cable			64MB	
4	La	aptop	W	indows XP	Cable		•	128MB	
5	La	aptop	Li	nux	Dial-up			256MB	
6	P	C	Li	nux	DSL		·	128MB	
7	P	DA	W	indows XP	DSL			256MB	
8	P	C	Fr	eeBSD	Cable			256MB	
9	PI	DA	Fr	eeBSD	Dial-up		T	128MB	

# Exercise 1

1. List all of the 2way combinations (pairs) for this input:

$f_0$	$f_1$	$f_2$	$f_3$
0	3	6	9
1	4	7	10
2	5	8	11

Hint: Example pairs are (0,3) (0,4) (0,5).... (8,11)

2. Create a combinatorial test suite for the input above. No credit will be given for an exhaustive test suite.

# Brief background

- Combinatorial testing has been used in several fields:
  - Agriculture
  - Combinatorial chemistry
  - Genomics
  - Software/hardware testing



- Study of Mozilla web browser found 70% of defects with 2-way coverage; ~90% with 3-way; and 95% with 4-way. [Kuhn et. al., 2002]
- Combinatorial testing of 109 software-controlled medical devices recalled by US FDA uncovered 97% of flaws with 2-way coverage; and only 3 required higher than 2. [Kuhn *et. al.*, 2004]

# Covering arrays

A covering array,  $CA_{\lambda}(N;t,k,v)$ , is an N x k array. In every N x t subarray, each t-tuple occurs at least  $\lambda$  times. In our application, t is the strength of the coverage of interactions, k is the number of components (factors), and v is the number of options for each component (levels). In all of our discussions, we treat only the case when  $\lambda = 1$ , (i.e. that every t-tuple must be covered at least once).

- Behind the scenes this combinatorial object is constructed to represent interaction test suites
- No efficient exact method is known
- Mathematicians and Computer Scientists have offered solutions from different view points. Their solutions have been measured by *time to generate test suites* and *sizes of test suites.*

# Perceived benefits of greedy algorithms

	Mathematical	Greedy	Search
Size of test suites	Accurate on special cases; but not as general as needed	Reasonably accurate	Most accurate (if given enough time)
Time to generate tests	Yes	Yes	Often time consuming (for good results)
Seeding/ Constraints	Difficult to accommodate seeds/constraints	Yes	Yes

# History of One-test-at-a-time Greedy Algorithms

- AETG
- Pros
  - □ First tool to generate test suites (based on covering arrays)
- Cons
  - Produces different test suites to the same inputs
  - □ Slow
- TCG
- Pros
  - Deterministic
  - Particularly good for mixed-level inputs
  - □ Faster
- Cons
  - Overly large test suites for fixed-level inputs
- DDA Pros
  - Deterministic
  - Competitive results
  - Logarithmic guarantee on the size of test suites

## Sample sizes of test suites

Parameters	DDA	AETG	TCG
$5^{1}3^{8}2^{2}$	21	19	20
$7^{1}6^{1}5^{1}4^{5}3^{8}2^{3}$	43	45	45
$5^{1}4^{4}3^{11}2^{5}$	27	30	30
$6^{1}5^{1}4^{6}3^{8}2^{3}$	34	34	33
$4^{15}3^{17}2^{29}$	35	41	35
$4^{1}3^{39}2^{35}$	27	28	27
313	18	15	20
$2^{100}$	15	10	16
$4^{40}$	43	42	46
4 <sup>100</sup>	51	51	55

[1] R. Bryce, C.J. Colbourn. A Density-Based Greedy Algorithm for Higher Strength Covering Arrays, *Journal of Software Testing, Verification, and Reliability*, (March 2009), 19(1):37-53.

[2] R. Bryce, C.J. Colbourn. The Density Algorithm for Pairwise Interaction Testing, Journal of Software Testing, Verification and Reliability, (August 2007), 17(3): 159-182. \*(Citeseer impact ranking of STVR: .36)

## Framework of One-row-at-a-time Greedy Methods

- Defines commonalities that all "one-row-at-atime" greedy algorithms have in common
- A process provides statistical feedback on the impact of different decisions that can be made in the framework
- Experiments explore several thousand instantiations of the framework and provide a requisite of knowledge

- Layer one: test suite repetitions
- Layer two: multiple candidates
- Layer three: factor ordering\*
- Layer four: level selection\*

Pairs left to	Test No.	Hardware	Operating System	Network Connection	Memory
48	1	РС	Windows XP	Dial-up	64MB
42	2	РС	Linux	DSL	128MB
36	3	РС	FreeBSD	Cable	256MB
	4	?	?	?	?

- Layer one: test suite repetitions
- Layer two: multiple candidates
- Layer three: factor ordering\*
- Layer four: level selection\*



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#### Framework

- Layer one: test suite repetitions
- Layer two: multiple candidates\*
- Layer three: factor ordering
- Layer four: level selection

#### Number of newly

a a ward wains

**3 candidate rows** 

e canana				covered pairs	
PDA	Linux	Cable	128MB	6	
PDA	Win XP	Cable	64MB	5	
PDA	Linux	Cable	128MB	5	23



# Framework experiment - ANOVA results for several inputs

Input:	$10^{1}9^{1}8^{1}7^{1}6^{1}$ $5^{1}4^{1}3^{1}2^{1}1^{1}$	$8^27^26^25^2$	$6^{6}5^{5}3^{4}$	$3^{4}$	6 <sup>4</sup>	$3^{40}$
Layer 1 (Reps)	-	1.0645	1.157	5.698	4.797	10.466
Layer 3 (Factor Ordering)	73.176	70.8598	69.431	10.723	2.472	28.836
Layer 5 Tie-break I	-	-	-	2.10	-	1.200
Layer 3 Tie-break 2	-	-	-	-	-	-
Layer 4 Tie-break 1	4.526	1.0975	4.148	33.646	21.267	3.433
Layer 4 Tie-break 2	-	-	-	-	-	-
Interaction of Layer 1 and Layer 2	-	1.4686	-	-	1.956	-
Interaction of Layer 2 and Layer 3	1.827	2.2132	1.061	1.45	-	-
Interaction of Layer 3 and Layer 3 Tie-break 1	-	-	-	3.435	1.29	2.866
Interaction of Layer 3 and Layer 4 Tie-break 1	3.535	2.1676	6.285	3.157	18.161	3.604
Lack Of Fit	13.649	17.7303	14.41	35.786	44.196	44.774
*Values that contribute <1% are not reported						

[1] R.Bryce, C.J. Colbourn, M.B. Cohen. *A Framework of Greedy Methods for Constructing Interaction Tests*. The 27<sup>th</sup> International Conference on Software Engineering (ICSE), St. Louis, Missouri. (May 2005), pp. 146-155. (*13% acceptance rate*)

\*Citeseer impact ranking of ICSE: 2.05

## ACTS – Free Download

- ACTS is a free tool to generate combinatorial test suites
- Download at: <u>http://csrc.nist.gov/groups/SNS/acts/download/</u>
- □ login ID is 'fireeye',
- □ password 'acts71362'
- Create a test suite for this input with 2way coverage and then generate a  $2^{nd}$  test suite with 3way

coverage:

$f_0$	$f_1$	$f_2$	$f_3$
0	3	6	9
1	4	7	10
2	5	8	11

# Prioritized combinatorial testing

- What if parts of a system are more important to test earlier?
- What if a tester learns during testing and wants to regenerate a test suite with new priorities?
- What if a tester has time to run pair-wise coverage and time to run some three-way tests?

## A variation of the covering array

An Q-biased covering array is a covering array CA(N; 2, k, v) in which the first rows form tests whose total benefit is as large as possible. That is, no CA(N; 2, k, v) has rows that provide larger total benefit.

#### Input

Factor	$v_0$	$v_1$	$v_2$	$v_3$
$f_0$	0(.2)	1(.1)	2(.1)	3(.1)
$f_1$	4(.2)	5(.3)	6(.3)	-
$f_2$	7(.1)	8(.9)	-	-

3 factors with varying numbers of associated > levels (options) and weights assigned to each level

# Algorithm Walkthrough

#### Input

Factor	$v_0$	$v_1$	$v_2$	$v_3$
$f_0$	0(.2)	1(.1)	2(.1)	3(.1)
$f_1$	4(.2)	5(.3)	6(.3)	-
$f_2$	7(.1)	8 (.9)	-	-

#### Step 1 – Calculate Factor Interaction Weights.

Factor Interaction Weight	$f_0$	$f_1$	$f_2$	Total Weight
$f_0$	-	.4	.5	.9
$f_1$	.4	-	.8	1.2
$f_2$	.5	.8	_	1.3

3 factors with varying numbers of associated levels (options) and weights assigned to each level

Larger weight means higher priority should be given to testing earlier!

Factors will be assigned values in order of "highest priority"

## Algorithm Walkthrough

- ☑ Input has been processed
- Factor interaction weights have been calculated (to determine order to assign level values to factors).

Input

Factor	$v_0$	$v_1$	$v_2$	$v_3$
$f_0$	0(.2)	1(.1)	2(.1)	3(.1)
$f_1$	4(.2)	5(.3)	6(.3)	-
$f_2$	7(.1)	8 (.9)	-	-

Step 2 – Calculate Factor-Level Interaction Weights to select the level that covers the most uncovered *weighted density*.

For a factor, i, and a level, 2, that number of levels for a factor is called  $v_{max}$ , and the factor interaction weight is called  $w_{max}$ 

**Factor-Level Interaction Weight =** 

$$\sum_{j=1}^{v_{\max}} \left( \frac{w_{f_{i_j}} * w_{\ell}}{w_{\max}} \right)$$

$$f_{2_{v_0}} = (.05/1.3) + (.08/1.3) = .1$$
  
$$f_{2_{v_1}} = (.45/1.3) + (.72/1.3) = .9$$

Remember, the factor interaction weight was 1.3 for factor 2.

## Algorithm Walkthrough

For a factor, i, and a level, 2, that number of levels for a factor is called  $v_{max}$ , and the factor interaction weight is called  $w_{max}$ 

Factor-Level Interaction Weight =

factor-interaction

weight

$$\sum_{j=1}^{v_{\text{max}}} \left( \frac{w_{f_{i_j}} * w_{\ell}}{w_{\text{max}}} \right)$$

□ Step 2 (continued) - Calculate Factor-Level Interaction Weights to select the level that covers the most uncovered *weighted density*.

$$f_{2_{v_0}} = (.05/1.3) + (.08/1.3) = .1$$

$$f_{1_{v_0}} = (.1/1.3) + (.2/.9) = .2569$$

$$f_{0_{v_0}} = (.2*.3) + (.2*.9) = .24$$

$$f_{0_{v_1}} = (.1*.3) + (.1*.9) = .12$$

$$f_{1_{v_1}} = (.15/1.3) + (.3*.9) = .38538$$

$$f_{0_{v_1}} = (.1*.3) + (.1*.9) = .12$$

$$f_{0_{v_2}} = (.1*.3) + (.1*.9) = .12$$
Weight between two levels divided by max factor-interaction weight + Use the term intermediate ter

Weight of level multiplied by

weight of level (of fixed factor)

Weights of levels between each  $_{31}$ multiplied

# Sample Results

Factor	$v_0$	$v_1$	$v_2$	$v_3$
$f_0$	0(.2)	1(.1)	2(.1)	3(.1)
$f_1$	4(.2)	5(.3)	6(.3)	-
$f_2$	7(.1)	8 (.9)	-	-

#### Output

Row Number	$f_0$	$f_1$	$f_2$
1	0	5	8
2	1	6	8
3	2	4	8
4	3	5	8
5	0	6	7
6	0	4	7
7	1	5	7
8	2	5	7
9	3	6	7
10	2	6	7
11	1	4	7
12	3	4	7



[1] R. Bryce, C.J. Colbourn. Prioritized Interaction Testing for Pairwise Coverage with Seeding and Avoids, *Information and Software Technology Journal* (IST, Elsevier), (October 2006), 48(10):960-970.

\* Citeseer impact ranking of ICST: .19

# Ongoing and future work

- Ultimate goal: to develop systematic testing methodologies that are widely used to improve software quality
- □ Reaching this goal:
  - Testing methodology driven by practical concerns of testers
    - Algorithms (for testing tools)
    - Empirical studies