

# The *METAflow* package for METAPOST

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## Abstract

This package supplies convenient mechanisms for drawing flowcharts in METAPOST. It includes commands for drawing line shapes (e.g., rectangles, ovals, drums, etc.), text labels, fill patterns, and arrow connectors.

## 1 Introduction

METAPOST is a superior means of drawing scientific diagrams for L<sup>A</sup>T<sub>E</sub>X documents for the following reasons:

- *Precision:* METAPOST graphics have a very clean, precise look because designers mathematically specify the correct placement of all figure elements rather than estimating their locations by point-and-click.
- *Scalability:* METAPOST outputs pure vector graphics that exhibit no quality degradation with scaling, making them ideal for professional publishing.
- *Output compatability:* Using `graphicx`, L<sup>A</sup>T<sub>E</sub>X can import METAPOST graphics directly into DVI, PostScript, and PDF documents without converting them to a lower quality graphic format.
- *Small size:* Embedded METAPOST graphics are typically much smaller than alternative formats, making the resulting documents more convenient to serve over the web.

The *METAflow* package creates convenient METAPOST macros for drawing flowcharts and other line-art pictures. Unlike other similar METAPOST packages, *METAflow* infers all shape positions and sizes from linear constraints rather than requiring the user to specify them as explicit macro parameters. This leverages the considerable power of METAPOST's constraint-solver to position and size shapes in natural ways, such as by auto-sizing them to their labels or auto-positioning them relative to other shapes.

```

1 input metaflow
2 prologues := 2;
3 filenameTEMPLATE "%j-%c.mps";
4 beginfig(1)
5 z1c = (0,0);
6 draw rect1(btex experiment etex);
7 putitem2 20right of 1;
8 draw oval2(btex results etex);
9 drawarrow connector(1,2,right,right);
10 putitems(2,3) like (1,2);
11 z3s = (55,30);
12 draw diamond3(btex evaluate etex);
13 drawarrow connector(2,3,right,right);
14 drawarrow connector1(3,1,down,up);
15 z4um = point 1.5 of cpl;
16 drawopen rect4(btex revise etex);
17 putitems(3,5) like (1,2);
18 drawopen rect5(btex success etex);
19 drawarrow connector(3,5,right,right);
20 endfig;
21 end

```

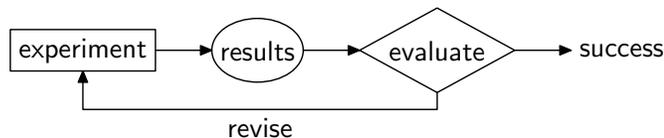
(a) Listing of chart.mp

```

1 \documentclass{article}
2 \usepackage{graphicx}
3 \begin{document}
4 Here is a nice diagram:
5 \begin{center}
6 \includegraphics
7   [width=.7\hsize]
8   {chart-1.mps}
9 \end{center}
10 \end{document}

```

(b) Listing of sample.tex



(c) The image that results from the two listings above

Figure 1: A simple METAPOST program and the image it draws

## 2 Basic Usage

The METAPOST and L<sup>A</sup>T<sub>E</sub>X source files in Figs. 1(a) and 1(b) produce the flowchart in Fig. 1(c) using METAflow. To compile the sample, perform the following steps:

1. Create a new text file named `chart.mp` with the content of Fig. 1(a).
2. Copy the `metaflow.mp` and `mftext.tex` files into the same directory.
3. Run METAPOST: `mpost -tex=latex chart.mp`
4. Create a new text file named `sample.tex` with the content of Fig. 1(b).
5. Run L<sup>A</sup>T<sub>E</sub>X: `pdflatex sample.tex`

**Initialization.** Line 1 of Fig. 1(a) loads the `metaflow` package; it requires the package file `metaflow.mp` to be in the same directory as your `chart.mp` file. Line 2 asks METAPOST to add font metric information to the output graphics, which is necessary for compatibility with many DVI and PostScript viewers.

Line 3 specifies that each output file should be named  $\langle jobname \rangle - \langle number \rangle .mps$ . An `mp` file may contain many figures, each of which begins with `beginfig` (Line 4) and ends with `endfig` (Line 20). The number in the `beginfig` line determines the  $\langle number \rangle$  part—in this case `chart-1.mps`.

**Anchor points.** Line 5 defines a point named `z1c` located at the origin. Point names in METAPOST start with *prefix* `z`, followed by a numerical *index* (e.g., 1), and concluding with an alphabetic *suffix* (e.g., c). The `METAflow` package reserves certain suffixes for anchor points of shapes, as illustrated in Fig. 2. Suffix `c` is for the center point of the shape, so Line 5 states that the center of shape 1 is at the origin. To refer to the *x*- or *y*-value of a point, just use prefix `x` or `y` in place of `z`. For example, we could have instead written `x1c=0` and `y1c=0` separately.

Defining the position of any anchor point defines the position of the whole shape. Positions can also be expressed relative to other points. For example,

$$z2m1 = z1mr + (20,0); \tag{1}$$

says that the middle-left (`m1`) point of shape 2 is 20 points to the right and 0 points above the middle-right (`mr`) point of shape 1.

`putitem` The `putitem` macro makes such constraints easier to type. To place the edge of shape  $\langle i \rangle$  a distance  $\langle n \rangle$  in the  $\langle dir \rangle$  direction from shape  $\langle j \rangle$ , write

$$\text{putitem}\langle i \rangle \langle n \rangle \langle dir \rangle \text{ of } \langle j \rangle$$

where  $\langle dir \rangle$  is one of `up`, `down`, `left`, `right`, `upright`, `downright`, `upleft`, or `downleft`. For example, Line 7 of Fig. 1(a) is equivalent to statement (1) above.

`putitems` To “copy” the relative positioning of a pair of items, use the `putitems` macro:

$$\text{putitems}(i_1, j_1) \text{ like } (i_2, j_2);$$

applies the same `putitem` command to items  $i_1$  and  $j_1$  as was applied to position items  $i_2$  and  $j_2$ . For example, Line 10 says that items 2 and 3 should be relatively positioned like items 1 and 2 (as specified in Line 7). This is better than retyping the “`20right`” in Line 7 because it allows you to later fine-tune the placement of all the figure items by changing only Line 7 instead of all its copies.

**Sizes.** Suffix `s` is reserved for the *size* of shapes. For example, Line 11 says that shape 3 is 55 points wide and 33 points high.

Whenever a shape has a label, `METAflow` assigns a default size to suffix `ds`. You can specify the shape’s size relative to this default by writing constraints like

$$z\langle i \rangle s = z\langle i \rangle ds + (5,2);$$

This makes shape  $\langle i \rangle$  5 points wider and 2 points higher than its default size. If you do not specify a shape's size and the shape has a label, *METAflow* uses the default size. If it does not have a label, you must specify a size.

Some combinations of constraints make it unnecessary to explicitly specify a size; for example, if you specify the positions of the lower-left and upper-right corners, *METAflow* infers the resulting size automatically.

**Shapes.** The `draw` command draws a shape at its prespecified position. The various shapes, their names, and their anchor points are shown in Fig. 2. Labels, if provided, are centered within the shape. To leave the shape unlabeled, you can omit the label (leaving an empty pair of parentheses). Be sure to specify a size in this case (see above).

`drawopen` Using `drawopen` instead of `draw` draws a shape's label (and any fills) without drawing its border. This is convenient for drawing text boxes, as demonstrated by Lines 16 and 18 of Fig. 1(a).

`connector` **Connectors.** The expression `connector( $i_1, i_2, dir_1, dir_2$ )` returns a *connector path* from shape  $i_1$  to shape  $i_2$ . The path leaves shape  $i_1$  in direction  $dir_1$  and enters shape  $i_2$  in direction  $dir_2$ . Indexes  $i_1$  and  $i_2$  are numbers, and directions  $dir_1$  and  $dir_2$  are each one of `up`, `down`, `left`, or `right`. The path avoids passing through shapes  $i_1$  and  $i_2$ , but does not attempt to avoid any other shapes.

To draw a connector path with an arrow at the end, use the `drawarrow` command, as in Lines 9, 13, and 19. To draw the path without an arrowhead, just use `draw`. To draw arrowheads at both ends, use `drawdblarrow`.

Line 14 assigns the name "1" to the connector it draws. This allows Line 15 to use the expression "`point  $n$  of cpl`" to refer to the  $n$ th point along connector path 1. In general, the 0th point is the start point, the  $n$ th point is the  $n$ th bend in the path, and the last point is the end point. Fractional points are interpolated, so the 1.5th point is halfway between the 1st and 2nd points.

**Line styles and colors.** Any METAPOST drawing options can be used at the end of any kind of `draw` command to specify the line style and color. Figure 3 shows some examples. These can come at the end of any `draw` command, including `drawarrow`, and can be combined when relevant. For example,

```
draw rect1() withpen (pencircle scaled 4)
              withcolor (red)
              dashed (evenly scaled 4);
```

draws a rectangle whose border is a thick, red, long-dashed line.

**Filled shapes.** Shapes can be filled with solid colors, stripes, or tessellated patterns by using the `filledwith`, `stripedwith`, and `tesselatedwith` operators, respectively. Figure 4 illustrates each. When line styles and fill styles are combined, as in Fig. 4(d), *all line styles must come after all fill operators*.

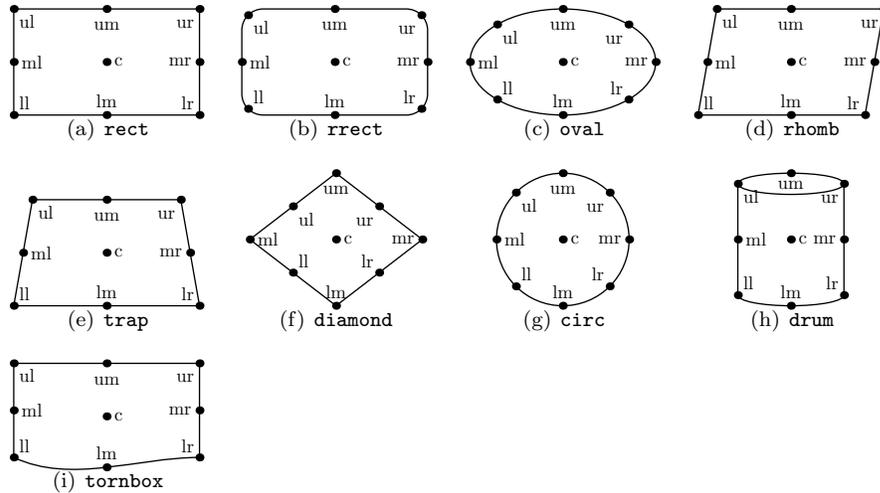


Figure 2: Shapes and their anchor points

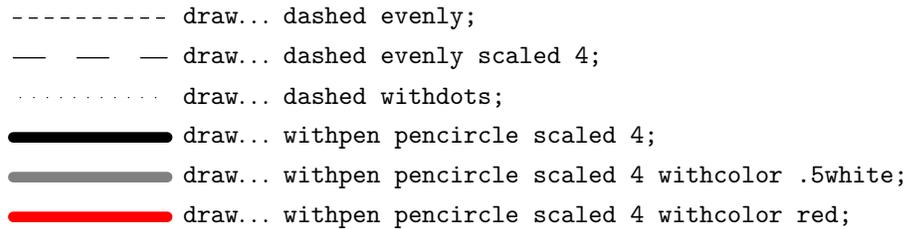


Figure 3: Line style examples

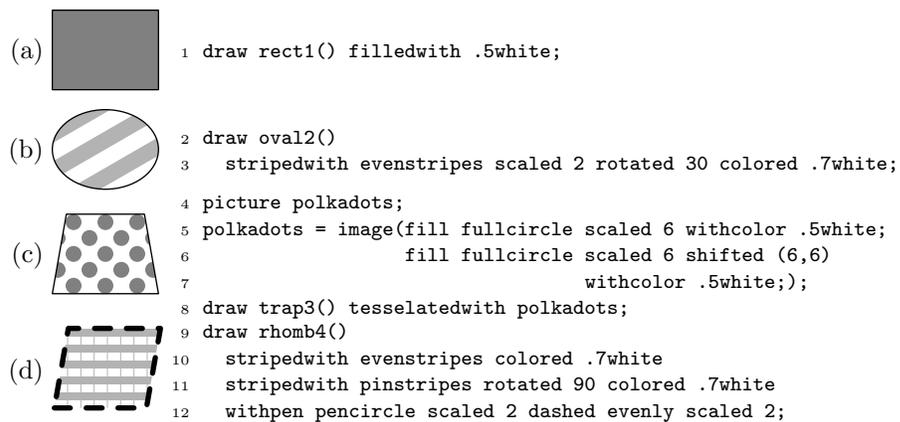


Figure 4: Filled shapes

`filledwith` The `filledwith` operator fills shapes with solid colors, as seen in Fig. 4(a).

`stripedwith` The `stripedwith` operator fills shapes with stripe patterns, as demonstrated by Fig. 4(b). A stripe pattern is usually the predefined picture `evenstripes` optionally `scaled` to change stripe thickness, optionally `rotated` to change orientation, and optionally `shifted` to adjust position. The alternative `pinstripes` picture creates stripes of zero thickness (i.e., lines).

`colored` Any picture's color can be adjusted with the `colored` operator. This is useful for changing stripe colors, as shown in Figs. 4(b) and 4(d). Note that the `colored` operator is *not* the same as the `withcolor` modifier; the former changes the color of a picture (e.g., a fill) whereas the latter specifies a line color for a `draw` command.

`tesselatedwith` The `tesselatedwith` operator fills shapes with a tessellated, rectangular picture. Figure 4(c) constructs such a picture using METAPOST's `image` macro.

Multiple fill operators can be layered, as in Fig. 4(d), to produce cross-hatching or other effects. They are applied from first to last, with opaque parts of later fills occluding those that came before. As noted earlier, any line style options must come last, after all fill operators, as Line 12 demonstrates.

`inback` **Layering.** By default, each drawing command contributes new material on top, occluding anything that may have been drawn previously (except that item labels are always drawn atop everything else). To instead draw something underneath what has been drawn before, prefix it with the word `inback`:

```
inback draw rect3() filledwith .8white;
```

`turntolayer` More complex layering can be achieved with the stand-alone command `turntolayer(n)`, which causes all subsequent drawing commands until the next `turntolayer` command to draw onto layer number *n*. The starting layer is number 0, with lower-numbered layers drawn behind higher-numbered ones. Negative-numbered layers are permitted.

### 3 Text

METAPOST documents typeset textual content in L<sup>A</sup>T<sub>E</sub>X using `btex` *<text>* `etex`:

```
draw rect1(btex Approximate $f^2(x)$ etex)
```

To use L<sup>A</sup>T<sub>E</sub>X (rather than plain T<sub>E</sub>X) to typeset such text, perform 3 steps:

1. Copy the included `mftext.tex` helper library to your working directory.
2. Add the following code to your `mp` file somewhere before your first figure:

```
verbatimtex
\documentclass[10pt]{article}
\renewcommand\familydefault{\sfdefault}
\input mftext
\begin{document}
etex
```

This material, if used, *must* be placed directly in the top-level `mp` file (not in an auxilliary file included via `input`), since that is the only place METAPOST looks for it.

- Execute METAPOST with: `mpost -tex=latex <mpfile>`

The  $\text{\LaTeX}$  code in step 2 accomplishes three things:

- It sets up a  $\text{\LaTeX}$  environment rather than one limited to plain  $\text{\TeX}$ .
- It makes 10-point Sans Serif the default font.
- It introduces macros `\textc`, `\textl`, and `\textr`, which center-, left-, and right-align (respectively) multiline text separated by `\\` (see Fig. 5).

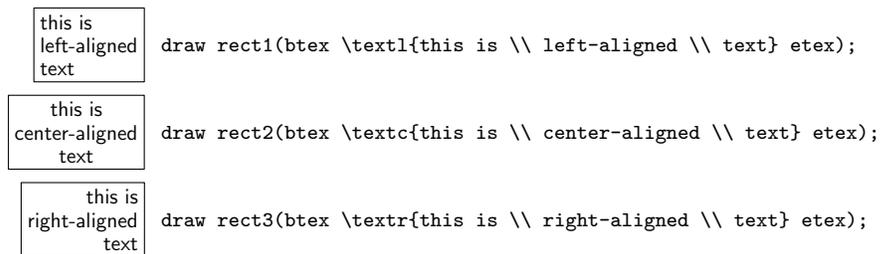


Figure 5:  $\text{\LaTeX}$  labels with textual alignment

## 4 Advanced Features

### 4.1 Rotated Shapes

Shapes can be rotated using the `rshape` operator:

$$\text{rshape}\langle i \rangle(\langle shape \rangle, \langle dir \rangle)(\langle label \rangle)$$

Figure 6 illustrates by rotating a trapezoid. Direction  $\langle dir \rangle$  is one of `up`, `down`, `left`, or `right`, where the `up` direction leaves the shape upright (i.e., unrotated).

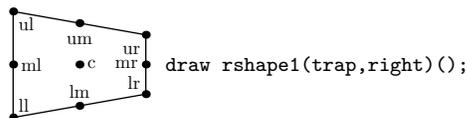


Figure 6: A rotated trapezoid

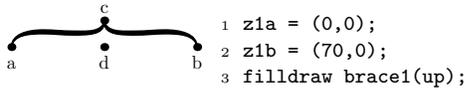


Figure 7: Braces

## 4.2 Braces

Curly braces are created as in Fig. 7. Define at least the **a** and **b** anchor points (which are interchangeable), and indicate the direction of the brace in the macro’s sole argument. The height and position of the cusp can be adjusted by additionally defining the **c** anchor point. The position but not the height can be adjusted by defining anchor point **d** instead, which must lie on the line segment from **a** to **b**.

The **brace** macro returns an outline path for the brace, so typically one should use **filldraw** to draw the outline and fill it. Unlike other shapes, braces do not have a size (**s**), default size (**ds**), or built-in label; and they rotate to match the slope of the line **a**-**b**.

## 4.3 Shape Adjustments

Most variables in METAPOST are *immutable*—their values never change. For example, the constraint “**z1c=(0,0)**” says that the center of shape 1 is the origin forever. In contrast, the variables described in this section are *mutable*—their values may change, and METAFLOW uses the current value when defining shapes. To change the value of a mutable parameter, use the special assignment operator “:=”. For example, command “**rradius:=10**” changes the radii of of future rounded rectangle corners to 10 (see below).

<b>rradius</b>	The radii of the rounded corners of <b>rrect</b> shapes can be changed by reassigning <b>rradius</b> .
<b>rhombangle</b>	The angle of the bottom-left corner of a <b>rhomb</b> or <b>trap</b> shape is given by <b>rhombangle</b> , which must be a number between 0 and 180.
<b>drumlidratio</b>	The ratio of the height to width of a <b>drum</b> ’s lid is given by <b>drumlidratio</b> . Its default value is 0.2.
<b>ilmargin</b>	When sizing shapes to fit their labels, the minimum distance permitted between the item label and its border is given by the number <b>ilmargin</b> .
<b>braceheight</b>	Figure 8 illustrates the six parameters that control the appearance of curly braces yielded by <b>brace</b> , along with their default values. The <b>braceheight</b> parameter is merely a default that is only used when the cusp anchor point ( <b>c</b> ) for the brace is not pre-specified.
<b>clawwidth</b>	
<b>beekheight</b>	
<b>beekangle</b>	
<b>bracethick</b>	
<b>braceret</b>	

## 4.4 Custom Connectors

Declaring a named connector via **connector** $\langle i \rangle(\dots)$  introduces an array of points named **z** $\langle j \rangle$ **cp** $\langle i \rangle$  where  $\langle i \rangle$  identifies the connector and  $\langle j \rangle$  identifies a bend or endpoint of the connector. For example, **z0cp5** is the start point of connector 5, **z1cp5** is its 1st bend (or endpoint if it has no bends), etc. Pre-specifying values for

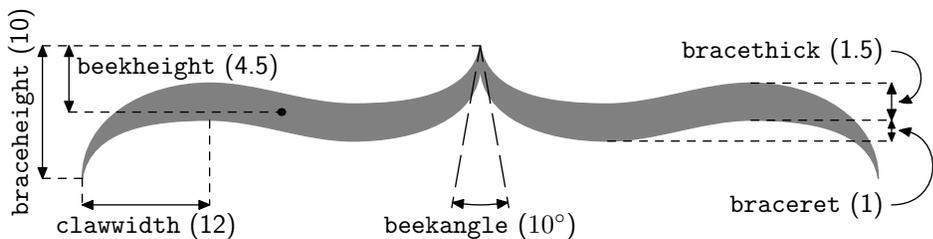


Figure 8: Brace parameters



```

1 drawarrow connector(1,2,right,left);
2 x1cp8 = .75[x1mr,x2ml];
3 drawarrow connector8(1,2,right,left) dashed evenly;
4 y2cp9 = y2um + 6;
5 drawarrow connector9(1,2,right,left) dashed evenly scaled 2;

```

Figure 9: Custom connectors

these points before the `connector` operator is used has the effect of customizing the connector path.

Figure 9 demonstrates. Line 1 draws the default connector path (the solid line) departing rightward from box 1 and entering leftward into box 2. Line 2 asserts that the  $x$ -ordinate of bend 1 of connector path 8 (`x1cp8`) should be 75% of the way from the middle-right of box 1 (`x1mr`) to the middle-left of box 2 (`x2ml`). This results in the short-dashed connector path in the figure. (Note that most of the path overlaps the solid-line default path and cannot be seen.) Line 4 asserts that the  $y$ -ordinate of bend 2 of connector path 9 (`y2cp9`) should be 6 points above the  $y$ -ordinate of the upper-middle point of box 2 (`y2um`). This causes the path to loop overtop box 2 instead of underneath, resulting in the long-dashed connector path in the figure.

*METAflow* will never change the number of bends in a path in response to connector customizations. If you want to radically change the path strategy, you should draw your own path from scratch using *METAPOST* commands instead of using the `connector` operator.

**cmargin** Default connector paths avoid passing within `cmargin` points of the bounding boxes of the source and destination items. You can adjust this margin by changing the value of `cmargin`:

```
cmargin := 10;
```

**popover** The `popover` macro can be used to “pop” one connector path over its intersections with a list of other paths, as demonstrated by Fig. 10. The syntax

```
<path> popover(<path list>)
```

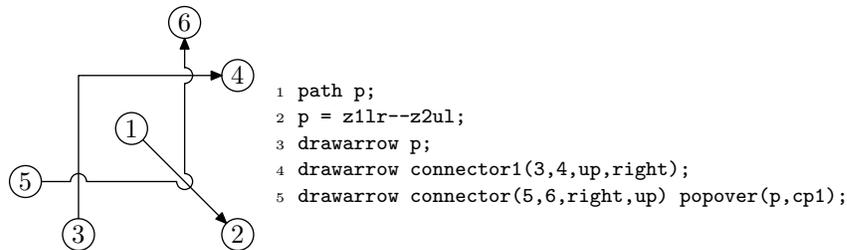


Figure 10: Popovers

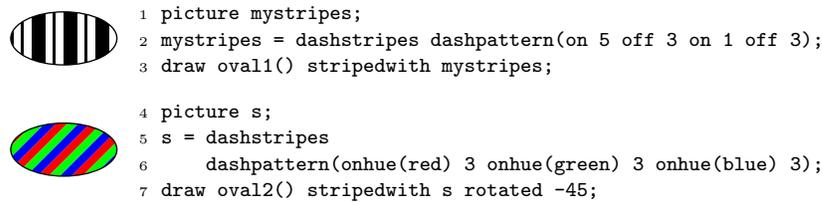


Figure 11: Custom stripe patterns

returns a path in which semi-circular arcs have been spliced into  $\langle path \rangle$  wherever it intersects any of the paths in  $\langle path list \rangle$  (a comma-separated list of paths). To change the radii of the arcs, modify `pradius` (e.g., “`pradius:=5`”). Any intersections closer than `pradius` to the ends of the  $\langle path \rangle$  or from any other intersections are ignored by `popover`.

## 4.5 Custom Stripe Patterns

**dashstripes** In addition to the predefined `evenstripes` and `pinstripes` stripe patterns, authors may define their own stripe patterns by first defining a METAPOST `dashpattern` and then converting it to a stripe pattern with the `dashstripes` operator. For example, Line 2 of Fig. 11 creates a stripe pattern consisting of a long (5-point) dash, a 3-point gap, then a short (1-point) dash, another 3-point gap, repeating.

The `dashstripes` operator projects each dash orthogonally to form a stripe. Since METAPOST `dashpatterns` are horizontal, this means that custom stripes start out vertical. To rotate them, apply the `rotated` operator to the result of the `dashstripes` operation.

A dash that has zero width (created via “on 0” in the `dashpattern` argument) becomes a line when striped, like the stripes in the `pinstripes` pattern. A pattern consisting solely of `pinstripes` must have more than one in the `dashpattern` operand. For example, instead of writing `dashpattern(on 0 off 3)`, which consists of exactly one pinstripe and is therefore illegal, write `dashpattern(on 0 off 3 on 0 off 3)`, which is equivalent but has two pinstripes, satisfying the requirement. (A pattern consisting of exactly one pinstripe is not permitted because a zero-width dash is a directionless point, preventing `dashstripes` from identifying

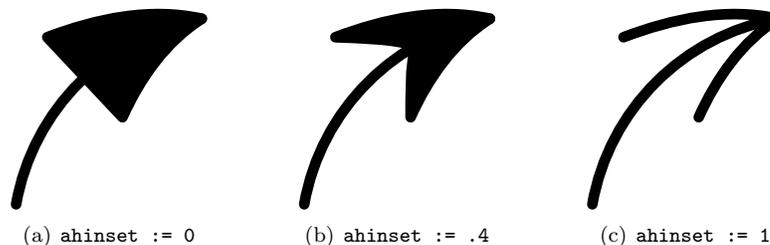


Figure 12: Arrowhead variants

the direction orthogonal to the pattern.)

**onhue** Custom stripe patterns can be recolored using `colored` in the typical way (see §2), but multicolored stripe patterns can be created directly using the `onhue` dash pattern operator. Line 6 demonstrates. Operation `onhue(<color>)` is like `on` except that it additionally specifies the `<color>` of the dash.

## 4.6 Helper Variables and Macros

**ip** Defining a shape item introduces a new path variable `ip<n>` (where `<n>` is the item's name) that holds the border of the shape. This is useful if you want to use METAPOST commands and operations to find (non-anchor) points on the item's border. The borders of all shapes other than drums are cycles.

**il** The picture variable `il<n>` holds the label (if any) of item `<n>`, and variable **ls** `z<n>ls` holds its size.

**cp** Each named custom connector declared via `connector<i>(...)` (see §4.4) introduces a variable named `cp<i>` that stores the connector path, and variables named `z<j>cp<i>` for the `j`th endpoint or bend in the path.

**llcorners** Plain METAPOST provides `llcorner`, `urcorner`, `lrcorner`, and `ulcorner`  
**urcorners** primitives that return the lower-left, upper-right, lower-right, and upper-left corner  
**lrcorners** of a path or picture. *METAflow* extends these with plural forms that return  
**ulcorners** the corners of a *list* of paths, pictures, and/or points. For example, the following creates a rectangle that circumscribes items 1, 2, and 3 (definitions are not shown).

```
z4ll = llcorners(ip1,ip2,ip3) - (10,10);
z4ur = urcorners(ip1,ip2,ip3) + (10,10);
draw rect4();
```

## 4.7 Arrowheads

The back edge of arrowheads can be customized by adjusting the value of `ahinset` to a value between 0 and 1. The possibilities are illustrated in Fig. 12. The default value of 0 draws arrowheads with straight back edges, value 1 draws open arrowheads with no back edge, and values between 0 and 1 yield V-shaped back edges.

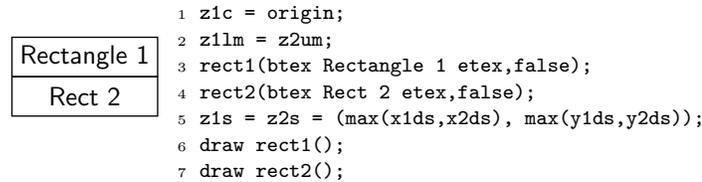


Figure 13: Rectangles with interdependent parameters

## 4.8 Interdependent Shapes

Sometimes the parameters of two or more shapes interrelate in such a way that none can be finalized and drawn until the others are declared. For example, suppose rectangles 1 and 2 should have identical sizes that are the maximum of their respective default sizes (as determined by their labels). Maximization is a non-linear function, so it cannot be specified as a linear constraint in METAFLOW. Both default sizes must therefore be known before the size of either shape can be computed.

Figure 13 illustrates how this can be accomplished in METAFLOW with three steps. First, declare each shape without finalizing or drawing it by supplying the optional boolean argument `false` to the shape's constructor (Lines 3–4). Second, supply any interdependent or non-linear constraints necessary to resolve all unknowns for the shapes (Line 5). Third, finalize and draw the shapes by applying the shape constructors again with no arguments (Lines 6–7).

## 4.9 Scripting

When drawing, it is convenient to have a means of quickly inspecting the results of edits. On Unix I recommend creating a Makefile with the following content:

```

texfiles = mydocument.tex
mpfiles = myfigures.mp

all: $(texfiles:%.tex=%.pdf) $(mpfiles:%.mp=%-1.mps)
%.pdf: %.tex $(mpfiles:%.mp=%-1.mps)
    →|pdflatex $<
    →|if grep "may have changed" $*.log; then pdflatex $<; fi
%-1.mps: %.mp
    →|mpost -tex=latex $<
    →|touch $@

```

where `mydocument.tex` and `myfigures.mp` are the names of your main `.tex` and `.mp` files, respectively. Then execute `gmake` to compile all documents and figures.

On Windows I recommend creating a plain text file (e.g., with Notepad) named `makefigs.bat` in the same directory as your `tex` and `mp` files with the following content:

```
mpost -tex=latex myfigures.mp
@if ERRORLEVEL 1 PAUSE & EXIT
pdflatex mydocument.tex
@PAUSE & EXIT
```

where `mydocument.mp` and `myfigures.tex` in the first and third lines should be replaced with the filenames of your `mp` and `tex` file, respectively. Double-click on your `makefigs.bat` file to recompile your document, including recompiling all figures.

## 5 Implementation

This package requires at least version 1.004 of METAPOST, since that version introduced the `colorpart` macro. (Earlier versions had broken or non-existent color primitives.)

```
1 if unknown mpversion: errmessage
2 "MetaPost v1.004 or later required (found one older than v0.900)";
3 elseif scantokens(mpversion) < 1.004: errmessage
4 "MetaPost v1.004 or later required (found v" & mpversion & ")";
5 fi
```

`init_metaflow` Each new figure is initialized by declaring `ip`, `il`, and `cp` as variable classes for item paths, item labels, and connector paths, respectively. The `layer` array is also initialized.

```
6 def init_metaflow =
7   save ip, il, cp, layer;
8   path ip[], cp[];
9   picture il[], layer[];
10  thislayer := 0;
11  layerlist := origin;
12  itemlabels := nullpicture;
13 enddef;
14 extra_beginfig := extra_beginfig & "init_metaflow";
```

At the end of each figure, draw all the item labels and layers. Drawing labels at the end prevents them from being covered by fills.

```
15 extra_endfig := extra_endfig & "flatten";
```

`rradius` The rounded corners of an `rrect` shape have radii `rradius`.

```
16 newinternal rradius;
17 rradius := 5;
```

`pradius` The `popover` macro introduces “pops” of radius `pradius`.

```
18 newinternal pradius;
19 pradius := 3;
```

`cmargin` Connector paths avoid passing within distance `cmargin` of the bounding box of the source or destination shapes. By default we set this to 1.5 times the length of an arrowhead. This prevents bends within connector arrowheads.

```
20 newinternal cmargin;
21 cmargin := 1.5ahlength;
```

`ilmargin` When sizing shapes based on textual labels, the minimum distance from the label to the shape edge in the vertical and horizontal directions is dictated by `ilmargin`.

```
22 newinternal ilmargin;
23 ilmargin := 3;
```

**drumlidratio** Set the default ratio of drum lid height to width.

```

24 newinternal drumlidratio;
25 drumlidratio := .2;

```

**rhombangle** Set the bottom-left angle of rhomboid shapes in degrees. This parameter must be a value between 0 and 180.

```

26 newinternal rhombangle;
27 rhombangle := 80;

```

**braceheight** The following parameters control the appearance of curly braces drawn with the `brace` macro as illustrated in Fig. 8. Specifically,

**clawwidth**

**beekheight**

**braceret**

**beekangle**

**bracethick**

- **braceheight** is the default height of the `c` anchor point above the `a-b` line,
- **clawwidth** is the width of the curved end pieces (and also the symmetric curves at the cusp),
- **beekheight** is the distance from the cusp to an imaginary line that passes through most of the brace,
- **braceret** is the vertical distance between the hill and valley of the curve,
- **beekangle** controls the pointiness of the cusp, and
- **bracethick** is the thickness of the curve at its thickest points.

```

28 newinternal braceheight, clawwidth, beekheight;
29 newinternal braceret, beekangle, bracethick;
30 braceheight := 10;
31 clawwidth := 12;
32 beekheight := 4.5;
33 braceret := 1;
34 beekangle := 10;
35 bracethick := 1.5;

```

**layerlist** The list of layers is stored as a sorted path of integer points along the major diagonal. Its value is reinitialized at the start of each figure, and updated with each layer-change.

```

36 path layerlist;
37 newinternal thislayer;

```

**itemlabels** A picture consisting of all item labels is accumulated separately from the accumulated picture so that all labels can all be drawn together at the end of the figure. This prevents fills from covering labels.

```

38 picture itemlabels;

```

**itemfinal** Users may optionally suppress the final portion of each shape macro, allowing constraints to remain unresolved and delaying the construction of the shape path and the drawing of the label. The following boolean remembers whether we're finalizing the current item now.

```

39 boolean itemfinal;

```

**gensuf** The following macro was adapted from the `generisize` macro in `boxes.mp`. It takes a string version of a suffix (as returned by `str`) and returns a new string in which all explicit numeric subscripts have been replaced by generic brackets (`[]`). Shapes that are presented with non-standard names use this to declare the types of new variables that have the non-standard name as a suffix.

```

40 vardef gensuf(expr s) =
41   save n,r,c; string r,c;
42   n := 0; r := "";
43   forever: exitunless n < length s;
44     c := substring(n,n+1) of s;
45     if (c>="0") and (c<="9"):
46       r := r & "[]";
47       forever: n := n + 1;
48         c := substring(n,n+1) of s;
49         exitunless (c=".") or ((c>="0") and (c<="9"));
50     endfor
51   elseif c="[":
52     if (substring(n+1,n+2) of s)="[":
53       r := r & "[["; n := n + 2;
54     else:
55       r := r & "[]"; n := n + 1;
56       forever: exitunless n < length s;
57         n := n + 1;
58         exitif (substring(n-1,n) of s)="]";
59       endfor
60     fi
61   else:
62     r := r & c; n := n + 1;
63   fi
64 endfor
65 r
66 enddef;

```

**inititem** Initialize a new shape item. All shapes must be named, since at least their positions must be pre-specified, and there is no way to do that without a name. Initialization involves defining the bounding box constraints that are common to all shapes, and parsing any arguments (e.g., the optional label).

```

67 vardef inititem@#(text _t) =
68   if (str @#)="":
69     errmessage("unnamed shape");
70   fi;
71   if known ip@#:
72     errmessage("redundant shape name: " & (str @#));
73   fi;
74   z@#bb.c = z@#c;
75   z@#bb.ur = z@#c + .5z@#s;
76   z@#bb.ll = z@#c - .5z@#s;
77   z@#bb.ul = (x@#bb.ll, y@#bb.ur);
78   z@#bb.lr = (x@#bb.ur, y@#bb.ll);

```

```

79 z@#bb.um = .5[z@#bb.ul,z@#bb.ur];
80 z@#bb.lm = .5[z@#bb.ll,z@#bb.lr];
81 z@#bb.ml = .5[z@#bb.ll,z@#bb.ul];
82 z@#bb.mr = .5[z@#bb.lr,z@#bb.ur];
83 save _pic, _fin; picture _pic; boolean _fin;
84 _fin := true;
85 for __t=_t:
86   if picture __t:
87     _pic = __t;
88   elseif string __t:
89     _pic = __t infont defaultfont scaled defaultscale;
90   elseif boolean __t:
91     _fin := __t;
92   else:
93     errmessage("illegal shape argument type");
94   fi
95 endfor;
96 itemfinal := _fin;
97 if known _pic:
98   z@#ls = urcorner _pic - llcorner _pic;
99   if not picture il@#:
100     scantokens ("picture il." & gensuf(str @#));
101   fi
102   il@# = _pic;
103 fi
104 enddef;

```

**finitem** Finish an item by drawing its optional label, defining its frame path (if there is a properly typed variable to receive it), and returning the frame path so that a drawing command can draw it. Rather than contributing the label directly to the current picture, it is drawn into a separate `labelitems` picture that will be added to the overall picture at the end. This prevents labels from being covered by fills. The path is only stored in a variable if doing so would not cause an error. This allows users to define items with non-standard names without first declaring a path variable when the path variable is never used.

```

105 vardef finitem@#(text p) =
106   if itemfinal:
107     if unknown x@#s: (x@#s,0) = (x@#ds,0) fi;
108     if unknown y@#s: (0,y@#s) = (0,y@#ds) fi;
109     if known il@#:
110       addto itemlabels also
111         (il@# shifted (z@#lc-.5[llcorner il@#,urcorner il@#]));
112     fi
113     if (path ip@#) and (unknown ip@#): ip@#=p; ip@# else: p fi
114   fi
115 enddef;

```

The following macros define shapes. Each shape definition begins with a call to `inititem`, then introduces constraints that tie all anchor points to the bound-

ing box points ( $z@#bb..$ ), then finishes the shape with a call to `finitem`. This ordering is important because it maximizes the chances that constraints can be resolved prior to reaching operations that fail for unresolved constraints.

Whenever an item label is given, each shape defines a default size  $z@#ds$  based entirely on the label size  $z@#ls$ . Some shapes require this relationship to be non-linear; in that case default size constraints are only computed when the label size is fully known.

`rect` Define a rectangular item.

```

116 vardef rect@(text cap) =
117   inititem@(cap);
118   z@#lr = z@#bb.lr;
119   z@#ur = z@#bb.ur;
120   z@#ul = z@#bb.ul;
121   z@#ll = z@#bb.ll;
122   z@#lm = z@#bb.lm;
123   z@#mr = z@#bb.mr;
124   z@#um = z@#bb.um;
125   z@#ml = z@#bb.ml;
126   z@#lc = z@c;
127   z@#ds = z@#ls + (2ilmargin,2ilmargin);
128   finitem@(z@#ll--z@#lr--z@#ur--z@#ul--cycle)
129 enddef;

```

`rrect` Define a rounded rectangular item.

```

130 vardef rrect@(text cap) =
131   inititem@(cap);
132   z@#lm = z@#bb.lm;
133   z@#mr = z@#bb.mr;
134   z@#um = z@#bb.um;
135   z@#ml = z@#bb.ml;
136   z@#ll-z@#bb.ll = z@#bb.ur-z@#ur = rradius*(1-sqrt(.5))*(1,1);
137   z@#lr-z@#bb.lr = z@#bb.ul-z@#ul = rradius*(1-sqrt(.5))*(-1,1);
138   z@#lc = z@c;
139   z@#ds = z@#ls + 2*(if (rradius-ilmargin)*sqrt(2) > rradius-1:
140                       (rradius-(rradius+1)/sqrt(2))*(1,1)
141                       else: (ilmargin,ilmargin) fi);
142   finitem@(
143     (subpath (0,2) of fullcircle scaled 2rradius
144               shifted (z@#bb.ur-(rradius,rradius)))--
145     (subpath (2,4) of fullcircle scaled 2rradius
146               shifted (z@#bb.ul+(rradius,-rradius)))--
147     (subpath (4,6) of fullcircle scaled 2rradius
148               shifted (z@#bb.ll+(rradius,rradius)))--
149     (subpath (6,8) of fullcircle scaled 2rradius
150               shifted (z@#bb.lr-(rradius,-rradius)))--
151     cycle
152   )
153 enddef;

```

**\_rax** This helper macro safely computes the  $x$  that satisfies  $x/y = \tan \theta$  where  $y$  is given and  $\theta$  is rhombangle.

```

154 vardef _rax(expr y) =
155   save ?; numeric ?;
156   (?,y) = whatever * dir rhombangle;
157   ?
158 enddef;

```

**rhomb** Define a rhomboid item.

```

159 vardef rhomb@(text cap) =
160   inititem@(cap);
161   z@#lm = z@#bb.lm;
162   z@#mr = .5[z@#lr,z@#ur];
163   z@#um = z@#bb.um;
164   z@#ml = .5[z@#ll,z@#ul];
165   z@#bb.ur-z@#ur = z@#ll-z@#bb.ll = (whatever,0);
166   z@#bb.ul-z@#ul = z@#lr-z@#bb.lr = (whatever,0);
167   z@#lc = z@#c;
168   z@#ul-z@#ll = whatever * dir rhombangle;
169   if rhombangle<90: z@#ll = z@#bb.ll
170     else: z@#ul = z@#bb.ul fi;
171   if known y@#ls:
172     z@#ds = z@#ls + 2*(abs(_rax(y@#ls+2ilmargin)) +
173                       max(ilmargin-abs(_rax(ilmargin)),0),
174                       ilmargin);
175   fi
176   finitem@(z@#ll--z@#lr--z@#ur--z@#ul--cycle)
177 enddef;

```

**trap** Define a trapezoid item.

```

178 vardef trap@(text cap) =
179   inititem@(cap);
180   z@#lm = z@#bb.lm;
181   z@#mr = .5[z@#lr,z@#ur];
182   z@#um = z@#bb.um;
183   z@#ml = .5[z@#ll,z@#ul];
184   z@#ul-z@#bb.ul = z@#bb.ur-z@#ur = (whatever,0);
185   z@#ll-z@#bb.ll = z@#bb.lr-z@#lr = (whatever,0);
186   z@#lc = z@#c;
187   z@#ul-z@#ll = whatever * dir rhombangle;
188   if rhombangle<90: z@#ll = z@#bb.ll
189     else: z@#ul = z@#bb.ul fi;
190   if known y@#ls:
191     z@#ds = z@#ls + 2*(abs(_rax(y@#ls+2ilmargin)) +
192                       max(ilmargin-abs(_rax(ilmargin)),0),
193                       ilmargin);
194   fi
195   finitem@(z@#ll--z@#lr--z@#ur--z@#ul--cycle)
196 enddef;

```

**diamond** Define a diamond item. The default diamond size is chosen to be the one that minimizes the sum  $a + b$  while still circumscribing the label, where  $a$  and  $b$  are half the width and height of the diamond, respectively. If  $a$  and  $b$  are both free, then it turns out that the optimal diamond satisfies  $a = x + \sqrt{xy}$  and  $b = y + \sqrt{xy}$ , where  $(x, y)$  is the upper right corner of the label when it is centered at the origin.

```

197 vardef diamond@#(text cap) =
198   inititem@#(cap);
199   z@#lm = z@#bb.lm;
200   z@#mr = z@#bb.mr;
201   z@#um = z@#bb.um;
202   z@#ml = z@#bb.ml;
203   z@#ll = .5[z@#bb.lm,z@#bb.ml];
204   z@#lr = .5[z@#bb.lm,z@#bb.mr];
205   z@#ur = .5[z@#bb.um,z@#bb.mr];
206   z@#ul = .5[z@#bb.um,z@#bb.ml];
207   z@#lc = z@#c;
208   if known z@#ls: z@#ds = begingroup
209     save xt, yt; numeric xt, yt;
210     (xt,yt) = .5z@#ls + if x@#ls>y@#ls: (0,ilmargin)
211               else: (ilmargin,0) fi;
212     2*((xt,yt) + sqrt(xt*yt))*(1,1)
213   endgroup; fi
214   finitem@#(z@#lm--z@#mr--z@#um--z@#ml--cycle)
215 enddef;

```

**oval** The default size for ovals is chosen so as to minimize the quantity  $a^2 + b^2$  while still circumscribing the label, where  $a$  and  $b$  are half the lengths of the horizontal and vertical axes, respectively. This avoids highly eccentric ovals in favor of rounder ones. If both  $a$  and  $b$  are free, it turns out that the optimal oval satisfies  $a = \sqrt{x(x+y)}$  and  $b = \sqrt{y(x+y)}$ , where  $(x, y)$  is the upper-right corner of the label when centered at the origin.

```

216 vardef oval@#(text cap) =
217   inititem@#(cap);
218   z@#lm = z@#bb.lm;
219   z@#mr = z@#bb.mr;
220   z@#um = z@#bb.um;
221   z@#ml = z@#bb.ml;
222   z@#ll-z@#bb.ll = z@#bb.ur-z@#ur = .5*(1-sqrt(.5))*z@#s;
223   z@#lr-z@#bb.lr = z@#bb.ul-z@#ul = .5*(1-sqrt(.5))*(-x@#s,y@#s);
224   z@#lc = z@#c;
225   if known z@#ls: z@#ds = begingroup
226     save xt,yt; numeric xt,yt;
227     (xt,yt) = .5z@#ls + if x@#ls>y@#ls: (0,ilmargin)
228               else: (ilmargin,0) fi;
229     2*sqrt(xt+yt)*(sqrt(xt),sqrt(yt))
230   endgroup; fi
231   finitem@#(fullcircle xscaled x@#s yscaled y@#s shifted z@#c)
232 enddef;

```

**circ** Define a circular item.

```

233 vardef circ@(text cap) =
234   inititem@(cap);
235   (x@s,0) = (y@s,0);
236   z#lm = z#bb.lm;
237   z#mr = z#bb.mr;
238   z#um = z#bb.um;
239   z#ml = z#bb.ml;
240   z#ll-z#bb.ll = z#bb.ur-z#ur = .5*(1-sqrt(.5))*z@s;
241   z#lr-z#bb.lr = z#bb.ul-z#ul = .5*(1-sqrt(.5))*(-x@s,y@s);
242   z#lc = z#c;
243   if known z#ls:
244     z#ds = length(z#ls + if x#ls>y#ls: (2ilmargin,0)
245                   else: (0,2ilmargin) fi) * (1,1);
246   fi
247   finitem@(fullcircle scaled x@s shifted z#c)
248 enddef;

```

**drum** Define a drum item. This is currently the only item that does not have a cyclic path for its frame. (The last full circle draws the lid, and does not end at the starting point.) To support fill operators (e.g., `filledwith`), acyclic paths must start with a cycle (which gets filled) and then finish off with a tail (which is ignored during filling). We therefore draw the outer border of the drum first and then finish off with a tail that draws the front of the top lid edge.

```

249 vardef drum@(text cap) =
250   inititem@(cap);
251   z#lm = z#bb.lm;
252   z#mr = z#bb.mr;
253   z#um = z#bb.um;
254   z#ml = z#bb.ml;
255   z#ll-z#bb.ll = z#lr-z#bb.lr = z#bb.ur-z#ur =
256     z#bb.ul-z#ul = 1.5*(z#c-z#lc) = (0,.5drumlidratio*x@s);
257   z#ds = z#ls + (2ilmargin, 2ilmargin + 1.5drumlidratio*x#ls);
258   finitem@(
259     z#ul--(halfcircle xscaled -x@s yscaled (-drumlidratio*x@s)
260           shifted .5[z#ll,z#lr])--
261     (fullcircle xscaled x@s yscaled (drumlidratio*x@s)
262     shifted .5[z#ul,z#ur])
263   )
264 enddef;

```

**tornbox** A box with a wavy bottom edge.

```

265 vardef tornbox@(text cap) =
266   inititem@(cap);
267   interim truecorners := 1;
268   save p,b; path p; numeric b;
269   p = origin{dir -25}..{right}(1,0);
270   b = ypart (llcorner p);
271   z#ul = z#bb.ul;

```

```

272 z@#ur = z@#bb.ur;
273 z@#ll = z@#bb.ll - x@#s*(0,b);
274 z@#lr = (x@#bb.lr,y@#ll);
275 z@#ml = .5[z@#ll,z@#ul];
276 z@#mr = .5[z@#lr,z@#ur];
277 z@#um = .5[z@#ul,z@#ur];
278 z@#lm = z@#ll + x@#s*(p intersectionpoint ((.5,0)--(.5,b)));
279 z@#lc = .5[z@#ml,z@#mr];
280 z@#ds = z@#ls + (2ilmargin,2ilmargin-x@#ls*b);
281 finitem@#(z@#ll{dir -25}..{right}z@#lr--z@#ur--z@#ul--cycle)
282 enddef;

```

**drawopen** Any shape can be “drawn” without its border by using the **drawopen** command instead of **draw**. The implementation simply evaluates and discards its argument.

```
283 def drawopen expr p = enddef;
```

**brace** Draw a curly brace. This is not a shape like the others since it has different anchor points and is intrinsically rotatable (without **rshape**). Therefore, it has its own specialized implementation.

```

284 vardef brace@#(expr o) =
285   save t,u,v,w,bh,ew,ret,h,p;
286   numeric t,w,bh,ew,ret,h;
287   pair u,v;
288   path p;
289   z@#d = t[z@#a,z@#b];
290   u = unitvector (z@#b-z@#a);
291   v = u rotated (if ypart(o rotated -angle u)>0: 90 else: -90 fi);
292   z@#c = z@#d + h*v;
293   if unknown t: t=.5; fi
294   if unknown h: h=braceheight; fi
295   if h<0: v:=-v; h:=-h; fi
296   w = min(length(z@#d-z@#a),length(z@#b-z@#d));
297   bh = min(beeckheight, h/2);
298   ew = min(clawwidth, w/2);
299   ret = braceret/(2clawwidth)*max(0,min(2clawwidth,w-2clawwidth));
300   p = ( % top-left
301         z@#c{-v rotated -beekangle/2} ..
302         {-u}(z@#c -ew*u -(bh+ret/2-bracethick/2)*v){-u} ..
303         {-u}(z@#a +ew*u +(h-bh+ret/2+bracethick/2)*v){-u} ..
304         {-v}z@#a) &
305     ( % bottom-left
306         z@#a{v rotated -beekangle/2} ..
307         {u}(z@#a +ew*u +(h-bh+ret/2-bracethick/2)*v){u} ..
308         {u}(z@#c -ew*u -(bh+ret/2+bracethick/2)*v){u} ..
309         {v}(z@#c -.5bracethick*v)) &
310     ( % bottom-right
311         (z@#c -.5bracethick*v){-v} ..
312         {u}(z@#c +ew*u -(bh+ret/2+bracethick/2)*v){u} ..
313         {u}(z@#b -ew*u +(h-bh+ret/2-bracethick/2)*v){u} ..

```

```

314     {-v rotated beekangle/2}z@#b) &
315     ( % top-right
316     z@#b{v} ..
317     {-u}(z@#b -ew*u +(h-bh+ret/2+bracethick/2)*v){-u} ..
318     {-u}(z@#c +ew*u -(bh+ret/2-bracethick/2)*v){-u} ..
319     {v rotated beekangle/2}z@#c) & cycle;
320   if (path ip@#) and (unknown ip@#): ip@#=-p; ip@# else: p fi
321 enddef;

```

**inback** Execute a drawing command so as to put its results behind everything that has already been drawn.

```

322 def inback text t =
323   begingroup
324     save pic_, ils_;
325     picture pic_,ils_;
326     pic_ = currentpicture;
327     ils_ = itemlabels;
328     currentpicture := nullpicture;
329     itemlabels := nullpicture;
330     t;
331     addto currentpicture also itemlabels;
332     addto currentpicture also pic_;
333     itemlabels := ils_;
334   endgroup
335 enddef;

```

**turntlayer** Switch to a different (possibly already existing) layer.

```

336 vardef turntlayer(expr n) =
337   save t; numeric t;
338   addto currentpicture also itemlabels;
339   itemlabels := nullpicture;
340   layer[thislayer] := currentpicture;
341   thislayer := n;
342   currentpicture := if known layer[n]: layer[n] else: nullpicture fi;
343   layer[n] := nullpicture;
344   t = xpart (layerlist intersectiontimes (n,n));
345   if t=-1:
346     layerlist := if ((n,n)<point 0 of layerlist): (n,n)..layerlist
347                 else: layerlist..(n,n) fi;
348   elseif t>floor t:
349     t := floor t;
350     layerlist := (subpath (0,t) of layerlist)..(n,n)..
351                (subpath (t+1,length layerlist) of layerlist);
352   fi
353 enddef;

```

**flatten** Flatten all layers onto layer 0, and make it current.

```

354 def flatten =
355   addto currentpicture also itemlabels;

```

```

356 if length layerlist>0:
357   layer[thislayer] := currentpicture;
358   currentpicture := nullpicture;
359   for t=0 upto length layerlist:
360     addto currentpicture also layer[xpart point t of layerlist];
361   endfor
362   picture layer[];
363   thislayer := 0;
364   layerlist := origin;
365 fi
366 enddef;

```

**anchor** Convert a direction vector to an anchor point name.

```

367 def anchor(suffix $(expr d) =
368   (if (xpart d)=0:
369     if (ypart d)=0: $c elseif (ypart d)>0: $um else: $lm fi
370     elseif (xpart d)>0:
371       if (ypart d)=0: $mr elseif (ypart d)>0: $ur else: $lr fi
372       elseif (ypart d)=0: $ml elseif (ypart d)>0: $ul else: $ll fi)
373 enddef;

```

**upright** It is helpful to have unit vectors for the ordinal directions in addition to the  
**downright** cardinal ones provided by plain METAPOST.

```

upleft 374 pair upright, downright, upleft, downleft;
downleft 375 upright = -downleft = unitvector (up+right);
376 downright = -upleft = unitvector (down+right);

```

**putitem** Position an item relative to another. If  $\langle d \rangle$  is a vector in a cardinal direction, a constraint is introduced that separates the relevant opposing bounding box mid-points by  $\langle d \rangle$ . Otherwise the constraint is between opposing bounding box corner points.

```

377 vardef putitem[] expr d of i =
378   anchor(z@bb,-d) = (if pair i: i else: anchor(z[i]bb,d) fi) + d
379 enddef;

```

**putitems** Position one pair of items like another pair of items. To get the custom syntax  
**like** `putitems( $i,j$ ) like( $i',j'$ )`, we define macro `putitems` so that it herds its two arguments into a 4-argument `like` macro. In order to introduce the proper constraint, at least one of the two item pairs must have fully known relative positions. The known pair can be safely examined without raising an unresolved constraint error. Based on the results, we introduce new (possibly heretofore unresolved) constraints for the other pair.

```

380 def putitems(suffix $,$$) text t = t($,$$) enddef;
381 vardef like(suffix $,$$,#,#) =
382   save d; pair d;
383   d = if known (z$$c-z$c): z$$c-z$c else: z##c-z#c fi;
384   anchor(z##,-d) - anchor(z#,d) = anchor(z$$,-d) - anchor(z$,d);
385 enddef;

```

```

    _corners Compute the corners of a set of objects.
urcorners 386 vardef _corners(text #,##,op)(expr u)(text t) =
ulcorners 387 interim truecorners := 1;
llcorners 388 save ux_,uy_,v_; numeric ux_,uy_; pair v_;
lrcorners 389 (ux_,uy_) = if pair u: u else: op u fi;
390 for uu = t:
391     v_ := if pair uu: uu else: op uu fi;
392     if (xpart v_)#ux_: ux_:=xpart v_; fi
393     if (ypart v_)#uy_: uy_:=ypart v_; fi
394 endfor
395 (ux_,uy_)
396 enddef;
397 def urcorners = _corners(>)(>)(urcorner) enddef;
398 def ulcorners = _corners(<)(>)(ulcorner) enddef;
399 def llcorners = _corners(<)(<)(llcorner) enddef;
400 def lrcorners = _corners(>)(<)(lrcorner) enddef;

```

**filledwith** Operation ( $\langle p \rangle$  filledwith  $\langle f \rangle$ ) fills a path  $\langle p \rangle$  with a color or picture  $\langle f \rangle$ . If path  $\langle p \rangle$  is acyclic, we look for a cyclic prefix subpath. (This works for drum shapes—the only acyclic shape at present.) If there is none, we just close it to make it a cycle and hope that works.

If  $\langle f \rangle$  is a color, a solid fill is contributed. If it is a picture, it is simply clipped to the path without any centering or tessellation. The other fill operators use this latter functionality to contribute their fill patterns.

```

401 tertiarydef p filledwith f =
402   begingroup
403     save c; path c;
404     c = (if picture p:
405         begingroup interim truecorners := 1;
406         bbox p
407         endgroup
408     elseif cycle p: p
409     else:
410         for t=1 upto length p:
411             if point t of p = point 0 of p:
412                 (subpath (0,t) of p) & cycle
413             elseif t = length p: p..cycle fi
414             exitif point t of p = point 0 of p;
415         endfor
416         fi);
417     if color f:
418         fill c withcolor f;
419     elseif picture f:
420         save pic;
421         picture pic;
422         pic = f;
423         clip pic to c;
424         draw pic;
425     else:

```

```

426     errmessage("non-color/picture argument to filledwith ignored");
427     fi;
428     p
429 endgroup
430 enddef;

```

**tesselatedwith** Create a fill pattern by tessellating a rectangular picture. The tessellation is aligned with the original picture's location, not any reference point of the shape it fills, so that nearby shapes with the same tessellated fill pattern look like windows into an unbroken underlying pattern. This makes nearby shapes with the same fill pattern look more compatible.

```

431 tertiarydef b tesselatedwith p =
432   begingroup
433     save tpic, pic, llx, lly, urx, ury, psizx, psizy;
434     picture tpic, pic;
435     tpic := nullpicture;
436     pic = p;
437     (psizx,psizy) = (urcorner pic) - (llcorner pic);
438     (llx,lly) = (llcorner pic) + ((llcorner b) - (llcorner pic));
439     llx := llx div psizx * psizx;
440     lly := lly div psizy * psizy;
441     (urx,ury) = (urcorner b) + (psizx,psizy);
442     for i = llx step psizx until urx:
443       for j = lly step psizy until ury:
444         addto tpic also (pic shifted (i,j));
445       endfor;
446     endfor;
447     b filledwith tpic
448   endgroup
449 enddef;

```

**stripedwith** Operation ( $\langle b \rangle$  stripedwith  $\langle p \rangle$ ) fills a bounding path  $\langle b \rangle$  with a stripe tessellation obtained by projecting every line segment in picture  $\langle p \rangle$  orthogonally to form a stripe. Zero-length segments (i.e., points) are directionless, so in that case the projection is orthogonal to the direction of the first line segment in the picture, the second line segment if the first one is zero-length, or the direction from the first to the second if the first two are both zero-length. A picture consisting of a single, zero-length line segment is ignored, yielding an empty pattern. All non-lines in the picture are also ignored. Colors of line segments are preserved, allowing multicolored patterns. Pen styles of zero-length line segments are also preserved (since those are projected to lines, for which a pen style makes sense).

```

450 tertiarydef b stripedwith p =
451   begingroup
452     save tpic, pic, pl, e, d, s, r, dl, fp, ll, ur, x, gr;
453     picture tpic, pic;
454     numeric pl, dl, r, gr;
455     pair s, ll, ur;
456     path d, fp;

```

```

457     tpic := nullpicture;
458     pic = p;
459     pl = length ((urcorner pic)-(llcorner pic));
460     for e within pic:
461         if stroked e:
462             d := pathpart e;
463             if ((point 0 of d) <> (point infinity of d)):
464                 gr = angle ((point infinity of d)-(point 0 of d));
465             elseif (point 0 of (pathpart pic)) <> (point 0 of d):
466                 gr = angle ((point 0 of d)-(point 0 of (pathpart pic)));
467             fi;
468         fi;
469         exitif known gr;
470     endfor;
471     if (known gr) and (pl>0):
472         for e within pic:
473             if stroked e:
474                 d := pathpart e;
475                 s := point 0 of d;
476                 dl := length ((point infinity of d)-s);
477                 r := if dl>0: angle ((point infinity of d)-s) else: gr fi;
478                 fp := b shifted -s rotated -r;
479                 ll := llcorner fp;
480                 ur := urcorner fp;
481                 for x = ((xpart ll) div pl*pl) step pl until (xpart ur)+pl:
482                     if dl>0:
483                         addto tpic contour ((x,ypart ll)--(x+dl,ypart ll)--
484                                                 (x+dl,ypart ur)--(x,ypart ur)--cycle)
485                                                 rotated r shifted s withcolor (colorpart e);
486                     else:
487                         addto tpic doublepath ((x,ypart ll)--(x,ypart ur))
488                                                 rotated r shifted s
489                                                 withpen (penpart e) withcolor (colorpart e);
490                     fi;
491                 endfor;
492             fi;
493         endfor;
494     fi;
495     b filledwith tpic
496 endgroup
497 enddef;

```

**dashstripes** Convert a dash pattern to a stripe pattern. Dash patterns are almost valid stripe patterns already, except that they lack proper bounding boxes. METAPOST adopts the peculiar convention of representing a dash pattern as a horizontal series of line segments whose position above the  $y$ -axis is the total width of the pattern. When the last part of the pattern is an “off”, the  $y$ -position of the pattern will therefore be larger than the  $x$ -position of the last dash’s endpoint. To construct a correct bounding box, we therefore just compute the max of the  $x$ - and  $y$ -positions. The

addition of the bounding box allows the stripe pattern to be properly tessellated after rotation, since rotated stripe patterns are no longer horizontal lines with fixed  $y$ -positions.

```

498 vardef dashstripes primary p =
499   save pic, ur;
500   picture pic; pic = p;
501   pair ur; ur = urcorner pic;
502   setbounds pic to
503     (ulcorner pic)--(max(xpart ur,ypart ur), ypart ur)--cycle;
504   pic
505 enddef;

```

**evenstripes** The **evenstripes** and **pinstripes** patterns are the stripe analogs of the **evenly** and **withdots** dash patterns. To make them easier for the user to shift and rotate, we reposition and reorient them so that the stripes run horizontally and are aligned with the  $x$ -axis. The **withdots** dash pattern cannot be directly used to create **pinstripes** because it has only one, zero-length dash, making it directionless. We must therefore construct a doubled version of the **withdots** pattern so that it has two dashes.

```

506 picture evenstripes, pinstripes;
507 evenstripes = dashstripes evenly shifted -(ulcorner evenly)
508               rotated 90;
509 pinstripes = dashstripes dashpattern(on 0 off 5 on 0 off 5)
510             shifted -(0,10) rotated 90;

```

**colored** Operation ( $\langle p \rangle$  **colored**  $\langle c \rangle$ ) recolors a picture  $\langle p \rangle$  a new color  $\langle c \rangle$ . This is useful for changing the color of stripe patterns.

```

511 primarydef p colored c =
512   begingroup
513     save pic;
514     picture pic;
515     pic := nullpicture;
516     addto pic also p withcolor c;
517     pic
518   endgroup
519 enddef;

```

**onhue** To make multicolor stripe patterns, we need a dash pattern constructor like **on** except with an extra color parameter. **METAPOST** does not have any means of defining parameterized binary operators, so to immitate one, we first define macro **onhue**( $\langle c \rangle \langle d \rangle$ ) so that it creates a picture of a  $\langle c \rangle$ -colored, length- $\langle d \rangle$  dash, and then expands to binary operator **\_onhue\_** applied to that picture.

```

520 def onhue(expr c) secondary d =
521   _onhue_
522   begingroup save pic;
523   picture pic; pic=nullpicture;
524   addto pic doublepath (0,d)..(d,d) withcolor c;
525   pic

```

```

526 endgroup
527 enddef;

_onhue_ Binary operation ( $\langle p \rangle$  _onhue_  $\langle d \rangle$ ) adds dash  $\langle d \rangle$  to picture  $\langle p \rangle$ . This is essentially
like on except that  $\langle d \rangle$  is an entire picture, not just a numeric length.

528 tertiarydef p _onhue_ d =
529 begingroup save pic, ur, delta;
530 picture pic; pic=p;
531 pair ur; ur=urcorner d;
532 numeric delta; delta=max(xpart ur,ypart ur);
533 addto pic also d shifted ((w,w)-(llcorner d));
534 w := w+delta;
535 pic shifted (0,delta)
536 endgroup
537 enddef;

connector Return a connector path exiting item  $\langle \$ \rangle$  in direction  $\langle dsrc \rangle$  and entering item
 $\langle \$\$ \rangle$  in direction  $\langle ddst \rangle$ . If the connector is unnamed, give it a temporary name.

538 vardef connector@#(suffix $,$$(expr dsrc,ddst) =
539 if (str @#)="":
540 numeric x[]cp.tmp, y[]cp.tmp;
541 path cp.tmp;
542 _connector.tmp
543 else:
544 if known cp@#:
545 errmessage("redundant connector name: " & (str @#));
546 fi;
547 _connector@#
548 fi($,$$,dsrc,ddst)
549 enddef;

```

There are 16 cases that must be considered for connector paths—one for each exit-entry cardinal direction pair. We can reduce this to 4 cases by first rotating everything so that the exit direction is rightward, solving the resulting connector path problem, and then re-rotating back to the original orientation. This strategy reduces the set of possibilities to the 4 possible entry directions.

Rather than doing the rotation using polar coordinates, which would entail non-linear constraints that METAPOST cannot solve automatically, we formulate the rotation as a reflection and/or juxtaposition of  $x$ - and  $y$ -ordinates. For example, mapping upward to rightward can be achieved by a juxtaposition and then an  $x$ -reflection.

```

_jux This helper macro conditionally juxtaposes and possibly inverts axes in a con-
straint in order to rotate everything so that the exit direction of the connector is
rightward.

550 def _jux(text a,b) =
551 if s.h=s.v: ((a)*s.h,(b)*s.v) else: ((b)*s.v,(a)*s.h) fi
552 enddef;

```

`_iv` This macro chooses amongst 4 choices based on angle `a`. The choices are for up, left, down, and right, respectively.

```

553 def _iv(expr a)(suffix b,c,d,e) =
554   if (45 <= a) and (a < 135): b
555   elseif (135 <= a) and (a < 225): c
556   elseif (225 <= a) and (a < 295): d
557   else: e fi
558 enddef;

```

`_connector` Rotate a connector path problem so that the exit direction is rightward, and then invoke the appropriate sub-logic for the appropriate (rotated) entry direction. Variables `i<n>r`, `i<n>l`, `i<n>t`, and `i<n>b` store the right, left, top, and bottom ordinates (respectively) of the source ( $n = 0$ ) and destination ( $n = 1$ ) items *after rotation*. Variables `s.h` and `s.v` store  $-1$  if the horizontal or vertical direction (respectively) is being reflected after rotation, and  $1$  otherwise.

```

559 vardef _connector@#(suffix $,$$(expr dsrc,ddst) =
560   save i, s;
561   numeric i[]a, i[]r, i[]l, i[]t, i[]b, i[]x, i[]y, s.h, s.v;
562   i0a = (angle dsrc) mod 360;
563   i1a = (angle -ddst) mod 360;
564   s.h = (if (135 <= i0a) and (i0a < 295): -1 else: 1 fi);
565   s.v = (if (45 <= i0a) and (i0a < 225): -1 else: 1 fi);
566   _jux(i0l)(i0b) = z$bb _iv(i0a,lr,ur,ul,ll);
567   _jux(i0r)(i0t) = z$bb _iv(i0a,ul,ll,lr,ur);
568   _jux(i1l)(i1b) = z$$bb _iv(i0a,lr,ur,ul,ll);
569   _jux(i1r)(i1t) = z$$bb _iv(i0a,ul,ll,lr,ur);
570   _jux(i0x)(i0y) = z$ _iv(i0a,um,ml,lm,mr);
571   _jux(i1x)(i1y) = z$$ _iv(i1a,um,ml,lm,mr);
572   _iv((i1a-i0a+360) mod 360,
573       _conn_down,_conn_right,_conn_up,_conn_left)@#
574 enddef;

```

`_conpath` Each `_conn_<dir>` macro (below) concludes with a call to the following macro, which re-rotates back to the original exit direction and returns the resulting connector path. The input to the macro is the suggested series of alternating  $x$ - and  $y$ -ordinates for the (rotated) path. Each ordinate is overridden with a user-supplied choice if it has already been defined by the user.

```

575 vardef _conpath@#(text tail) =
576   save n,h;
577   numeric n;
578   boolean h;
579   h := (s.h = s.v);
580   if unknown x0cp@#: x0cp@# = (if h: i0x*s.h else: i0y*s.v fi) fi;
581   if unknown y0cp@#: y0cp@# = (if h: i0y*s.v else: i0x*s.h fi) fi;
582   n := 0;
583   for o=tail:
584     if h:
585       if unknown y[n+1]cp@#: y[n+1]cp@# = y[n]cp@#; fi;

```

```

586     if unknown x[n+1]cp@#:
587         x[n+1]cp@#*(if odd n: s.v else: s.h fi) = o; fi;
588     else:
589         if unknown x[n+1]cp@#: x[n+1]cp@# = x[n]cp@#; fi;
590         if unknown y[n+1]cp@#:
591             y[n+1]cp@#*(if odd n: s.v else: s.h fi) = o; fi;
592         fi;
593         h := not h;
594         n := n+1;
595     endfor;
596     if (unknown cp@#) and (numeric cp@#): path cp@#; fi;
597     cp@# = z0cp@# for j=1 upto n: --z[j]cp@# endfor;
598     cp@#
599 enddef;

```

The following macros solve the connector path problem for each of the possible entry directions. They all assume that the exit direction is rightward.

`_conn_right` Compute a right-exiting, right-entering connector path.

```

600 vardef _conn_right@# =
601     if (i0y=i1y) and (i0x <= i1x):
602         _conpath@#(i1x)
603     elseif (i0r+2cmargin <= i1l) or
604         ((i0x <= i1x) and
605         (i1b < i0t+2cmargin) and (i1t > i0b-2cmargin)):
606         _conpath@#(.5[i0r,i1l],i1y,i1x)
607     elseif (i1b >= i0t+2cmargin) or (i1t <= i0b-2cmargin):
608         _conpath@#(i0r+cmargin,.5[i0t,i1b],i1l-cmargin,i1y,i1x)
609     elseif (i1y <= i0y):
610         _conpath@#(i0r+cmargin,min(i0b,i1b)-cmargin,i1l-cmargin,i1y,i1x)
611     else:
612         _conpath@#(i0r+cmargin,max(i0t,i1t)+cmargin,i1l-cmargin,i1y,i1x)
613     fi
614 enddef;

```

`_conn_up` Compute a right-exiting, up-entering connector path.

```

615 vardef _conn_up@# =
616     if (i1l >= i0r+2cmargin) and (i1y < i0y+cmargin):
617         _conpath@#(.5[i0r,i1l],i1b-cmargin,i1x,i1y)
618     elseif (i1y < i0y) or
619         ((i1x < i0l) and (i1y <= i0t+2cmargin)):
620         _conpath@#(max(i0r,i1r)+cmargin,min(i0b,i1b)-cmargin,i1x,i1y)
621     elseif (i1x <= i0r) or
622         ((i1x < i0r+cmargin) and (i1b >= i0t+2cmargin)):
623         _conpath@#(i0r+cmargin,.5[i0t,i1b],i1x,i1y)
624     else:
625         _conpath@#(i1x,i1y)
626     fi
627 enddef;

```

`_conn_down` Compute a right-exiting, down-entering connector path.

```
628 vardef _conn_down@# =
629   if (i1l >= i0r+2cmargin) and (i1y > i0y-cmargin):
630     _conpath@#(.5[i0r,i1l],i1t+cmargin,i1x,i1y)
631   elseif (i1y > i0y) or
632     ((i1x < i0l) and (i1y <= i0b-2cmargin)):
633     _conpath@#(max(i0r,i1r)+cmargin,max(i0t,i1t)+cmargin,i1x,i1y)
634   elseif (i1x <= i0r) or
635     ((i1x < i0r+cmargin) and (i1b <= i0b-2cmargin)):
636     _conpath@#(i0r+cmargin,.5[i0b,i1t],i1x,i1y)
637   else:
638     _conpath@#(i1x,i1y)
639   fi
640 enddef;
```

`_conn_left` Compute a right-exiting, left-entering connector path.

```
641 vardef _conn_left@# =
642   if (i1x <= i0l-2cmargin) and
643     (i1y <= .5[i0b,i0t]) and (i1y > i0b-cmargin):
644     _conpath@#(i0r+cmargin,i0b-cmargin,.5[i0l,i1r],i1y,i1x)
645   elseif (i1x <= i0l-2cmargin) and
646     (i1y > .5[i0b,i0t]) and (i1y < i0t+cmargin):
647     _conpath@#(i0r+cmargin,i0t+cmargin,.5[i0l,i1r],i1y,i1x)
648   elseif (i1l >= i0r+2cmargin) and
649     (i1b < i0y+cmargin) and (i1t > i0y-cmargin):
650     if (abs(i1t-i0y) < abs(i0y-i1b)):
651       _conpath@#(.5[i0r,i1l],i1t+cmargin,i1r+cmargin,i1y,i1x)
652     else:
653       _conpath@#(.5[i0r,i1l],i1b-cmargin,i1r+cmargin,i1y,i1x)
654     fi
655   else:
656     _conpath@#(max(i0r,i1r)+cmargin,i1y,i1x)
657   fi
658 enddef;
```

`rshape` Create a rotated shape. Known bug: `rshape` might not work with a non-integer name.

```
659 vardef rshape@#(suffix $(expr d)(text cap) =
660   save a,s;
661   a = (angle d) mod 360;
662   s.h = (if (135 <= a) and (a < 315): -1 else: 1 fi);
663   s.v = (if (45 <= a) and (a < 225): 1 else: -1 fi);
664   _jux(x@#c)(y@#c) = z.xf@#c;
665   _jux(x@#lc)(y@#lc) = z.xf@#lc;
666   forsuffixes u=s,ls,ds:
667     z@#u = (if s.h=s.v: z.xf@#u else: (y.xf@#u,x.xf@#u) fi);
668   endfor
669   forsuffixes u=,bb:
670     _jux(x@#u.ul)(y@#u.ul) = z.xf@#u _iv(a,ul,ur,lr,ll);
```

```

671   _jux(x@#u.ml)(y@#u.ml) = z.xf@#u _iv(a,ml,um,mr,lm);
672   _jux(x@#u.ll)(y@#u.ll) = z.xf@#u _iv(a,ll,ul,ur,lr);
673   _jux(x@#u.lm)(y@#u.lm) = z.xf@#u _iv(a,lm,ml,um,mr);
674   _jux(x@#u.lr)(y@#u.lr) = z.xf@#u _iv(a,lr,ll,ul,ur);
675   _jux(x@#u.mr)(y@#u.mr) = z.xf@#u _iv(a,mr,lm,ml,um);
676   _jux(x@#u.ur)(y@#u.ur) = z.xf@#u _iv(a,ur,lr,ll,ul);
677   _jux(x@#u.um)(y@#u.um) = z.xf@#u _iv(a,um,mr,lm,ml);
678   endfor
679   inititem@#(cap);
680   if itemfinal:
681     save pth; path pth;
682     pth = $.xf@#() rotated ((a-90) div 90 * 90);
683     finitem@#(pth)
684   else:
685     $.xf@#(false)
686   fi
687 enddef;

```

**supertime** Translate a time along a subpath to a time along its superpath. That is, if  $p' = \text{subpath}(t_1, t_2)$  of  $p$  and  $t = \text{supertime } t'$  of  $(t_1, t_2)$ , then point  $t$  of  $p = \text{point } t'$  of  $p'$ .

```

688 vardef supertime expr t of b =
689   save s,e; (s,e) = b;
690   if t<=-1: t
691   elseif t<=1:
692     t[s,if e<s: max(ceiling(s)-1,e) else: min(floor(s)+1,e) fi]
693   elseif t<=abs(floor(e)-floor(s)):
694     if e<s: ceiling(s)-t else: floor(s)+t fi
695   elseif t<=abs(floor(e)-floor(s))+1:
696     (t-floor(t))[if e<s: ceiling(e) else: floor(e) fi,e]
697   else: t fi
698 enddef;

```

**\_\_poppath** Reserve a global array for storing arrays of paths used in computing popovers.

```

699 path __poppath[];

```

**popover** The top-level popover macro has syntax like a binary operator, but its second argument is a list of paths, which is not a legal data type in METAPOST. We therefore evaluate and store the paths into a path array first, and then expand to a real binary operator. Note that each path expression might itself contain a popover macro, so some careful grouping is required.

```

700 def popover(text pths) =
701   _popover begingroup
702     save __n;
703     __n:=0;
704     for x=pths:
705       __poppath[__n] = begingroup save __poppath; x endgroup;
706       __n := __n + 1;
707     endfor

```

```

708   __n
709 endgroup
710 enddef;

```

`_popover` Next, a special case is required for cycles. If a cycle has an intersection near its endpoints, it is first re-parameterized to shift its endpoint away from the intersection. This allows the rest of the code to safely treat the path as a non-cycle.

```

711 tertiarydef p _popover n =
712   if cycle p: begingroup
713     save t,u,c,q,r,s; path c,q,r,s;
714     c = fullcircle scaled 2pradius shifted point 0 of p;
715     t = xpart (p intersectiontimes c);
716     u = xpart ((reverse p) intersectiontimes c);
717     if (t<0) or (u<0): p else:
718       q = subpath (0,t) of p;
719       r = subpath (0,u) of reverse p;
720       for i=0 upto n-1:
721         if xpart(q intersectiontimes __poppath[i])>=0:
722           s = __popover(subpath (-u,length p - u) of p,n) -- cycle;
723         elseif xpart(r intersectiontimes __poppath[i])>=0:
724           s = __popover(subpath (t,length p + t) of p,n) -- cycle;
725         fi
726       exitif known s;
727     endfor
728     if known s: s else: __popover(p,n) & cycle fi
729   fi
730 endgroup else: __popover(p,n) fi
731 enddef;

```

`__popover` The following macro returns a new path like  $p$  except spliced with circular arcs of radius `pradius` everywhere  $p$  intersects one of the  $n$  paths in the `__poppath` array. Intersections closer than `pradius` to one another or to the ends of the path are ignored. The pops try to prefer upward and rightward pop directions except when  $p$  is bent at the point of intersection. In that case, the pops take the “long way” around the circle to maximize visibility.

```

732 vardef __popover(expr p,n) =
733   save t;
734   t := -1;
735   for i=0 upto n-1:
736     t := xpart(p intersectiontimes __poppath[i]);
737     exitif t>=0;
738   endfor
739   if t<=0: p else:
740     save i,c,st,et,sv,ev,a; pair i,sv,ev; path c;
741     i = point t of p;
742     c = fullcircle scaled 2pradius shifted i;
743     st = xpart ((subpath (t,0) of p) intersectiontimes c);
744     et = xpart ((subpath (t,length p) of p) intersectiontimes c);
745     if (st<0) or (et<0): p else:

```

```

746     st := supertime st of (t,0);
747     et := supertime et of (t,length p);
748     sv = point st of p - i;
749     ev = point et of p - i;
750     a = angle(ev rotated -angle sv);
751     __popover(subpath (0,st) of p, n) --
752     (if (abs(a)>=179):
753         if (-91<angle ev) and (angle ev<89): reverse fi
754         elseif a>0: reverse fi
755         fullcircle zscaled 2sv cutafter (origin--2ev) shifted i --
756     __popover(subpath (et,length p) of p, n)
757     fi
758     fi
759 enddef;

```

**cfilldraw** Create a macro like `filldraw` except that it draws without filling when its argument is an acyclic path.

```

760 def cfilldraw expr p =
761   addto currentpicture
762   if cycle p: contour else: doublepath fi p
763   withpen currentpen _op_
764 enddef;

```

**\_finarr** This replaces the `filldraw` commands in the `drawarrow` macro with `cfilldraw`, so that the `arrowhead` macro may return an acyclic path that is simply drawn, not filled.

```

765 vardef _finarr text t =
766   draw _apth t;
767   cfilldraw arrowhead _apth t
768 enddef;

```

**\_findarr** Likewise, this replaces the `filldraw` commands in the `drawdblarrow` macro with `cfilldraw`.

```

769 vardef _findarr text t =
770   draw _apth t;
771   cfilldraw arrowhead _apth withpen currentpen t;
772   cfilldraw arrowhead reverse _apth withpen currentpen t;
773 enddef;

```

The default METAPOST code for arrowheads has an aesthetic flaw that we here correct. It computes the front edge of an arrowhead for path  $p$  by rotating the subpath  $q$  of points within distance `ahlength` of  $p$ 's endpoint both `ahangle/2` degrees clockwise and counter-clockwise, forming a pointed vee. This works when the path is linear, but when it's curved, two problems arise: (1) Subpath  $q$  is slightly too long—the distance along  $q$  is greater than `ahlength` (though the straight-line chord from its start point to endpoint is indeed `ahlength`). (2) The back edge of the arrowhead is not orthogonal to  $p$  where they intersect, making the arrowhead look noticeably lopsided (see Fig. 14(a)).

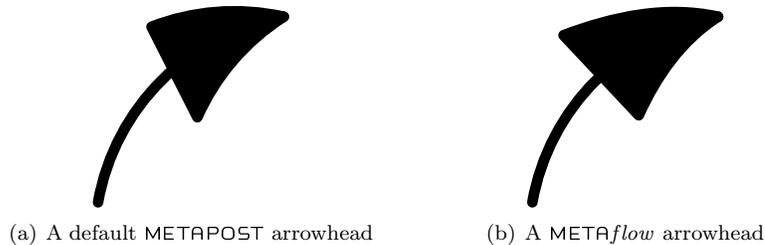


Figure 14: Arrowheads before and after correction

A correct arrowhead (see Fig. 14(b)) should instead be the result of projecting each point  $t$  orthogonally to the direction of  $p$  at  $t$ . Thus, the half of the arrowhead projected outside curve  $p$  should be longer than the half projected inside the curve, making the straight connecting line exactly orthogonal to  $p$ . In general, the direction of the arrowhead's edge at each point  $t$  should be the direction of  $p$  at point  $t$  rotated  $\text{ahangle}/2$  degrees inward toward  $p$ .

The exact formula for this curve is not generally representable as a cubic Bézier curve (see research on *offset curves*), but it can be reasonably approximated by computing the proper points and trajectories at integer times  $t$  and letting METAPOST interpolate the rest.

**taper** Compute a new path that tapers toward path  $\langle p \rangle$  until it intersects  $\langle p \rangle$  at its endpoint forming angle  $\langle a \rangle$ .

```

774 vardef taper(expr p,a) =
775   save r;
776   numeric r;
777   r = sind(a)/cosd(a);
778   (point 0 of p +
779     r * arclength p * unitvector direction 0 of p rotated 90)
780   {(direction 0 of p) rotated -a}
781   for t=1 upto (length p)-1:
782     .. {(point t of p - precontrol t of p) rotated -a}
783     (point t of p +
784       r * (arclength subpath (t,length p) of p) *
785       dir (.5[angle (point t of p - precontrol t of p),
786         angle (postcontrol t of p - point t of p)] + 90))
787     {(postcontrol t of p - point t of p) rotated -a}
788   endfor
789   .. {(direction length p of p) rotated -a}(point length p of p)
790 enddef;

```

**sarrowhead** A straight arrowhead has a straight line for its back edge.

```

791 vardef sarrowhead expr p =
792   save q; path q;
793   q = subpath (arctime (arclength p - ahlength) of p,length p) of p;
794   (taper(q,.5ahangle) &

```

```

795   reverse taper(q,-.5ahangle) -- cycle)
796 enddef;

oarrowhead An open arrowhead is unfilled.
797 vardef oarrowhead expr p =
798   save q; path q;
799   q = subpath (arctime (arclength p - ahlength) of p,length p) of p;
800   (taper(q,.5ahangle) &
801     reverse taper(q,-.5ahangle))
802 enddef;

varrowhead A V-arrowhead insets the back with a V-shape.
803 vardef varrowhead expr p =
804   save va,q,qq;
805   numeric va;
806   path q,qq;
807   va = angle (ahinset*ahlength,
808               ahlength*sind(.5ahangle)/cosd(.5ahangle));
809   q = subpath (arctime (arclength p - ahlength) of p,length p) of p;
810   qq = subpath (0,arctime ahinset*ahlength of q) of q;
811   (reverse taper(qq,va) ..
812     taper(q,.5ahangle) &
813     reverse taper(q,-.5ahangle) ..
814     taper(qq,-va) & cycle)
815 enddef;

ahinset The depth of the V in a V-arrow is determined by the value of ahinset which
        should be a number between 0 and 1. The larger the number, the deeper the V.
816 newinternal ahinset;
817 ahinset := 0;

arrowhead Replace METAPOST's default arrowhead macro with one that chooses the arrow-
        head type based on the value of ahinset.
818 vardef arrowhead expr p =
819   if ahinset <= 0: sarrowhead
820   elseif ahinset >= 1: oarrowhead
821   else: varrowhead fi p
822 enddef;

```