

Ensemble Solar Forecasting Statistical Quantification and Sensitivity Analysis

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Abstract— Uncertainties associated with solar forecasts present challenges to maintain the existing grid reliability especially at high solar penetrations. This study aims to quantify the errors associated with the day-ahead solar forecast parameters and the theoretical solar power output for a 51kW solar plant in a utility area in the state of Vermont, U.S. Forecasts were generated by three numerical weather prediction (NWP) models, including the Rapid Refresh (RAP), the High Resolution Rapid Refresh (HRRR), and the North American Model (NAM), and a machine learning ensemble model. A photovoltaic (PV) performance model was adopted to calculate theoretical solar power generation using the forecast parameters (e.g., irradiance, cell temperature, and wind speed). Errors of the power outputs were quantified, using statistical moments and a suite of metrics, such as the normalized root mean squared error (NRMSE). In addition, the PV model's sensitivity to different forecast parameters was quantified and analyzed. Results showed that the ensemble model yielded forecasts in all parameters with the smallest NRMSE. The NRMSE of solar irradiance forecasts of the ensemble NWP model was reduced by 28.10% compared to the best of the three NWP models. Furthermore, the sensitivity analysis indicated that the errors of the forecasted cell temperature only attributed approximately 0.12% to the NRMSE of the power output as opposed to 7.44% from the forecasted solar irradiance.

Keywords- solar forecasting; uncertainty; numerical weather prediction; machine learning; sensitivity analysis

I. INTRODUCTION

Solar power installation has accelerated rapidly in the United States due to the establishment of state Renewable Portfolio Standards and the decreasing price of photovoltaic (PV) system components [1]. Solar power has been predicted to provide 14% of the U.S electricity needs by 2030 and 27% by 2050 [2]. However, the uncertainty and variability of solar power create challenges for grid operators to manage the increasing integration of solar power while ensuring its continued reliability. Thus, solar power forecasting is important in different operating timeframes from real-time to years to proactively integrate solar power. Longer range forecasts at time horizons beyond weeks ahead help with operation management and planning, maintenance planning, etc. Day-ahead forecast is useful for unit commitment planning and scheduling of

slow starting thermal units to ensure the balance between generation and anticipated load. Operating schedules are adjusted as they get closer to real-time accounting for minutes- to hours- ahead forecasts. Forecasts are valuable in assisting operators to manage power systems' reliability and to improve the economic efficiency [3-4]. However, forecasts inaccuracies can result in issues in power system scheduling, which may lead to significant economic consequences [5]. In addition to the improving the accuracy of forecasts, it is also critical to better understand the uncertainties inherent in solar power forecasts.

A. Overview of Solar Forecasting

Different forecasting methods have been developed to forecast solar irradiance and power at time horizons of minutes-, hours-, and days- ahead, including physical-based, statistical-based, and hybrid approaches. The physical approaches, like cloud movement tracking and numerical weather prediction (NWP) models, rely on weather forecasts and solar panels specification to generate solar power forecasts [6-8]. Short-term irradiance forecasts, based on cloud formation using satellite and ground observation, range from 3 minutes up to 6 hours, ahead of the operating point [9]. For forecast horizons beyond 6 hours, NWP models tend to outperform the cloud movement based forecast [10]. Furthermore, ensemble of individual NWP forecasts using machine learning techniques has been shown to have better accuracies than individual forecasts [11]. NWP models are generally used in conjunction with PV performance simulation tools, like PV Lib and PVWatts [12-13], to convert harvested solar irradiance to solar power. Statistical approaches, such as regressive modeling and artificial neural networks (ANNs) [14-15], yield power forecasts based on historical data and exogenous variables at time horizons ranging from 5 minutes up to 6 hours [16]. Hybrid forecast methods, such as inputting processed satellite images as inputs to ANNs [17], and utilizing Model Output Statistics for ensemble NWP forecasts [18], combine both physical- and statistical-based approaches to yield enhanced forecasts.

B. Research Objectives

This research aims to better understand the day-ahead solar forecasting errors of three regional NWP models and an

ensemble machine learning model through statistical quantification and to compare their relative performances. The three studied NWP models are the Rapid Refresh (RAP), the High Resolution Rapid Refresh (HRRR), and the North America Model (NAM). The PV Lib tool was used to calculate the theoretical solar power generation using the forecasted parameters as inputs [12]. Error statistics of meteorological parameters and solar power were examined at a 51kW solar plant in a utility area in Vermont, U.S. The sensitivity of power output to each forecast parameter was also studied to determine the critical parameters in solar forecasting.

The remainder of the paper is organized as follows. Section II summarizes the forecast models and methods used in this study. The results and discussion are presented in Section III. Conclusion and suggestions for future research are included in the final section.

II. DATA AND METHODS

A. NWP Models and Ensemble Machine-Learning Model

Regional NWP models, such as RAP, HRRR, NAM, forecast atmospheric state based on initial conditions defined by the global NWP models and vertical atmospheric profile. The three studied regional models were able to forecast atmospheric state at different resolution and time horizons, as shown in Table I [11]. Due to the coarse-graining of the physical atmospheric state, the regional NWP forecasts often have errors dependent on the current weather situation category. To enhance the accuracy of solar forecasts, the ensemble forecasting model, named Watt-Sun [11, 19], was developed by the IBM in collaboration with NREL, Argonne, Northeastern University, etc. as part of the project work performed under the SunShot Initiative’s “Improving the Accuracy of Solar Forecasting program.” [20] The ensemble forecasts leverage machine-learning based approach to account for categorization parameters, like cloud liquid water, ice contents, etc. in addition to the parameters of direct interests, such as solar irradiance and temperature, etc. The categorization parameters create specific weather categories exhibiting the condition dependent errors in each model. Thus, the machine learning model is trained using both sets of parameters from multiple regional models and measurement of prediction parameters to yield improved forecasts [11]. Forecasts generated by both the ensemble model and the individual NWP models, were examined in this study.

TABLE I. RESOLUTION AND FORECASTING HORIZON OF THE NWP MODELS

Model	Spatial Resolution and Coverage	Temporal Resolution	Forecasting Horizon
RAP	13 km	15 min 2-Dimension 1 h 3-Dimension	18 h
HRRR	3 km	15 min 2-Dimension 1 h 3-Dimension	15 h
NAM	5 km	1 h	0-60 h

B. PV Performance Model

The PV performance model, PV Lib was adopted in this study to convert available solar irradiance to PV AC power generation at a specific location. Forecasts parameters (e.g., irradiance, cell temperature) generated from the NWP models and the ensemble model were used as the two major inputs to yield power generation. The first variable is effective irradiance, which refers to total amount of plane of array (POA) irradiance adjusted for angle of incidence losses, soiling, and spectral mismatch. An assumption of moderate cleaned PV arrays with 2% irradiance loss was made [21]. Other than directly forecasted cell temperature, the cell temperature can also be calculated in PV Lib, based on module materials, incident irradiance, ambient temperature, and wind speed at 10m. More details of the PV Lib model can be found in [12].

C. Data Summary

Hourly solar forecasts from the NWP models and the ensemble model of a 51kW solar plant were analyzed. Forecast parameters include POA irradiance, solar irradiance components (direct normal irradiance (DNI), diffuse horizontal irradiance (DHI), and global horizontal irradiance (GHI)), ambient temperature (T_A), cell temperature (T_C), and wind speed (WS). Measurements of four parameters were taken hourly at the site. Hourly data was available from 7am to 10pm between July 2013 and February 2014. Parameters available from measurements and different models are marked with “+”, as shown in Table II. In this study, to minimize bias errors introduced by relatively small irradiance values, hourly data with measured irradiance less than the threshold irradiance of 5 W/m² were removed [22].

D. Statistical Metrics

Three types of errors present in the process of solar forecasts, including measurement errors due to the measuring devices for different parameters, forecast errors, and irradiance-to-power model errors. In this study, measurement errors were assumed to be negligible due to the limited information about the measurement device. The forecast errors and the model errors are the major focus of this study.

This section presents the statistical metrics used to quantify the forecast errors associated with the parameters and power outputs. The accuracy of the major forecasted inputs and power outputs was determined by comparing them to the measurements. The associated errors were defined as forecast values minus measurement. A suite of metrics have been proposed in [23] to evaluate the performance of solar forecasts. In this paper, the errors were characterized by four statistical moments, mean, variance, skewness, and kurtosis. In addition, the 1st order error measurement, mean absolute error (MAE), and the 2nd order error measurement, root mean squared error (RMSE), were also used to quantify the forecast errors. RMSE provides an overall error measure throughout the forecasting period while weighing heavily on the extreme forecast errors, whereas MAE provides an overall error measure without punishing the extreme forecast-errors [23, 24]. Normalized root mean squared errors percentage (NRMSE (%)) and normalized mean absolute errors

percentage (NMAE (%)) were also calculated to compare the performance across four models. Forecast errors of each parameter and power output were normalized by the corresponding capacity values, i.e. 1000 W/m^2 for irradiance, 19.54°C based on the average measured cell temperature, and 51 kW for the analyzed solar plant.

Wind speed is also an input of the PV Lib model. A power law was used to estimate the measured wind speed at 10m, assuming that the solar plant location has neutral atmospheric conditions,

$$WS_{10} = WS_2 \times \left(\frac{Z_{10}}{Z_2} \right)^{\frac{1}{7}} \quad (1)$$

where Z is the elevation (m) [25].

In order to analyze and compare the forecast errors at different cloudy condition, the daily average cloudy conditions were characterized by using the daily average clearness index (k^*), which is the ratio of the forecasted (or measured irradiance) to the irradiance from the clear sky model [26]. Based on the daily average clearness index, data were then categorized into different cloud conditions [27], as shown in Table III.

TABLE II. AVAILABLE PARAMETERS FROM DIFFERENT MODELS AND MEASUREMENT

Parameters	Measurement	RAP	HRRR	NAM	Ensemble
AC Power (W)	+				
POA (W/m^2)	+	+	+	+	+
GHI (W/m^2)		+	+	+	
DNI (W/m^2)		+	+	+	
DHI (W/m^2)		+	+	+	
T_c ($^\circ\text{C}$)	+	+	+	+	+
T_A ($^\circ\text{C}$)		+	+	+	
WS_2 (m/s)	+				+
WS_{10} (m/s)		+	+	+	

TABLE III. CLEARNESS INDEX CATEGORIZATION

Clearness Index (k^*)	Cloud Conditions Category
$k^* \leq 0.3$	Overcast
$0.3 < k^* \leq 0.7$	Mostly cloudy
$0.7 < k^* \leq 1$	Partly cloudy
$k^* > 1$	Sunny

E. Sensitivity Analysis

Theoretical power generation was computed using the PV Lib. A design of experiments was applied to generation a total of 13 scenarios based on the inputs extracted from the measurements and the forecast models, as shown in Table IV. Through comparison of outputs from different scenarios in the sensitivity analysis, the errors of the power outputs were investigated to pinpoint the inputs that have a larger influence on the power output and to evaluate forecast models' performance. Identifying the critical parameters could allocate necessary efforts to reduce forecast errors associated with the specific parameters.

At the beginning of the sensitivity analysis, systematic errors attributed by the PV Lib model was quantified by inputting both measured POA and measured T_c in scenario A1. Systematic errors calculated in A1 were later used to subtract from the errors calculated in the following case

studies as a way to account for the model error. The first case study focused on examining the sensitivity of power outputs to irradiance in comparison to cell temperature in the ensemble model. Errors associated with power outputs based on both measured and forecasted inputs of effective irradiance and cell temperature from the ensemble model were compared in scenarios B1-3. The second case study compared the performance of the power outputs between individual forecast models and the ensemble model. Forecasted parameters from each model were used to convert to solar power in scenarios B-, C-, D-, and E-1. The third case study investigated the effects of individual solar irradiance components and POA irradiance on calculated cell temperature and on power forecasts in each NWP model in scenarios C-, D-, E-1, C-, D-, E-2 and C-, D-, E-3. Through the sensitivity analysis, optimal combinations of forecast inputs are identified to yield more accurate power forecasts.

TABLE IV. SCENARIOS SIMULATED IN THE PV LIB MODEL

Scenarios	Input 1 - Effective Irradiance	Input 2 - Cell Temperature
<i>Measurement</i>		
A1	Measured POA	Measured T_c
<i>Ensemble Model</i>		
B1	Forecasted POA	Forecasted T_c
B2	Measured POA	Forecasted T_c
B3	Forecasted POA	Measured T_c
<i>RAP, HRRR, NAM</i>		
C, D, E1	Forecasted POA	Forecasted T_c
C, D, E2	Forecasted POA	Calculated cell temperature ($T_{c,c}$) based on forecasted POA & T_A & WS_{10}
C, D, E3	Forecasted POA	Calculated cell temperature ($T_{c,c}$) based on forecasted GHI , DNI , and DHI & T_A & WS_{10}

III. RESULTS AND DISCUSSION

A. Error Quantification of Forecast Parameters

This section presents the forecast errors associated with the POA irradiance, T_c , and WS_{10} . Table V shows that the ensemble model forecasts have the smallest errors in all forecast parameters. The RMSE of POA forecast from RAP, HRRR, NAM is 240.88 , 275.42 , and 254.59 W/m^2 , respectively. The RMSE of ensemble POA forecast using machine-learning approach based on additional categorization parameters is 173.18 W/m^2 , which is approximately 28.10 % of error reduction compared to the best of the individual model. Similarly, the ensemble forecast in cell temperature and wind speed also enabled error reductions than the best of individual NWP.

In correlating the error statistics of irradiance forecasts and the clearness index distribution in Fig. 1, the ensemble model was found to have the largest number of days with correct forecasted cloud conditions, as shown in Table VI. Forecast models were found to predict accurate cloud condition most often on sunny days. However, due to the use of POA irradiance instead of GHI , the predictions of the cloud structure in a larger spatial area might be limited.

The performance of different parameters forecast is sensitive to the NWP models. The NRMSE (%) of POA irradiance forecasts generated by the RAP was the smallest, which was approximately 24.09%. As for cell temperature forecasts, the NAM had the smallest NRMSE (%), which was about 35.79 %. Lastly, the HRRR had the smallest NRMSE (%) for WS_{10} forecasts. The observed better forecasts in a specific forecast model could be caused by the unique spatial and temporal resolutions utilized in each NWP model. It is important to note that these results are observed at the specific studied location, which may not apply to other sites.

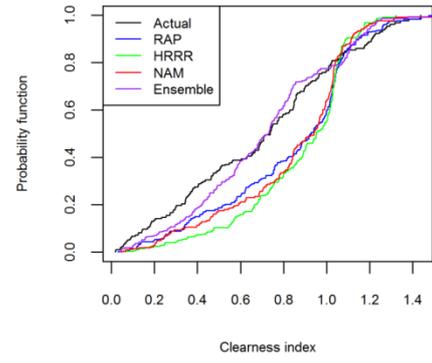


Figure 1. Cumulative distribution of daily clearness index for measurement, three NWP models, and the ensemble model

TABLE V. STASTICAL QUANTIFICATION OF ERROR ASSOCIATED WITH FORECAST PARAMETERS

Plane of Array Irradiance (POA)								
Metrics	Mean (W/m^2)	STD (W/m^2)	Skewness	Kurtosis	RMSE (W/m^2)	NRMSE (%)	MAE (W/m^2)	NMAE (%)
RAP	108.70	215.02	0.71	5.26	240.88	24.09	161.51	16.15
HRRR	145.07	234.18	0.90	4.17	275.42	27.54	184.93	18.49
NAM	114.99	227.20	0.75	5.07	254.59	25.46	169.59	16.96
Ensemble	-0.94	173.23	0.18	5.17	173.18	17.32	118.54	11.85
Cell Temperature (T_c)								
Metrics	Mean ($^{\circ}C$)	STD ($^{\circ}C$)	Skewness	Kurtosis	RMSE ($^{\circ}C$)	NRMSE (%)	MAE ($^{\circ}C$)	NMAE (%)
RAP	4.02	6.29	0.55	4.52	7.46	38.17	5.49	28.11
HRRR	6.08	6.46	0.77	3.94	8.87	45.38	6.72	34.39
NAM	3.14	6.26	0.37	4.29	7.00	35.79	5.17	26.46
Ensemble	-0.02	4.76	0.42	4.51	4.76	24.36	3.52	17.98
Wind Speed at 10m (WS_{10})								
Metrics	Mean (m/s)	STD (m/s)	Skewness	Kurtosis	RMSE (m/s)	MAE (m/s)		
RAP	1.60	1.40	-0.27	3.56	2.13	1.82		
HRRR	1.24	1.27	-0.13	4.09	1.78	1.46		
NAM	2.34	1.70	0.15	3.42	2.89	2.47		
Ensemble	-0.01	1.01	-0.98	6.41	1.01	0.73		

TABLE VI. NUMBER OF DAYS WITH ACCURATE CLOUD CONDITIONS FORECASTS

Model	Overcast ($k \leq 0.3$)	Mostly Cloudy ($0.3 < k \leq 0.7$)	Partly Cloudy ($0.7 < k \leq 1$)	Sunny ($k > 1$)	Total # of correct days	% of accuracy
Measurement	37	46	48	33	164	
RAP	19	20	16	27	82	50.00%
HRRR	10	14	15	26	65	39.63%
NAM	18	15	21	23	77	46.95%
Ensemble	24	33	25	23	105	64.02%

B. Systematic Errors in the Conversion Model

Systematic errors of the PV lib model were first quantified based on the measured POA irradiance and measured T_c in scenario A1. The measurement errors were assumed to be negligible due to the limited information, and thus errors obtained in scenario A1 were assumed to be attributed by the PV Lib model. The PV Lib model was found to have a strong tendency to over-predict, as shown in the positive mean in scenario A1 in Table VII. The NRMSE and NMAE were found to be 9.55% and 3.83%, respectively, which were used to subtract from the normalized errors associated with the other 12 scenarios.

C. Sensitivity Analysis for Inputs in the Ensemble Model

In analyzing the errors introduced by individual input, the NRMSE attributed by T_c forecasts (B2) and POA irradiance forecasts (B3) were found to be 0.12 % and 7.44%, respectively, as shown in Table VII. Results illustrated that accurate POA irradiance forecasts were able to improve the power output accuracy in a larger magnitude compared to T_c forecasts. By changing the input from forecast irradiance in scenario B1 to measured irradiance in scenario B2, the NMAE was reduced by 6.35%. As for scenario B3, by inputting measured cell temperature, the NMAE was only reduced by 0.48%, as observed in Fig. 2.

D. Performance Comparison among Models

As shown in Table VII, the power output forecasts yielded by the ensemble model (B1) outperformed the three NWP models (C, D, and E-1). The NRMSE is 6.63% for ensemble forecast in comparison to 14.04% for RAP, 17.14% for HRRR, and 14.88% for NAM. The NRMSE of the ensemble model had an error reduction of 52.83% compared to the best individual NWP model.

The distribution of the power errors of each model is shown in Fig. 3. The positive error tails indicated that all models exhibited an over-forecast tendency. The distribution of errors in the ensemble model was narrower than the other individual NWP models, and had a larger probability with smaller errors. Among the individual NWPs, the power outputs of RAP were the most accurate, followed by the NAM and the HRRR.

E. Sensitivity Analysis on Calculated Cell Temperature and Power Output in Individual NWP Models

This section studied whether calculated cell temperature would yield more accurate power forecasts compared to directly forecasted cell temperature. Calculated cell temperature was based on T_A , WS_{10} , and either POA irradiance (scenario C, D, and E2) or individual solar irradiance components (scenario C, D, and E3). Table VII shows that by changing forecasted cell temperature in C, D, and E1 to calculated cell temperature in C, D, and E2 for all three models, the RMSE increased by at most 14 W and the MAE was increased by at most 4 W, accounting for less than 0.02% of the site's solar capacity. No improvement on the accuracy of solar power output was observed.

By using calculated cell temperature based on individual solar irradiance components in C, D, and E3, the RMSE was decreased for the RAP, but increased for the HRRR and the NAM. In contrary, the NMAE was reduced

by 35 W for the RAP and the HRRR, and 24 W for the NAM, indicating that the overall errors were reduced by approximately 0.05%.

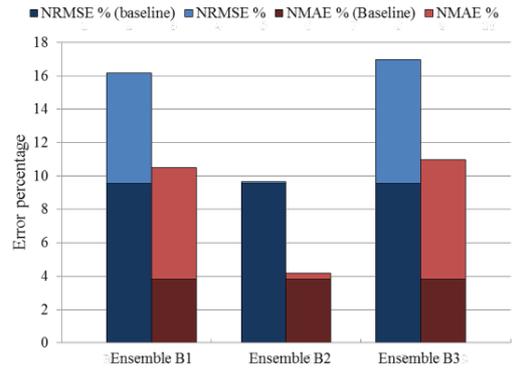


Figure 2. Relative RMSE and MAE percentage for the power outputs in scenarios B1-3 accounting for the systematic errors, which are represented by the darker parts of the bar.

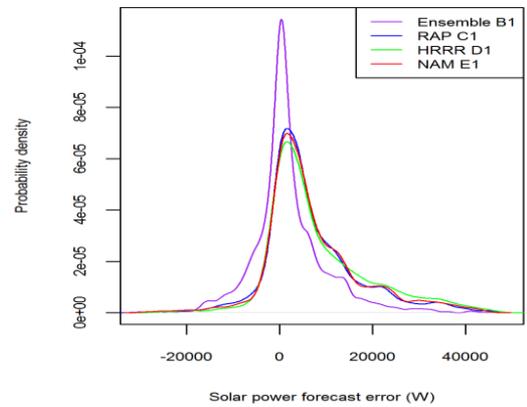


Figure 3. Error distribution of power outputs in scenarios B,C,D, and E1, where all scenarios were based on forecasts POA irradiance and cell temperature.

TABLE VII. STATISTICAL QUANTIFICATION OF POWER ERRORS FOR ALL SCENARIOS

Metrics	Mean (W)	STD (W)	Skewness	Kurtosis	RMSE (W)	NRMSE (%)	MAE (W)	NMAE (%)
Theoretical Power based on measurement								
A1	1840.70	4508.69	6.36	53.12	4868.82	9.55	1950.75	3.83
Ensemble								
B1	2022.55	7997.94	1.00	6.71	3378.78	6.63	3412.48	6.69
B2	1973.32	4519.16	5.93	48.34	61.26	0.12	175.75	0.34
B3	2021.44	8424.81	1.05	6.73	3792.88	7.44	3656.32	7.17
RAP								
C1	6642.53	10033.71	0.98	5.13	7162.13	14.04	6257.44	12.27
C2	6643.67	10046.34	0.99	5.14	7173.29	14.07	6259.45	12.27
C3	6606.64	10055.58	1.00	5.16	7160.62	14.04	6222.86	12.20
HRRR								
D1	8157.81	10896.54	1.03	4.22	8740.73	17.14	7321.67	14.36
D2	8160.12	10912.51	1.03	4.24	8754.90	17.17	7325.06	14.36
D3	8125.76	10924.18	1.04	4.25	8743.70	17.14	7286.20	14.29
NAM								
E1	7042.59	10279.75	0.92	4.80	7589.66	14.88	6584.63	12.91
E2	7043.33	10287.69	0.92	4.81	7596.63	14.90	6585.99	12.91
E3	7019.16	10304.64	0.93	4.82	7596.99	14.90	6560.67	12.86

IV. CONCLUSIONS AND FUTURE WORK

This paper characterized and analyzed errors and uncertainties inherent in forecast parameters generated by the three NWP models and the ensemble model. The sensitivity of power output to different forecast parameters was also quantified. The study was applied to a 51 kW solar plant. Results showed that the ensemble model performed better than the three individual NWP models. Among the three individual NWP models at the studied site, the RAP was able to yield more accurate forecasts in POA irradiance, the HRRR in wind speed, and the NAM in cell temperature.

To analyze the sensitivity of power output to different forecasted solar parameters, a total of 13 scenarios were investigated. Results showed that (i) POA irradiance had a larger influence on the power outputs in comparison to cell temperature; (ii) all four models presented an over-forecast behaviors; and (iii) using the calculated cell temperature instead of directly forecasted cell temperature can slightly increase the overall forecast accuracy of the solar power generation.

Future studies will focus on quantifying uncertainties in forecast parameters for particular seasons or for a longer period of time, as well as for other geographical regions. Furthermore, future sensitivity analyses will attempt to identify an optimal set of forecast parameters that can generate more accurate solar power forecasts.

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