## Math 2415

## Homework on 15.7 and 15.8 (Coordinate systems only)

1. The following points are given in cylindrical coordinates, $(r, \theta, z)$. Express each in rectangular and in spherical coordinates.
(a) $\left(1,45^{\circ}, 1\right)$
(b) $(2, \pi / 2,-4)$
2. The following points are given in rectangular coordinates, $(x, y, z)$. Express each in cylindrical and in spherical coordinates.
(a) $(0,3,4)$
(b) $(\sqrt{2}, 1,1)$
3. Express the plane $z=x$ in (a) cylindrical and (b) spherical coordinates
4. A tank in the shape of a circular cylinder of radius 5 m and height 12 m is half filled with water and lying on its side. Describe the air space inside the tank using a suitably chosen cylindrical coordinate system. Justify your answer with the aid of a sketch.
5. Sketch the surfaces whose equations are given as follows
(a) $r=2$ (cylindrical coordinates)
(b) $r=3 z$ (cylindrical coordinates)
(c) $r^{2}+4 z^{2}=1$ (cylindrical coordinates)
6. Convert the equations to (a) cylindrical and (b) spherical coordinates
(a) $z=x^{2}+y^{2}$
(b) $x^{2}+y^{2}-3 z^{2}=0$
(c) $x^{2}+y^{2}=4$
7. Sketch the solid described by the following inequalities
(a) $0 \leq \rho \leq 4, \pi / 2 \leq \phi \leq \pi, 0 \leq \theta \leq \pi / 4$
(b) $r \leq z \leq 1-r^{2}$. Hint: First sketch the curves $z=r$ and $z=1-r^{2}$ in $(r, z)$-space.
