

**Math 2415**  
**Paper Homework #13**

**1. 16.2, Line Integrals:**

- (a) Evaluate  $\int_C f \, ds$  where  $C$  has parametrization  $\mathbf{r}$  with  $\mathbf{r}(t) = (t, t^2, 1)$  for  $0 \leq t \leq 2$  and  $f(x, y, z) = x$ .
- (b) Evaluate  $\int_C yz \, dy + xy \, dz$  where  $C$  is the curve given by  $x = \sqrt{t}$ ,  $y = t$ ,  $z = t^2$  for  $1 \leq t \leq 2$ .

**2. 16.3, Conservative Vectors and FTC for Line Integrals:** Consider the vector field

$$\mathbf{F}(x, y) = (1 - ye^{-x})\mathbf{i} + e^{-x}\mathbf{j}.$$

- (a) Show that  $\mathbf{F}$  is a conservative vector field.
  - (b) Find a function  $f$  so that  $\mathbf{F} = \nabla f$ .
  - (c) Calculate  $\int_C \mathbf{F} \cdot d\mathbf{r}$ , where  $C$  is the curve  $\mathbf{r}(t) = e^t\mathbf{i} + \sin t\mathbf{j}$ , for  $0 \leq t \leq \pi/2$ .
- 3. 16.4, Green's Theorem:** Use Green's Theorem to calculate  $\int_C \mathbf{F} \cdot d\mathbf{r}$ , where  $\mathbf{F}(x, y) = (6y + x)\mathbf{i} + (y + 2x)\mathbf{j}$  and  $C$  is the circle  $(x - 2)^2 + (y - 3)^2 = 4$  traversed clockwise.