## Math 2415

## Paper Homework #6

## 1. 14.3, Partial Derivatives:

- (a) First Derivatives:
  - The plane y = 2 intersects the graph of  $z = f(x, y) = xy^3 + 5x^2$  in a curve, *C*.
  - i. Calculate  $\frac{\partial f}{\partial x}$  at (x, y) = (3, 2).
  - ii. Find a parametrization of the tangent line to the curve C at the point where x = 3.
- (b) Mixed Partials: In this multiple choice problem provide a justification for your answer.

In the contour plot below dark shades represent small values of the function and light shades represent large values of the function. What is the sign of the mixed partial derivative?



- (c) 2nd Derivatives: Verify that the following functions solve the wave equation, u<sub>tt</sub> = u<sub>xx</sub>.
  i. u(x, t) = cos(4x) cos(4t)
  - ii. u(x, t) = f(x t) + f(x + t), where f is any differentiable function of one variable.

## 2. 14.4, Tangent Planes and Linear Approximation:

- (a) Let  $f(x, y) = x^2 y^2 x$ .
  - i. Find the equation for the tangent plane to the graph of f at (2, 1, 2).
  - ii. Use a linear approximation to find the approximate value of f(1.9, 1.1).

(b) In this multiple choice problem provide a justification for your answer.

Suppose  $f_x(3,4) = 5$ ,  $f_y(3,4) = -2$ , and f(3,4) = 6. Assuming the function is differentiable, what is the best estimate for f(3.1,3.9) using this information?

- (a) 6.3
- (b) 9
- (c) 6
- (d) 6.7