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# Message Authentication Codes

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Based on [Prof. Ninghui Li's](#) Slides

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## Lecture Outline

- Message Authentication Code





## Limitation of Using Hash Functions for Authentication

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- Require an authentic channel to transmit the hash of a message
  - anyone can compute the hash value of a message, as the hash function is public
  - not always possible
- How to address this?
  - use more than one hash functions
  - use a key to select which one to use



## Hash Family

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- A hash family is a four-tuple  $(X, Y, K, H)$ , where
  - $X$  is a set of possible messages
  - $Y$  is a finite set of possible message digests
  - $K$  is the keyspace
  - For each  $K \in K$ , there is a hash function  $h_K \in H$ .  
Each  $h_K: X \rightarrow Y$
- Alternatively, one can think of  $H$  as a function  $K \times X \rightarrow Y$



## Message Authentication Code

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- A MAC scheme is a hash family, used for message authentication
- $MAC = C_K(M)$
- The sender and the receiver share  $K$
- The sender sends  $(M, C_K(M))$
- The receiver receives  $(X, Y)$  and verifies that  $C_K(X)=Y$ , if so, then accepts the message as from the sender
- To be secure, an adversary shouldn't be able to come up with  $(X, Y)$  such that  $C_K(X)=Y$ .

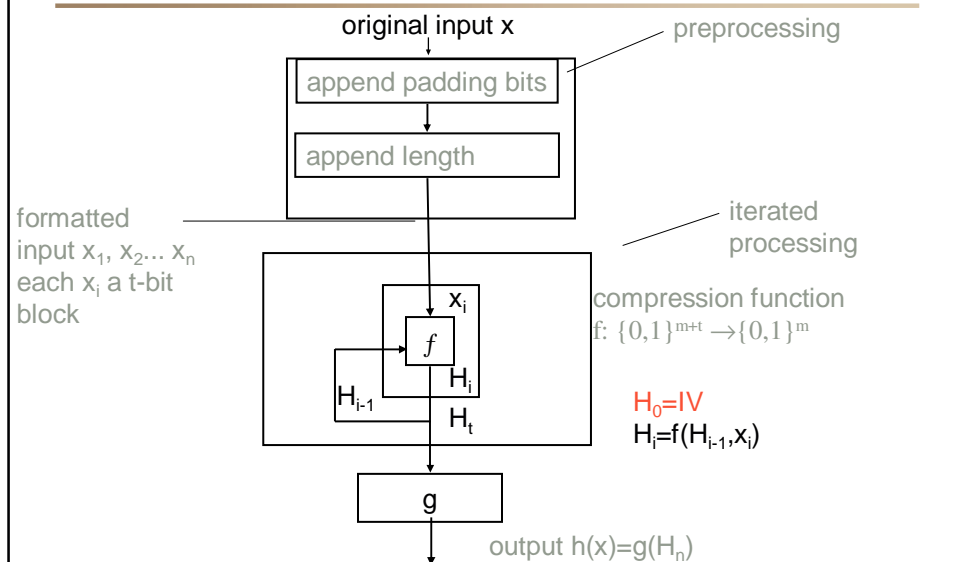


## Constructing MAC from Hash Functions

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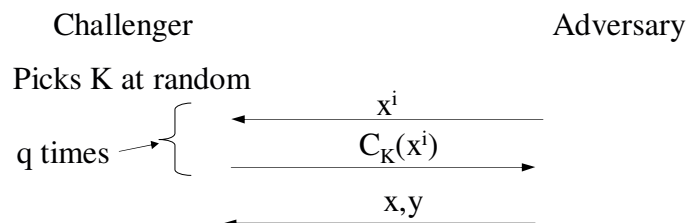
- Given a cryptographic (iterative) hash function  $h$ ,
- Define  $C_K(M)$  to be  $h(M)$  with  $K$  as IV
- Is this secure?
- Given a message  $x$  and its MAC  $C_K(x)$ , the adversary can construct  $x'$  and  $C_K(x')$ 
  - let  $pad(x)$  be the padding added to  $x$
  - let  $x'=x \parallel pad(x) \parallel w$ ,  $y'=x' \parallel pad(x')$
  - then  $C_K(x')$  can be computed from  $C_K(x)$

## Model for Iterated Hash Functions



## Existential Forgery Attack against MAC

- Let  $C$  be a MAC function  $C_K(M)$  is the MAC for  $M$  under  $K$ .

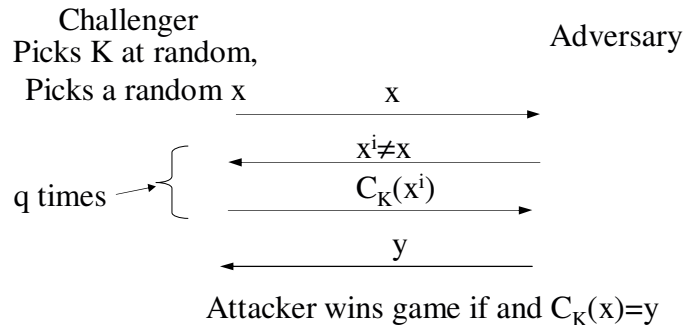


Attacker wins game if  $x \notin \{x^1, \dots, x^q\}$   
and  $C_K(x) = y$

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## Selective Forgery Attack Against MAC

- Let  $C$  be a MAC function  $C_K(M)$  is the MAC for  $M$  under  $K$ .



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## MAC Security

- The pair  $(x, z)$  is called a forgery
- A  $(\epsilon, q)$  forger
  - can produce a forgery with probability  $\epsilon$ , after making  $q$  queries
  - generally talks about existential forgery
- The attacker against the MAC scheme  $C_K(M) = h(M)$  with  $K$  as IV is a  $(1, 1)$  forger



## Constructing MAC using Hash Functions

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- Are the following MAC schemes secure? What kind of forgers exist for them?
  - $C_K(M) = h(K || M)$ , where  $h$  is a cryptographic hash function



## HMAC Goals

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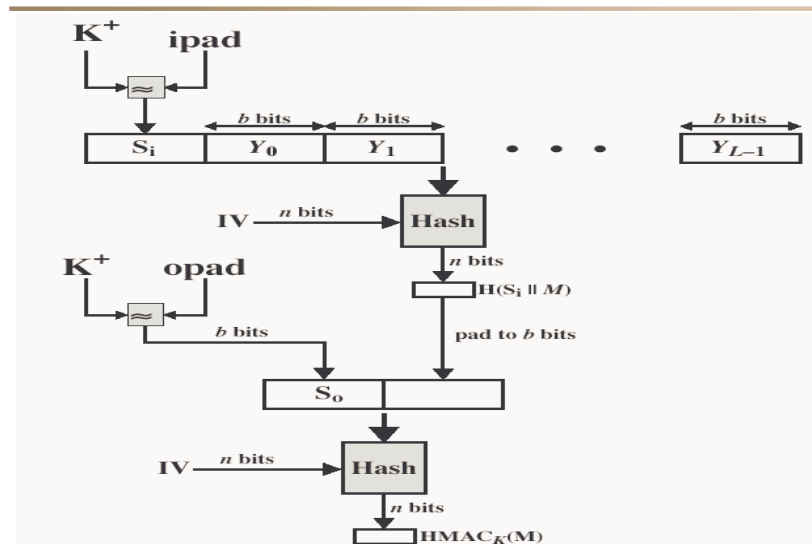
- Use **available** hash functions without modification.
- Preserve the original performance of the **hash function** without incurring a significant degradation.
- Use and handle keys in a **simple** way.
- Allow **easy replacement** of the underlying hash function in the event that faster or more secure hash functions are later available.
- Have a well-understood cryptographic analysis of the strength of the authentication mechanism based on **reasonable assumptions** on the underlying hash function.

# HMAC

$$\text{HMAC}_K = \text{Hash}[(K^+ \oplus \text{opad}) \parallel \text{Hash}[(K^+ \oplus \text{ipad}) \parallel M]]$$

- $K^+$  is the key padded out to input block size of the hash function and opad, ipad are specified padding constants
- Key size:  $L/2 < K < L$
- MAC size: at least  $L/2$ , where  $L$  is the hash output

## HMAC Overview



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## HMAC Security

- Security of HMAC relates to that of the **underlying** hash algorithm
- If used with a secure hash functions (s.t. SHA1) and according to the specification (key size, and use correct output), **not known practical attacks** against HMAC
- In general, HMAC be attacked as follows:
  - **brute force** on the key space
  - attacks on the **hash function itself**
    - birthday attack, although the use of key makes this attack more difficult
    - attacks against the compression function

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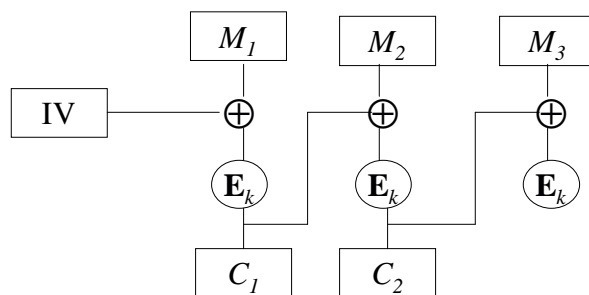
## CBC-MAC

- Given a block cipher **E** with block size  $m$
- Given message  $M = M_1 || M_2 || \dots || M_n$
- MAC of  $M$  is  $\mathbf{E}_k(M)$ 
  - $z_0 = IV = 0^m$
  - $z_i = \mathbf{E}_k(z_{i-1} \oplus M_i)$  for  $1 \leq i \leq n$
  - $MAC = z_n$
- Random IV is needed in CBC encryption to prevent codebook attack on first block, not needed here.



## Encryption Modes: CBC

- **Cipher Block Chaining (CBC)**: next input depends of previous output
  - Plaintext is  $M_1, M_2, M_3, M_4$ ,
  - Ciphertext is:  $C_1 = IV \oplus E_k(M_1)$   $C_2 = C_1 \oplus E_k(M_2)$   
 $C_3 = C_2 \oplus E_k(M_3)$   $C_4 = C_3 \oplus E_k(M_4)$



## Security of CBC-MAC

- Secure for messages of a fixed number of blocks assuming the block cipher is PRP
- Not secure with variable lengths, example attack
  - given three pairs of messages/MACs  $(x_1, y_1)$   $(x_2, y_2)$ ,  $(x_1 || z, y_3)$ , then
    - $y_1 = E_k[IV \oplus x_1]$
    - $y_2 = E_k[IV \oplus x_2]$
    - $y_3 = E_k[y_1 \oplus z] = E_k[y_2 \oplus (z \oplus y_1 \oplus y_2)]$
    - let  $z' = (z \oplus y_1 \oplus y_2)$ ,  $(x_2 || z', y_3)$  is also a valid pair



## Optional Security Enhancement for CBC-MAC

- MAC of M is
  - $z_0 = IV = 0^m$
  - $z_i = E_{K1}(z_{i-1} \oplus M_i)$  for  $1 \leq i \leq n$
  - $MAC = E_{K1} D_{K2}[z_n]$
- Reduces threat of exhaustive key search
- Defends against the previous attack



## Data Integrity Combined with Encryption

- Encryption alone does not guarantee data integrity
- Combining encryption with hash
  - $C = E_K[x \parallel h(x)]$
  - breaking encryption also compromises integrity
  - may be vulnerable to known-plaintext attack

## MAC with Encryption

- $C = E_k[x \parallel h_k(x)]$ 
  - separate keys used for encryption & for MAC
  - the algorithms E and h should be independent
  - precludes exhaustive key search on MAC key
- Alternative 1:  $C = E_k[x], h_k(E_k[x])$ 
  - allows message authentication without knowing x or K
  - authenticates only the ciphertext
- Alternative 2:  $E_k[x], h_k(x)$ 
  - requires  $h_k(x)$  does not leak information about x

## CCM Mode

- CCM mode is a NIST standard that provides an authenticated encryption
- MAC is produced as a part of the encryption process
- CCM mode uses CTR mode for encryption and CBC-MAC for authentication
  - Given message  $M = M_1 \parallel M_2 \parallel \dots \parallel M_n$
  - $C_i = M_i \oplus E_k(ctr+i \text{ mod } 2^m)$
  - $temp = \text{CBC-Mac}(M, k)$  and  $C' = temp \oplus E_k(ctr)$
  - Return  $C_1 \parallel \dots \parallel C_n \parallel C'$



## Next Lectures..

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- Number theory
- Readings:
  - Stingson: 5.1, 5.2, 5.4