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## Modes of Operation

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## Block Ciphers

- Block length is fixed ( $n$ -bit)
- How to encrypt large messages?
  - Partition into  $n$ -bit blocks
  - Choose mode of operation
    - Electronic Codebook (ECB),
    - Cipher-Block Chaining (CBC),
    - Cipher Feedback (CFB),
    - Output Feedback (OFB),
    - Counter (CTR)
- Padding schemes

## Evaluation criteria

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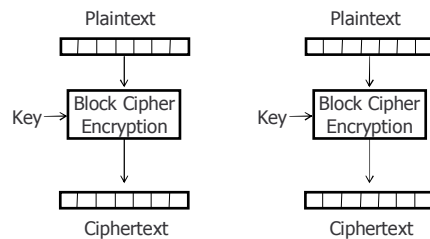
- Identical messages
  - under which conditions ciphertext of two identical messages are the same
- Chaining dependencies
  - how adjacent plaintext blocks affect encryption of a plaintext block
- Error propagation
  - resistance to channel noise
- Efficiency
  - preprocessing
  - parallelization: random access

## Notation

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- Message  $x$  consists of plaintext blocks of size  $n$ 
  - $x = x_1 || x_2 || \dots || x_t$
- Ciphertext of plaintext block  $x_i$  denoted as  $c_i$
- Chaining requires an initialization vector that first plaintext block  $x_1$  will depend on. Initialization vector denoted as  $IV$ .
  - $IV$  should be selected randomly for each message ( $x$ )

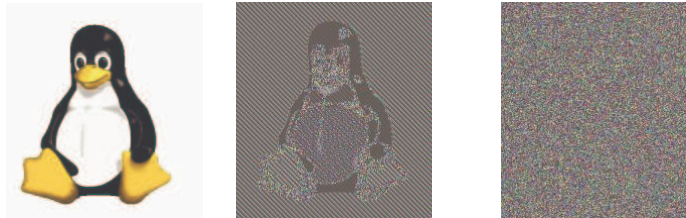
## Electronic Codebook (ECB)



- Each block encrypted independently
- Identical plaintexts encrypted similarly
- No chaining, no error propagation

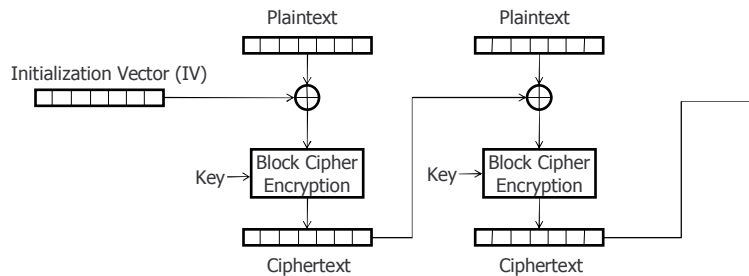
## Electronic Codebook (ECB)

- Does not hide data patterns, unsuitable for long messages
  - Wiki example: pixel map using ECB



- Susceptible to replay attacks
  - Example: a wired transfer transaction can be replayed by re-sending the original message)

## Cipher-Block Chaining (CBC)

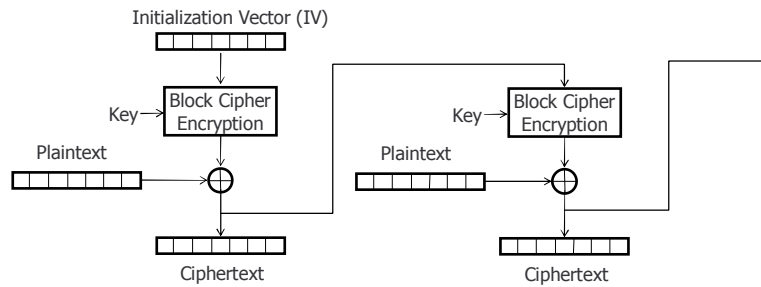


- Allows random access to ciphertext
- Decryption is parallelizable
  - Plaintext block  $x_j$  requires ciphertext blocks  $c_j$  and  $c_{j-1}$

## Cipher-Block Chaining (CBC)

- Identical messages: changing IV or the first plaintext block results in different ciphertext
- Chaining: Ciphertext block  $c_j$  depends on  $x_j$  and all preceding plaintext blocks (dependency contained in  $c_{j-1}$ )
- Error propagation: Single bit error on  $c_j$  may flip the corresponding bit on  $x_{j+1}$ , but changes  $x_j$  significantly.
- IV need not be secret, but its integrity should be protected

## Cipher Feedback (CFB)

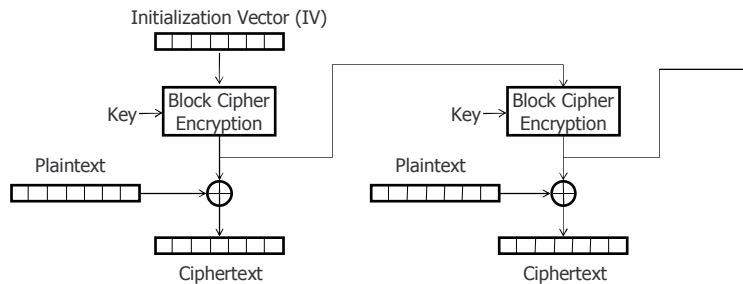


- Allows random access to ciphertext
- Decryption is parallelizable
  - Plaintext block  $x_j$  requires ciphertext blocks  $c_j$  and  $c_{j-1}$

## Cipher Feedback (CFB)

- Identical messages: as in CBC
- Chaining: Similar to CBC
- Error propagation: Single bit error on  $c_j$  may flip the corresponding bit on  $x_j$ , but changes  $x_{j+1}$  significantly.
- IV need not be secret (XORed with  $x_1$ )

## Output Feedback (OFB)

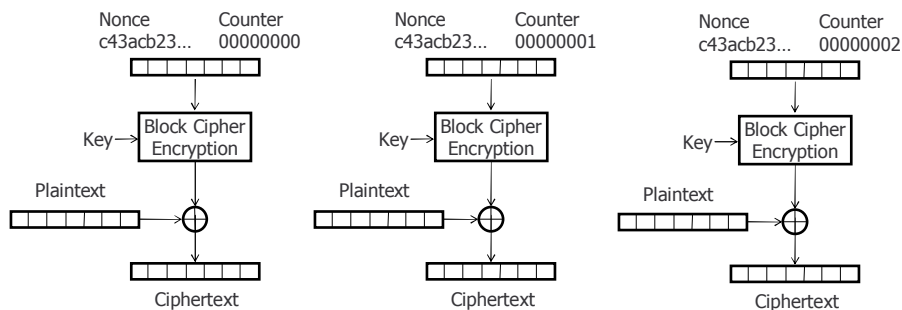


- Preprocessing possible (keep enc/decrypting previous output block)
- No random access, not parallelizable

## Output Feedback (OFB)

- Identical messages: same as CBC
- No chaining dependencies
- Error propagation: Single bit error on  $c_j$  may only affect the corresponding bit of  $x_j$
- IV need not be secret, but should be changed if a previously used key is to be used again

## Counter (CTR)



- Preprocessing possible (inc/decrement and enc/decrypt counter)
- Allows random access

## Counter (CTR)

- Both encryption & decryption are parallelizable
  - Encrypted counter is sufficient to enc/decrypt
- Identical messages: changing nonce results in different ciphertext
- No chaining dependencies
- No error propagation
- Nonce should be random, and should be changed if a previously used key is to be used again

## Summary

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- Choice of encryption mode affects
  - Encryption/decryption speed
  - Security against active adversaries (bit flips)
  - Security against passive adversaries (ECB)
  - Error propagation