## Chapter 19: Chemical Kinetics

Key topics:
Reaction Rates
Factors That Affect Reaction Rates
Reaction Mechanisms

How fast does a reaction occur?
e.g., many famous painting are changing color...


## Collision Theory of Chemical Reactions

A very simple picture of a chemical reaction between two molecules is that

1. They must collide with enough energy to react
2. They must collide in the correct orientation to react

The collision (kinetic energy) can be transferred into vibrational energy, which can lead to bond breaking. This is the first step in a chemical reaction.

The minimum energy required to initiate a reaction is called the activation energy, $\mathrm{E}_{\mathrm{a}}$. If the collision is $<\mathrm{E}_{\mathrm{a}}$, it is ineffective and the reactants simply bounce off each other. Temperature has a large effect on having energy > $\mathrm{E}_{\mathrm{a}}$.


The correct orientation is also needed for an effective reaction:


Transition state theory (TST), also known as Activated Complex Theory, is a more sophisticated theory that has two main assumptions

1) The transition state is in equilibrium with the reactions.
2) One (special) vibrational motion results in the breakup of the transition state into the products.


## Measuring Reaction Progress \& Expressing Reaction Rate

We can express the reaction rate as either:

- Rate of disappearance of reactants (decrease or -ie)
- Rate of appearance of products (increase or +ie)


Reaction progress with time. The rate changes over time.
We can follow a color change, conductance change, pressure change, or whatever is convenient.
Consider the reaction $\mathrm{A} \rightarrow \mathrm{B}$.
average rate $=-\frac{\Delta[A]}{\Delta t}=\frac{\Delta[B]}{\Delta t}$
$\mathrm{Br}_{2}(a q)+\mathrm{HCOOH}(a q) \rightarrow 2 \mathrm{Br}^{-}(a q)+2 \mathrm{H}^{+}(a q)+\mathrm{CO}_{2}(g)$ (colored)


Reaction progress can be monitored using a spectrometer.
average rate $=-\frac{\Delta\left[\mathrm{Br}_{2}\right]}{\Delta t}=-\frac{\left[\mathrm{Br}_{2}\right]_{\text {final }}-\left[\mathrm{Br}_{2}\right]_{\text {initial }}}{t_{\text {final }}-t_{\text {initial }}}$
The average rate decreases over time (see Table 19.1).
The instantaneous rate is given by the tangent line:


From Table 19.1:

| Time (s) | $\left[\mathrm{Br}_{2}\right]$ | Rate (M/s) |
| :---: | :---: | :---: |
| 50 | 0.0101 | $3.52 \times 10^{-5}$ |
| 250 | 0.00500 | $1.75 \times 10^{-5}$ |

We can see that when $\left[\mathrm{Br}_{2}\right]$ is halved, the rate is halved. Therefore rate $\propto\left[\mathrm{Br}_{2}\right]$, or rate $=k\left[\mathrm{Br}_{2}\right]$ where $k$ is the proportionality constant.
$k=$ rate constant (does depend on the temperature)

Value of $k$ ? $k=$ rate $/\left[\mathrm{Br}_{2}\right]$

$$
\text { at } t=50 \mathrm{~s}, \quad k=\frac{3.52 \times 10^{-5} \mathrm{Ms}^{-1}}{0.0101 \mathrm{M}}=3.49 \times 10^{-3} \mathrm{~s}^{-1}
$$

at $t=250 \mathrm{~s}, \quad k=\frac{1.75 \times 10^{-5} \mathrm{Ms}^{-1}}{0.00500 \mathrm{M}}=3.50 \times 10^{-3} \mathrm{~s}^{-1}$
(same within experimental error)
Consider the reaction $\mathrm{A} \rightarrow 2 \mathrm{~B}$.
rate $=-\frac{\Delta[A]}{\Delta t}=\frac{1}{2} \frac{\Delta[B]}{\Delta t}$
In general for the reaction $a A+b B \rightarrow c C+d D$
rate $=-\frac{1}{a} \frac{\Delta[A]}{\Delta t}=-\frac{1}{b} \frac{\Delta[B]}{\Delta t}=\frac{1}{c} \frac{\Delta[C]}{\Delta t}=\frac{1}{d} \frac{\Delta[D]}{\Delta t}$
e.g., Write the balanced equation corresponding to the following rate expression
rate $=-\frac{1}{2} \frac{\Delta\left[\mathrm{~N}_{2} \mathrm{O}_{5}\right]}{\Delta t}=\frac{1}{2} \frac{\Delta\left[\mathrm{~N}_{2}\right]}{\Delta t}=\frac{1}{5} \frac{\Delta\left[\mathrm{O}_{2}\right]}{\Delta t}$
Solution:
-ve sign indicates reactants and +ve sign indicates products.
So this reaction should be: $2 \mathrm{~N}_{2} \mathrm{O}_{5} \rightarrow 2 \mathrm{~N}_{2}+5 \mathrm{O}_{2}$ We should double check that the reaction is balanced.
e.g., Consider the following unbalanced equation: $A+B \rightarrow C$. When $C$ is being formed at the rate of $0.086 \mathrm{M} / \mathrm{s}, A$ is being consumed at a rate of $0.172 \mathrm{M} / \mathrm{s}$, and $B$ at $0.258 \mathrm{M} / \mathrm{s}$. Balance the equation from this information.

Solution:
We are told that $\frac{\Delta[\mathrm{C}]}{\Delta t}=0.086, \quad \frac{\Delta[\mathrm{~A}]}{\Delta t}=-0.172, \quad \frac{\Delta[\mathrm{~B}]}{\Delta t}=-0.258$ If we write the balanced equation $a \mathrm{~A}+b \mathrm{~B} \rightarrow \mathrm{cC}$, we know that
$-\frac{1}{a} \frac{\Delta[\mathrm{~A}]}{\Delta t}=-\frac{1}{b} \frac{\Delta[\mathrm{~B}]}{\Delta t}=\frac{1}{c} \frac{\Delta[\mathrm{C}]}{\Delta t} \quad$ or $\quad \frac{0.172}{a}=\frac{0.258}{b}=\frac{0.086}{c}$
If we divide each expression by 0.086 we get
$\frac{2}{a}=\frac{3}{b}=\frac{1}{c} \quad$ Therefore $a=2, b=3$, and $c=1$.
Dependence of Reaction Rate on Reactant Concentration
In the bromine reaction we considered earlier,
$\mathrm{Br}_{2}(a q)+\mathrm{HCOOH}(a q) \rightarrow 2 \mathrm{Br}^{-}(a q)+2 \mathrm{H}^{+}(a q)+\mathrm{CO}_{2}(g)$ we determined the rate $=k\left[\mathrm{Br}_{2}\right]$.

In terms of the reactant concentrations, we write rate $=k\left[\mathrm{Br}_{2}\right]^{x}+[\mathrm{HCOOH}]^{y}$
with $x=1$ and $y=0$. The exponents ( $x$ and $y$ ) are empirically determined. Without experimental data we can't simply predict their values.

In general, for $a A+b B \rightarrow c C+d D$, the rate law is rate $=k[\mathrm{~A}]^{x}[\mathrm{~B}]^{y}$.
$>x=0$ : the reaction is $0^{\text {th }}$ order with respect to $A$.
$>x=1$ : the reaction is $1^{\text {st }}$ order with respect to $A$.
$>x=2$ : the reaction is $2^{\text {nd }}$ order with respect to $A$.
The overall reaction order is the sum of the exponents, so the bromine reaction is $1^{\text {st }}$ order overall $(1+0=1)$.

To determine the rate law, we often analyze initial rate data from experiments. (The initial rate is the instantaneous rate at the beginning of the reaction.)

For the reaction $\mathrm{F}_{2}(g)+2 \mathrm{ClO}_{2}(g) \rightarrow 2 \mathrm{FClO}_{2}(g)$ we have the following experimental data:

| TABLE 19.2 | Initial Rate Data for the Reaction Between $\mathrm{F}_{2}$ and $\mathrm{ClO}_{2}$ |  |  |
| :---: | :---: | :---: | :---: |
| Experiment | $\left[\mathbf{F}_{2}\right](\boldsymbol{M})$ | $\left[\mathbf{C l O}_{2}\right](\boldsymbol{M})$ | Initial rate $(\mathbf{M} / \mathbf{s})$ |
| 1 | 0.10 | 0.010 | $1.2 \times 10^{-3}$ |
| 2 | 0.10 | 0.040 | $4.8 \times 10^{-3}$ |
| 3 | 0.20 | 0.010 | $2.4 \times 10^{-3}$ |

We know the rate law must be rate $=k\left[\mathrm{~F}_{2}\right]^{x}\left[\mathrm{ClO}_{2}\right]^{y}$. Comparing exp. 1 and 3 ,

$$
\begin{aligned}
\frac{\text { rate }_{3}}{\text { rate }_{1}}=\frac{k\left[\mathrm{~F}_{2}\right]^{x}\left[\mathrm{ClO}_{2}\right]^{y}}{k\left[\mathrm{~F}_{2}\right]^{x}\left[\mathrm{ClO}_{2}\right]^{y}} & =\frac{2.4 \times 10^{-3} \mathrm{Ms}^{-1}}{1.2 \times 10^{-3} \mathrm{Ms}^{-1}}=\frac{k[0.20]^{x}[0.010]^{y}}{k[0.10]^{x}[0.010]^{y}} \\
& \Rightarrow 2=2^{x} \Rightarrow x=1
\end{aligned}
$$

Comparing exp. 1 and 2,

$$
\begin{aligned}
& \frac{\text { rate }_{2}}{\text { rate }_{1}}=\frac{k\left[\mathrm{~F}_{2}\right]^{x}\left[\mathrm{ClO}_{2}\right]^{y}}{k\left[\mathrm{~F}_{2}\right]^{x}\left[\mathrm{ClO}_{2}\right]^{y}}=\frac{4.8 \times 10^{-3} \mathrm{Ms}^{-1}}{1.2 \times 10^{-3} \mathrm{Ms}^{-1}}=\frac{k[0.10]^{x}[0.040]^{y}}{k[0.10]^{x}[0.010]^{y}} \\
& \Rightarrow 4=4^{y} \Rightarrow y=1
\end{aligned}
$$

Therefore we have

$$
\text { rate }=k\left[\mathrm{~F}_{2}\right]^{1}\left[\mathrm{ClO}_{2}\right]^{1} \quad\left(2^{\text {nd }} \text { order overall }\right)
$$

Then we can determine $k$ from any single exp.
$k=\frac{\text { rate }}{\left[\mathrm{F}_{2}\right]\left[\mathrm{ClO}_{2}\right]}=\frac{2.4 \times 10^{-3} \mathrm{Ms}^{-1}}{[0.20 \mathrm{M}][0.010 \mathrm{M}]}=1.2 \mathrm{M}^{-1} \mathrm{~s}^{-1}$
The rate has units of $\mathrm{M} \mathrm{s}^{-1}$, so $k$ has units as follows:


## Units of the Rate Constant $k$ for Reactions of Various Overall Orders

Overall reaction order
0
1

2

3*

$$
\begin{array}{cc}
\text { Sample rate law } & \text { Units of } k \\
\text { rate }=k & M \cdot \mathrm{~s}^{-1} \\
\text { rate }=k[\mathrm{~A}] \text { or rate }=k[\mathrm{~B}] & \mathrm{s}^{-1} \\
\text { rate }=k[\mathrm{~A}]^{2}, \text { rate }=k[\mathrm{~B}]^{2}, \text { or } \\
\text { rate }=k[\mathrm{~A}][\mathrm{B}]
\end{array} \quad M^{-1} \cdot \mathrm{~s}^{-1} .
$$

Units of $k$
*Another possibility for a third-order reaction is rate $=k[\mathrm{~A}][\mathrm{B}][\mathrm{C}]$, although such reactions are very rare.

Note:
$>$ rate law defined in terms of reactants only
> exponents are usually positive whole numbers or zero

- can be negative (inhibitor)
- can be a fraction (won't see in this course)
e.g., For the reaction $\mathrm{A}+\mathrm{B} \rightarrow 2 \mathrm{C}$, the rate $=k[\mathrm{~A}]^{2}$ with $k=1.3$ $\times 10^{-2} \mathrm{M}^{-1} \mathrm{~s}^{-1}$. Fill in the missing table entries:

| Experiment | $[\mathrm{A}](M)$ | $[\mathrm{B}](M)$ | Initial rate $(\mathrm{M} / \mathrm{s})$ |
| :--- | :--- | :--- | :--- |
| 1 | 0.013 | 0.250 | $2.20 \times 10^{-6}$ |
| 2 | 0.026 | 0.250 |  |
| 3 |  | 0.500 | $2.20 \times 10^{-6}$ |

Solution:
Blue entry: the rate is the same as exp. 1, so [A] must be the same as exp. 1 since this is what the rate depends on.

Green entry: since [A] doubles from exp. 1, the rate must be $2^{2}$ $=4$ times the rate of exp. $1=8.80 \times 10^{-6}$.

## Dependence of Reaction Concentration on Time

How do the reactant (and product) concentrations change with time? Analyze this in terms of the overall reaction order.

## First Order Reactions

A first order reaction depends on the concentration of one of the reactants raised to the first power. We will write such a reaction as $\mathrm{aA} \rightarrow$ products.
rate $=-\frac{1}{a} \frac{\Delta[\mathrm{~A}]}{\Delta t}=k[\mathrm{~A}] \Rightarrow-\frac{\Delta[\mathrm{A}]}{\Delta t}=(a k)[\mathrm{A}]=k^{*}[\mathrm{~A}]$
where we have redefined the rate constant to include the stoichiometric coefficient. Now we change $\Delta$ to $d$ (finite change to infinitesimal change) and just write $k$ for $k^{*}$
$-\frac{d[\mathrm{~A}]}{d t}=k[\mathrm{~A}] \Rightarrow \frac{d[\mathrm{~A}]}{[\mathrm{A}]}=-k d t$ or $\frac{1}{[\mathrm{~A}]} d[\mathrm{~A}]=-k d t$
and integrate from $t=0$ to $t=t$
$\int_{[\mathrm{A}]_{0}}^{[\mathrm{A}]_{t}} \frac{1}{[\mathrm{~A}]} d[\mathrm{~A}]=-k \int_{0}^{t} d t$
which gives the first order integrated rate law
$\ln [\mathrm{A}]_{t}-\ln [\mathrm{A}]_{0}=-k t$ or $\ln \frac{[\mathrm{A}]_{t}}{[\mathrm{~A}]_{0}}=-k t$ or $[\mathrm{A}]_{t}=[\mathrm{A}]_{0} e^{-k t}$
e.g., For $2 A \rightarrow B, k=7.5 \times 10^{-3} \mathrm{~s}^{-1}$.

With $[A]_{0}=2.25 \mathrm{M}$, find $[\mathrm{A}]$ after 2 minutes.
Solution:
2 minutes $=120 \mathrm{~s}$, so
$[\mathrm{A}]_{t}=[\mathrm{A}]_{0} e^{-k t}=(2.25 M) e^{-0.9}=0.91 M$

From concentration vs. time data (e.g. Lab 17 in Chem 1112) we would do the following:


First order kinetics; we obtain a straight line when the data is plotted on a logarithmic scale.

Half-life: The half-life of a reaction $\left(\mathrm{t}_{1 / 2}\right)$ is the time required for the reactant concentration to drop to half of its original value. We express this as

$$
[\mathrm{A}]_{t}=[\mathrm{A}]_{t_{1 / 2}}=\frac{[\mathrm{A}]_{0}}{2} \Rightarrow \frac{[\mathrm{~A}]_{t_{1 / 2}}}{[\mathrm{~A}]_{0}}=\frac{1}{2}
$$

Then the integrated rate law gives
$\ln \frac{[\mathrm{A}]_{t_{1 / 2}}}{[\mathrm{~A}]_{0}}=\ln \frac{1}{2}=-k t_{1 / 2}$

$$
\ln \frac{1}{2}=-\ln 2 \approx-0.693 \text { so that } t_{1 / 2}=\frac{0.693}{k}
$$



First order kinetics; the concentration is halved every half-life. (from chemwiki.ucdavis.edu)
e.g., Calculate the rate constant for the first order decay of ${ }^{24} \mathrm{Na}$ ( $\mathrm{t}_{1 / 2}=14.96$ hours).

Solution:
$14.96 \mathrm{~h}=\frac{0.693}{k} \Rightarrow k=\frac{0.693}{14.96 \mathrm{~h}}=4.63 \times 10^{-2} \mathrm{~h}^{-1} \quad\left(\times \frac{24 \mathrm{~h}}{1 \text { day }}=1.11 \mathrm{day}^{-1}\right)$
e.g., The decomposition of $\mathrm{H}_{2} \mathrm{O}_{2}$ is first order:
$\mathrm{H}_{2} \mathrm{O}_{2} \rightarrow \mathrm{H}_{2} \mathrm{O}+1 / 2 \mathrm{O}_{2}$ with $k=7.00 \times 10^{-4} \mathrm{~s}^{-1}$ and $\left[\mathrm{H}_{2} \mathrm{O}_{2}\right]_{0}=$ 0.100 M . How long will it take for $\left[\mathrm{H}_{2} \mathrm{O}_{2}\right]=0.0370 \mathrm{M}$ ?

## Solution:

$\ln \frac{[\mathrm{A}]_{t}}{[\mathrm{~A}]_{0}}=-k t \Rightarrow t=-\frac{1}{k} \ln \frac{[\mathrm{~A}]_{t}}{[\mathrm{~A}]_{0}}=-\frac{1}{7 \times 10^{-4} \mathrm{~s}^{-1}} \ln \frac{0.0370 M}{0.100 M}$
$=1420 \mathrm{~s}=23.7 \mathrm{~min}$.

## Second Order Reactions

For $A+B \rightarrow C$,
A second order reaction looks like either

1) rate $=k[A]^{2}$
2) rate $=k[\mathrm{~A}][\mathrm{B}]$

We will only consider case 1 ).
Similar to the first order case, we redefine the rate constant to include the stoichiometric coefficient. We write
rate $=-\frac{\Delta[\mathrm{A}]}{\Delta t}=k[\mathrm{~A}]^{2}$
Now we change $\Delta$ to $d$ (finite
change to infinitesimal change):
$-\frac{d[\mathrm{~A}]}{d t}=k[\mathrm{~A}]^{2} \Rightarrow \frac{1}{[\mathrm{~A}]^{2}} d[\mathrm{~A}]=-k d t$
Then we integrate from $t=0$ to $t=t$
$\int_{[\mathrm{A}]_{0}}^{[\mathrm{A}]_{t}} \frac{1}{[\mathrm{~A}]^{2}} d[\mathrm{~A}]=-k \int_{0}^{t} d t \Rightarrow-\frac{1}{[\mathrm{~A}]_{t}}+\frac{1}{[\mathrm{~A}]_{0}}=-k t$
and rearrange
$\frac{1}{[\mathrm{~A}]_{t}}=k t+\frac{1}{[\mathrm{~A}]_{0}}$


Second order kinetics: a plot of $1 /[\mathrm{A}]$ vs. time has slope $k$ and intercept 1/[A] ${ }_{0}$

To compute the half-life, we use $\left.{ }^{[\mathrm{A}}\right]_{t}=[\mathrm{A}]_{t_{1 / 2}}=[\mathrm{A}]_{0} / 2$

$$
\frac{1}{[\mathrm{~A}]_{0} / 2}=k t_{1 / 2}+\frac{1}{[\mathrm{~A}]_{0}} \Rightarrow t_{1 / 2}=\frac{1}{k[\mathrm{~A}]_{0}}
$$

e.g., The reaction $2 \mathrm{~A} \rightarrow \mathrm{~B}$ is second order in A with $k=32 \mathrm{M}^{-1}$ $\mathrm{s}^{-1}$. (a) With $[\mathrm{A}]_{0}=0.0075 \mathrm{M}$, how long does it take for $[\mathrm{A}]$ to drop to 0.0018 M ? Calculate the half-life of the reaction for $[\mathrm{A}]_{0}$ $=0.0075 \mathrm{M}$ and for $[\mathrm{A}]_{0}=0.0025 \mathrm{M}$.

Solution:
$\frac{1}{[\mathrm{~A}]_{t}}=k t+\frac{1}{[\mathrm{~A}]_{0}} \Rightarrow k t=\frac{1}{[\mathrm{~A}]_{t}}-\frac{1}{[\mathrm{~A}]_{0}} \Rightarrow t=\frac{1}{k[\mathrm{~A}]_{t}}-\frac{1}{k[\mathrm{~A}]_{0}}$
$t=\frac{1}{\left(32 M^{-1} \mathrm{~s}^{-1}\right)(0.0018 M)}-\frac{1}{\left(32 M^{-1} \mathrm{~s}^{-1}\right)(0.0075 M)}=17.36 \mathrm{~s}-4.17 \mathrm{~s}$
$=13.2 \mathrm{~s}$. For the half-life,
$t_{1 / 2}=\frac{1}{\left(32 M^{-1} \mathrm{~S}^{-1}\right)(0.0075 \mathrm{M})}=4.17 \mathrm{~s}$
$t_{1 / 2}=\frac{1}{\left(32 M^{-1} \mathrm{~S}^{-1}\right)(0.0025 M)}=12.5 \mathrm{~s}$

Zeroth Order Reactions
A zeroth order reaction is independent of reactant concentration: For $\mathrm{AA} \rightarrow$ products, rate $=k[\mathrm{~A}]^{0}=k$.

Once again, we redefine the rate constant to include the stoichiometric coefficient and write
$-\frac{\Delta[\mathrm{A}]}{\Delta t}=k$
Now we change $\Delta$ to $d$ (finite change to infinitesimal change):
$-\frac{d[\mathrm{~A}]}{d t}=k \Rightarrow d[\mathrm{~A}]=-k d t$
Then we integrate from $t=0$ to $t=t$
$\int_{[\mathrm{A}]_{0}}^{[\mathrm{A}]_{t}} d[\mathrm{~A}]=-k \int_{0}^{t} d t \Rightarrow[\mathrm{~A}]_{t}-[\mathrm{A}]_{0}=-k t$ or $[\mathrm{A}]_{t}=-k t+[\mathrm{A}]_{0}$


A plot of $[A]$ versus time yields a straight line with slope $-k$ and intercept $[A]_{0}$

| TABLE 19.5 | Summary of the Kinetics of Zeroth-Order, First-Order, <br> and Second-Order Reactions |  |
| :---: | :---: | :---: |
| Order | Rate law | Integrated rate law |
| 0 | rate $=k$ | $[\mathrm{~A}]_{t}=-k t+[\mathrm{A}]_{0}$ |
| 1 | rate $=k[\mathrm{~A}]$ | $\ln \frac{[\mathrm{A}]_{t}}{[\mathrm{~A}]_{0}}=-k t$ |
| 2 | rate $=k[\mathrm{~A}]^{2}$ | $\frac{1}{[\mathrm{~A}]_{t}}=k t+\frac{1}{[\mathrm{~A}]_{0}}$ |

## Dependence of Reaction Rate on Temperature

Reactions almost always occur faster at higher temperature. Quantified by the Arrhenius Equation for the rate constant $k=A e^{-E_{a} / R T}$

A = frequency factor
$\mathrm{E}_{\mathrm{a}}=$ activation energy
$\mathrm{R}=$ gas constant $=8.314 \mathrm{~J} \mathrm{~K}^{-1} \mathrm{~mol}^{-1}$
$\mathrm{T}=$ temperature (in K)
Increase $\mathrm{E}_{\mathrm{a}}$ : decrease $k$ Increase T : increase $k$

Take the logarithm of the Arrhenius Equation:
$\ln k=\ln A-\frac{E_{a}}{R T}$
(used $\ln x y=\ln x+\ln y)$
$\ln (\mathrm{k}) \mathrm{S}_{\text {slope }=-\mathrm{E}_{\mathrm{a}} / \mathrm{R}}^{\ln (\mathrm{A})}$
We can obtain the activation energy and the frequency factor from a plot of $\ln k$ versus $1 / \mathrm{T}$.

Now, consider two different temperatures:
$\ln k_{1}=\ln A-\frac{E_{a}}{R T_{1}}(1) \quad$ and $\quad \ln k_{2}=\ln A-\frac{E_{a}}{R T_{2}}(2)$
Subtract (1) - (2) to obtain
$\ln \frac{k_{1}}{k_{2}}=\frac{E_{a}}{R}\left(\frac{1}{T_{2}}-\frac{1}{T_{1}}\right)$
e.g., Determine $\mathrm{E}_{\mathrm{a}}$, and also k at 655 K , from the data:

| $T(K)$ | $k\left(\mathrm{~s}^{-1}\right)$ |
| :--- | :--- |
| 625 | $1.1 \times 10^{-4}$ |
| 635 | $1.5 \times 10^{-4}$ |
| 645 | $2.0 \times 10^{-4}$ |

## Solution:

From the first two data points,

$$
\begin{aligned}
& \ln \frac{1.1}{1.5}=\frac{E_{a}}{R}\left(\frac{1}{635 \mathrm{~K}}-\frac{1}{625 \mathrm{~K}}\right) \Rightarrow-0.31=\left(E_{a} / R\right)\left(-2.52 \times 10^{5} \mathrm{~K}^{-1}\right) \\
& E_{a}=(-0.31)\left(8.314 \mathrm{~J} \mathrm{~K}^{-1} \mathrm{~mol}^{-1}\right) /\left(-2.52 \times 10^{5} \mathrm{~K}^{-1}\right)=102.3 \mathrm{~kJ} / \mathrm{mol}
\end{aligned}
$$

Then, using $\mathrm{T}=645 \mathrm{~K}$ and $\mathrm{T}=655 \mathrm{~K}$, we have
$\ln \frac{2.0}{k}=\frac{102.3 \times 10^{3} \mathrm{~J} \mathrm{~mol}^{-1}}{8.314 \mathrm{~J} \mathrm{~K}^{-1} \mathrm{~mol}^{-1}}\left(\frac{1}{655 \mathrm{~K}}-\frac{1}{645 \mathrm{~K}}\right)=-0.291$
$\Rightarrow \ln 2.0 \times 10^{-4}-\ln k=-0.291 \Rightarrow \ln k=-8.226$
$\Rightarrow \quad k=e^{-8.226}=2.7 \times 10^{-4}$

## Reaction Mechanisms

- Most reactions occur in a series of steps
- The balanced equation does not tell us how the reaction occurs!
- The series of steps is the reaction mechanism

Consider the reaction $2 \mathrm{NO}(g)+\mathrm{O}_{2}(g) \rightarrow 2 \mathrm{NO}_{2}(g)$
This reaction cannot occur as written because

1. The simultaneous collision of 3 molecules is unlikely
2. $\mathrm{N}_{2} \mathrm{O}_{2}$ is detected during the course of the reaction

Possible mechanism:
elementary rxn 1: $\quad \mathrm{NO}+\mathrm{NO} \rightarrow \mathrm{N}_{2} \mathrm{O}_{2} \quad$ (slow)
elementary rxn 2: $\quad \mathrm{N}_{2} \mathrm{O}_{2}+\mathrm{O}_{2} \rightarrow 2 \mathrm{NO}_{2} \quad$ (fast)
The elementary reactions must add up to give the overall rxn. Rate determining step: slowest step in the rxn mechanism (elementary step with the largest activation energy)


Step 1 (slow) is the rate determining step (highest activation energy).
$\mathrm{N}_{2} \mathrm{O}_{2}$ is called an intermediate because

1. It appears in the mechanism but not in the balanced Eq.
2. It is produced in one step and consumed in a later step.

For each elementary reaction, the rate law is given by the stoichiometry coefficients:
elementary rxn 1: $\quad \mathrm{NO}+\mathrm{NO} \rightarrow \mathrm{N}_{2} \mathrm{O}_{2} \quad$ (slow) rate $_{1}=k_{1}[\mathrm{NO}]^{2}$
elementary rxn 2: $\quad \mathrm{N}_{2} \mathrm{O}_{2}+\mathrm{O}_{2} \rightarrow 2 \mathrm{NO}_{2} \quad$ (fast) rate $_{2}=k_{2}\left[\mathrm{~N}_{2} \mathrm{O}_{2}\right]\left[\mathrm{O}_{2}\right]$

The rate law of the rate-determining step must be equal to the overall reaction rate law.

For $2 \mathrm{NO}(g)+\mathrm{O}_{2}(g) \rightarrow 2 \mathrm{NO}_{2}(g)$ this is: rate $=k[\mathrm{NO}]^{2}$

For the reaction $\mathrm{H}_{2}+2 \mathrm{ICI} \rightarrow 2 \mathrm{HCl}+\mathrm{I}_{2}$ the experimentally determined rate law $=k[\mathrm{H} 2][I \mathrm{Cl}]$.

What reaction mechanism is consistent with this information?

$$
\begin{array}{lll}
\text { elementary rxn 1: } & \mathrm{H}_{2}+\mathrm{ICl} \rightarrow \mathrm{HCl}+\mathrm{HI} & \text { (slow) } \\
\text { elementary rxn 2: } & \mathrm{HI}+\mathrm{ICI} \rightarrow \mathrm{HCl}+\mathrm{I}_{2} & \text { (fast) }
\end{array}
$$

e.g., Propose a plausible mechanism for the reaction $A+2 B \rightarrow C+D$ given that the rate law is $k[A][B]$

Solution:
elementary rxn 1: $\quad A+B \rightarrow C+E \quad$ (slow)
elementary rxn 2: $\quad B+E \rightarrow D \quad$ (fast)

## Mechanisms with a Fast First Step

Consider the reaction $2 \mathrm{NO}(g)+\mathrm{Cl}_{2}(g) \rightarrow 2 \mathrm{NOCl}(g)$ with experimentally determined rate $=\mathrm{k}\left[\mathrm{NO}^{2}\left[\mathrm{Cl}_{2}\right]\right.$.

One possibility is that this reaction is an elementary step. But this is unlikely because it would require 3 molecules simultaneously colliding.

A more plausible mechanism is
elementary rxn 1: $\quad \mathrm{NO}+\mathrm{Cl}_{2} \rightarrow \mathrm{NOCl}_{2}$
elementary rxn 2: $\quad \mathrm{NOCl}_{2}+\mathrm{NO} \rightarrow 2 \mathrm{NOCl}$
(slow)

The overall rate law is given by the rate-determining step, which gives rate $=k\left[\mathrm{NOCl}_{2}\right][\mathrm{NO}]$

But this rate expression contains an intermediate, $\mathrm{NOCl}_{2}$. We need an expression that only contains the reactants, or else we can't compare to the experimental rate law.

Since $\mathrm{NOCl}_{2}$ is produced quickly and consumed slowly, it reaches a steady state concentration, and the first (fast) step establishes a dynamic equilibrium (forward = backward rate).

We express this as:

$$
\begin{gathered}
\mathrm{NO}+\mathrm{Cl}_{2} \underset{k_{-1}}{\stackrel{k_{1}}{\rightleftharpoons}} \mathrm{NOCl}_{2} \\
\mathrm{NOCl}_{2}+\mathrm{NO} \xrightarrow{k_{2}} 2 \mathrm{NOCl}
\end{gathered}
$$

The dynamic equilibrium is
$k_{1}[\mathrm{NO}]\left[\mathrm{Cl}_{2}\right]=k_{-1}\left[\mathrm{NOCl}_{2}\right]$
which lets us express
$\left[\mathrm{NOCl}_{2}\right]=\frac{k_{1}}{k_{-1}}[\mathrm{NO}]\left[\mathrm{Cl}_{2}\right]$
The rate law is then:
rate $=k_{2}\left[\mathrm{NOCl}_{2}\right][\mathrm{NO}]=\frac{k_{2} k_{1}}{k_{-1}}[\mathrm{NO}]^{2}\left[\mathrm{Cl}_{2}\right]$
e.g., The reaction $\mathrm{H}_{2}+\mathrm{I}_{2} \rightarrow 2 \mathrm{HI}$ proceeds via a 2-step mechanism in which the rate law for the rate-determining step $=k\left[H_{2}\right]\left[[]^{2}\right.$. Write the mechanism and rewrite the rate law using only reactant concentrations.

Solution:
$\begin{array}{ll}\text { elementary rxn } 1: & \mathrm{I}_{2} \underset{k_{-1}}{\stackrel{k_{1}}{\rightleftharpoons}} 2 \mathrm{I} \quad \text { (fast) } \\ \text { elementary rxn 2: } & \mathrm{H}_{2}+2 \mathrm{I} \stackrel{k_{2}}{\rightleftharpoons} 2 \mathrm{HI} \quad \text { (slow) }\end{array}$

The dynamic equilibrium is $k_{1}\left[\mathrm{I}_{2}\right]=k_{-1}[\mathrm{I}]^{2}$
so that $[\mathrm{I}]^{2}=\frac{k_{1}}{k_{-1}}\left[\mathrm{I}_{2}\right] \Rightarrow$ rate $=\frac{k_{2} k_{1}}{k_{-1}}\left[\mathrm{H}_{2}\right]\left[\mathrm{I}_{2}\right]$

## Catalyst:

In the presence of iodide ions $\left(\mathrm{I}^{-}\right)$, the decomposition of hydrogen peroxide speeds up.

Overall rxn: $\quad 2 \mathrm{H}_{2} \mathrm{O}_{2}(a q) \rightarrow 2 \mathrm{H}_{2} \mathrm{O}(I)+\mathrm{O}_{2}(g)$
Experimental rate law $=k\left[\mathrm{H}_{2} \mathrm{O}_{2}\right]\left[{ }^{-}\right]$
elementary rxn 1: elementary rxn 2 :

$$
\begin{array}{ll}
\mathrm{H}_{2} \mathrm{O}_{2}+\mathrm{I}^{-} & \rightarrow \mathrm{H}_{2} \mathrm{O}+\mathrm{IO}^{-} \\
\mathrm{H}_{2} \mathrm{O}_{2}+\mathrm{IO}^{-} & \rightarrow \mathrm{H}_{2} \mathrm{O}+\mathrm{O}_{2}+\mathrm{I}^{-} \tag{fast}
\end{array}
$$

Recall that $\mathrm{IO}^{-}$is called an intermediate because

1. It appears in the mechanism but not in the balanced Eq.
2. It is produced in one step and consumed in a later step.

What about the iodide ion?

1. It, also, does not appear in the balanced Eq.
2. It is consumed in one step and produced in a later step.

It is present at the start of the rxn, and it is present at the end. It is called a catalyst. Its function is to speed up the reaction.

| $\begin{array}{\|l\|l} \hline \text { 진 } \\ \stackrel{\rightharpoonup}{\omega} \\ \text { w } \end{array}$ | Reactants |  |
| :---: | :---: | :---: |
| A catalyst lowers the activation energy for a chemical reaction. |  |  |

## Types of Catalysts

Heterogeneous catalysts: The reactants and catalyst are in different phases. The catalyst is often a solid (with a high surface area).
These are extremely important in industrial chemistry.
Homogeneous catalysts: The reactants and catalyst are in the same phase.

Enzyme catalysts: biological catalysts (in living cells)


