

UNIVERSITY OF TEXAS AT DALLAS  
Telecommunications Engineering  
*TE3302 Signals & Systems*  
Fourier Transform and Sampling

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*Answers to the practice problem set for the final exam.*

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F.1  $X(j\omega) = \frac{1}{j\omega + b}$

(a)  $V(j\omega) = \frac{e^{j4\omega/5}}{j\omega + 5b}$

(b)  $V(j\omega) = \frac{2}{(j\omega + b)^3}$

(c)  $V(j\omega) = \frac{1}{j(\omega - 1) + b}$

(d)  $V(j\omega) = \frac{1}{2j(\omega - 4) + b} + \frac{1}{2j(\omega + 4) + b}$

(e)  $V(j\omega) = \frac{-\omega^2}{j\omega + b}$

(f)  $V(j\omega) = \frac{1}{(j\omega + b)^2}$

(g)  $V(j\omega) = -2\pi e^{-b\omega} u(\omega)$

F.2 (a)  $x(t) = \frac{6}{\pi} \cos \omega t - \frac{4}{\pi} \sin 2\omega t$

(b)  $x(t) = 0.5\delta(t - 4) + 0.5\delta(t + 4)$

(c)  $x(t) = e^{-2t+3}u(t - 1.5) - e^{-2t+5}u(t - 2.5)$

(d)  $x(t) = 1.5(e^{-2t}u(t) + e^{-4t}u(t))$

F.3 (a)  $X(j\omega) = -4je^{-j\omega} \frac{\sin^2 \omega/2}{\omega}$

(b)  $X(j\omega) = 2 \frac{\sin 3\omega/2}{\omega} e^{-j\omega/2} + 2 \frac{\sin \omega}{\omega}$

F.4  $y(t) = 2 \cos \omega_0 t + 3 \sin 2\omega_0 t$

F.5 (a)  $w_s$  (Nyquist frequency or rate) =  $8,000\pi$

(b)  $w_s$  (Nyquist frequency or rate) =  $2,000\pi$