

MIDTERM II-Solutions

EE/TE4367 Telecommunications Switching & Transmission

SPRING 2007, Prof. Murat Torlak

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Problem 1. General, 30 points

- (a) The bandwidth-distance factor of a fiber system resulting from chromatic dispersion is determined from the fiber dispersion coefficient and the spectral width of the source. *(Fill up the blank)*
- (b) SONET defines optical carrier (OC) levels and electrically equivalent synchronous transport signal levels for the fiber-optic-based transmission hierarchy.
- (c) What is the purpose of building SONET in ring architecture? What are two basic types of the rings?

Network Survivability

Unidirectional Ring

Bidirectional Ring

- (d) Two plesiochronous digital networks, A and B, utilize cesium beam clocks accurate to ± 3 parts in 10^{13} . The networks are operated by independent long-distance companies and are synchronized to each other by means of a UTC signal. If a company leases a T1 line, which is terminated at one end in network A and at the other end in network B, how often must the networks be resynchronized to each other to avoid a framing bit error in the customer's T1 signal in the worst case? *Hint:* You may assume that a framing bit error occurs when the two networks are out of synchronization by $\geq 1/2$ of a T1 "bit time".

$$\text{A T1 bit time} = \frac{1}{1.544 \times 10^6} = 6.47668 \times 10^{-7} \text{ sec/bit}$$

6 parts in 10^{13} or 6×10^{-13} errored bits per bit transmitted

$$\frac{6.47668 \times 10^{-7}}{6 \times 10^{-13}} \text{ errored bits per bit} = 1.07945 \times 10^6 \text{ seconds per errored bit}$$

Or, 5.39273×10^5 seconds per errored half bit = 149.92 hrs.

Problem 2. Fiber Optics Transmission (30 points)

| Optical Source | | | |
|----------------|-----------------|-----------------------------|--------------------------|
| Device Type | Wavelength (nm) | Launched Output Power (dBm) | FWHM Spectrum Width (nm) |
| Ge LED | 1300 | -19 | 100 |

| Optical Detector | | | |
|---------------------|-----------------|-----------------------------|------------------|
| Device Type | Wavelength (nm) | Launched Output Power (dBm) | Data Rate (Mbps) |
| inGaAs <i>p-i-n</i> | 1300 | -35 | 100 |

A 1300-nm, graded-index, single-mode, 100 Mbps fiber system with 0.5 dB/km loss in the fiber is to be used for a token-passing bus local area network. Assume the system uses the source-detector pair above. The BDP of the fiber is 800 Mbps-km.

(a) What is the total loss margin (or budget) of the system?

$$\text{Loss Budget} = -19 \text{ dBm} - (-35 \text{ dBm}) = 16 \text{ dB}$$

(b) Find the distance limit of the system.

$$\text{BDP} = 800 \text{ Mbps-km} = D \times 100 \text{ Mbps}$$

$$D = 8 \text{ km}$$

(c) How many passive taps with 0.5 dB of loss can be inserted per kilometer without affecting the distance between transmitter and receiver?

$$0.5 \text{ dB/km} \times 8 \text{ km} = 4 \text{ dB loss due to fibre}$$

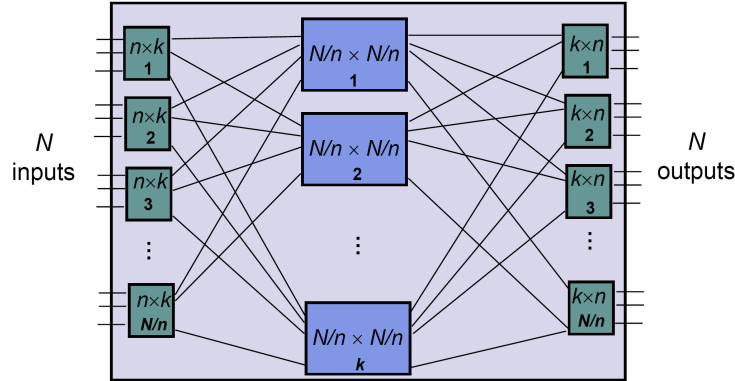
$$16 \text{ dB} - 4 \text{ dB} = 12 \text{ dB loss left}$$

$$\text{No. of taps} = \frac{12 \text{ dB}}{0.5 \text{ dB}} = 24 \text{ taps}$$

$$\text{No. of taps/km} = \frac{24}{8} = 3 \text{ taps/km}$$

Problem 3. Multistage Switch (40 points)

You are asked to design a three-stage space switch as shown below with 256 inputs. Blocking should be less than 0.002 and the channel utilization is given as 0.1652.



- (a) Find n (the size of each inlet-outlet group) if the number of $N/n \times N/n$ center-stage arrays is $k=9$, What is the number of inlet arrays (first stage)? *Hint: Valid solution of n , when rounded to the closest integer, has to make N/n an integer.*

$$p = 0.1652 \quad N = 256 \quad B = 0.002 \quad \beta = \frac{k}{n}$$

$$B = (1 - (1 - p')^2)^k \quad p' = \frac{p}{\beta} = \frac{pn}{k}$$

$$\Rightarrow 0.002 = \left(1 - \left(1 - 0.1652 \times \frac{n}{9}\right)^2\right)^9$$

$$\sqrt[9]{0.002} = 1 - \left(1 - 0.1652 \times \frac{n}{9}\right)^2$$

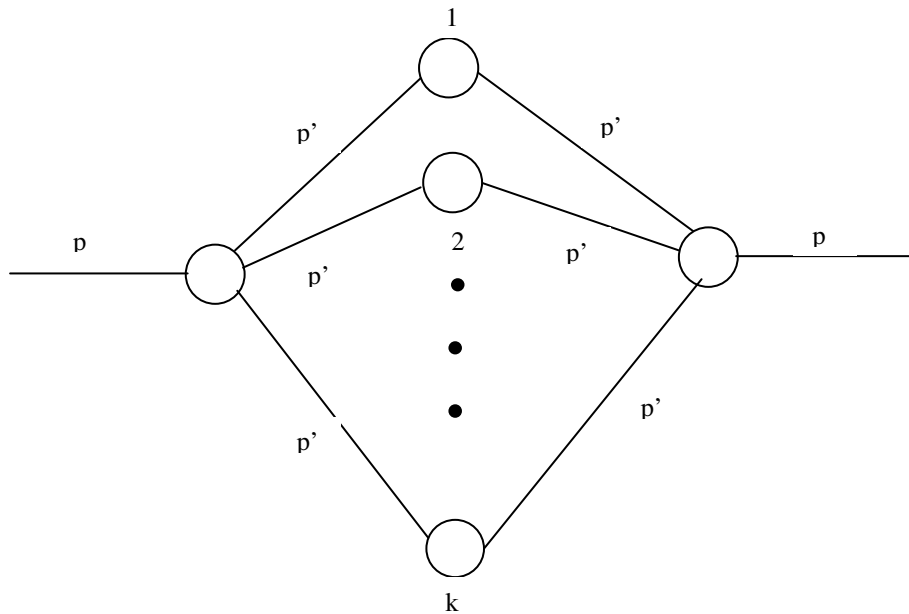
$$\Rightarrow \frac{(0.1652)^2 n^2}{81} - \frac{0.3304}{9} n + \sqrt[9]{0.002} = 0$$

$$n \in \{16, 92.95\} \quad \text{valid solution } n = 16$$

$$\frac{N}{n} = \frac{256}{16} = 16 \text{ (integer)}$$

$$\therefore \frac{N}{16} = 16 \text{ inlet arrays.}$$

(b) Draw the probability of the three-stage switch described above.
Carefully label probabilities on the graph.



$$p' = p \left(\frac{n}{k} \right)$$

(c) Find the total number of crosspoints required by the three-stage switched design in part (a).

$$\begin{aligned} N_x &= 2 \times \frac{N}{n} \times n \times k + k \times \frac{N}{n} \times \frac{N}{n} \\ &= 2 \times 16 \times 16 \times 9 + 9 \times \frac{(256)^2}{(16)^2} = 6912 \end{aligned}$$

(d) If a three-stage space switch is designed with $n=8$, what should be the value of k for a strictly nonblocking operation? Compare the complexity of this non-blocking switch to the blocking switch complexity in part (c).

$$k = 2n - 1 = 15$$

$$\begin{aligned} N_x &= 2 \times 32 \times 8 \times 15 + 15 \times (32)^2 \\ &= 23040 \quad (\text{much higher than part (c)}). \end{aligned}$$